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# 1 Paramagnetic Spin Hall Magnetoresistance

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24 We report the observation of the spin Hall magnetoresistance (SMR) in a  
25 paramagnetic insulator. By measuring the transverse resistance in a Pt/Gd<sub>3</sub>Ga<sub>5</sub>O<sub>12</sub>  
26 (GGG) system at low temperatures, paramagnetic SMR is found to appear with an  
27 intensity that increases with the magnetic field aligning GGG's spins. The observed  
28 effect is well supported by a microscopic SMR theory, which provides the parameters  
29 governing the spin transport at the interface. Our findings clarify the mechanism of spin  
30 exchange at a Pt/GGG interface, and demonstrate tunable spin-transfer torque through  
31 the field-induced magnetization of GGG. In this regard, paramagnetic insulators offer a  
32 key property for future spintronic devices.

33 Spintronics [1,2] aims to add new functionalities to the conventional electronics using  
34 interconversion of spin angular momentum between different carriers in solids. Especially, the  
35 spin exchange between conduction-electron spins in a normal metal (NM) and magnetization,  
36  $\mathbf{M}$ , in a ferromagnet (FM) is a central topic to the branch of spintronics trying to manipulate  
37  $\mathbf{M}$  for developing new types of magnetic memory devices [3,4]. When spin angular  
38 momentum is transferred into a FM through a NM/FM interface [Fig. 1(a)], it modifies the  
39 transverse dynamics of  $\mathbf{M}$  by exerting two types of torque, known as spin-transfer  
40 (damping-like) torque [5,6] and field-like torque [7], while it hardly couples to the  
41 longitudinal component. This is because the magnetic susceptibility in spin order, such as FM,  
42 is anisotropic due to the broken rotational symmetry reflecting spontaneous  $\mathbf{M}$ ; the magnetic  
43 susceptibility is large (small) along the transverse (longitudinal) direction, resulting in  
44 anisotropy into the spin injection.

45 The efficiency of the transverse spin injection has been characterized by the spin-mixing

46 conductance  $G_{\uparrow\downarrow}$  [8,9]. Its evaluation is of crucial importance in spintronics as  $G_{\uparrow\downarrow}$  governs the  
47 device performance [10]. To this end, the spin Hall magnetoresistance (SMR) [11-21] can be a  
48 powerful tool. SMR is a resistance modulation effect in NM caused by a spin-current flow in  
49 NM and spin injection across a NM/FM interface. So far, SMR has been detected in NMs  
50 with various ordered (ferri-, ferro-, and antiferro-) magnets [11-21], which quantified  $G_{\uparrow\downarrow}$  in  
51 the magnets. SMR has also been reported in some paramagnetic systems [22-25], but the  
52 mechanism of the effects has not been elucidated.

53 In this Letter, we demonstrate spin Hall magnetoresistance in a paramagnetic insulator (PI)  
54  $\text{Gd}_3\text{Ga}_5\text{O}_{12}$  (GGG), with a NM (Pt) contact. Unlike ordered magnets, a paramagnet has no  
55 spontaneous magnetization and shows huge longitudinal susceptibility. At the interface,  
56 conduction-electron spins in the NM couple not only to the transverse component  
57 (spin-transfer and field-like torque) but also to the longitudinal component of spins in PI  
58 through the interfacial spin-flip process [Fig. 1(b)], whose efficiency is characterized by the  
59 effective spin conductance (or spin-sink conductance)  $G_s$  [9,26-29]; both  $G_{\uparrow\downarrow}$  and  $G_s$  are  
60 crucial for spin exchange at NM/PI interfaces. First, we show evidence of the paramagnetic  
61 SMR in Pt/GGG through transverse resistivity measurements. By combining experimental  
62 and theoretical results, we then evaluate  $G_{\uparrow\downarrow}$  and  $G_s$ , and demonstrate that these spin  
63 conductances are controllable with external magnetic fields  $B$ . Such controllability in  
64 paramagnets is distinct from SMR in ordered magnets, highlighting the novelty of the  
65 paramagnetic SMR.

66 The sample consists of a Pt Hall bar (thickness  $d = 5$  nm, width  $w = 100$   $\mu\text{m}$ , and length  $l =$   
67  $800$   $\mu\text{m}$ ) on a single-crystalline GGG (111) slab. We measured longitudinal and transverse

68 resistivity  $\rho_L = wdR_L/l$  and  $\rho_T = dR_T$ , where  $R_L = V_L/J_c$  ( $R_T = V_T/J_c$ ) is the Pt longitudinal  
69 (transverse) resistance [15] (see Appendix A) by applying current  $J_c$  of typical amplitude of  
70 200  $\mu\text{A}$  using a DC reversal method [30] with applying  $B$  up to 9 T.

71 Figure 1(c) shows the temperature ( $T$ ) dependence of  $M$  of the GGG slab measured by a  
72 vibrating sample magnetometer. The  $M$ - $T$  curve follows the Curie-Weiss law down to 2 K  
73 with a very low Curie-Weiss temperature  $\theta_{\text{CW}} = -2$  K.  $M$  arises from  $\text{Gd}^{3+}$  spins ( $S = 7/2$ ),  
74 which are coupled via a weak exchange interaction [31] of 0.1 K. Because of the half-filled  
75  $4f$ -shell in  $\text{Gd}^{3+}$ , the orbital angular moment is zero, leading to the very small magnetic  
76 anisotropy of 0.04 K [31], which makes GGG an ideal paramagnetic system.

77 We have investigated paramagnetic SMR in a Pt/GGG junction system shown in Fig 1(d).  
78 SMR originates from a combination of the direct and inverse spin Hall effects (SHE and  
79 ISHE) [32-34]. When the charge current  $\mathbf{J}_c$  is applied to the Pt layer, SHE creates a  
80 conduction-electron spin current,  $\mathbf{J}_s$ , with the spin polarization  $\sigma$  flowing along the  $\sigma \times \mathbf{J}_c$   
81 direction. When the spin current  $\mathbf{J}_s$  reaches the interface, it is reflected back into the Pt layer  
82 and again converted into a charge current via ISHE, causing the modulation of the Pt  
83 resistivity  $\rho_{\text{Pt}}$ . We can tune the reflected spin current and thereby  $\rho_{\text{Pt}}$  by the field-induced  
84 magnetization  $\mathbf{M} \sim \langle \mathbf{S}_{\parallel} \rangle$  of GGG. At the Pt/GGG interface, conduction-electron spins in Pt  
85 interact with the paramagnetic spins  $\mathbf{S}$  in GGG via the interface exchange interaction, that  
86 exerts torque on  $\mathbf{S}$ . This torque is maximal (minimal) when  $\sigma \perp \langle \mathbf{S}_{\parallel} \rangle$  ( $\sigma \parallel \langle \mathbf{S}_{\parallel} \rangle$ ), where the  
87 intensity of the reflected spin current and the resultant ISHE are suppressed (enhanced).  
88 Therefore,  $\rho_{\text{Pt}}$  becomes higher for  $\sigma \perp \langle \mathbf{S}_{\parallel} \rangle$  than for  $\sigma \parallel \langle \mathbf{S}_{\parallel} \rangle$ . Besides, the effective magnetic

89 field due to the interface exchange interaction affects the motion of conduction electrons in  
90 the Pt layer and gives an additional Hall component, referring to the spin Hall anomalous Hall  
91 effect (SHAHE) [12,15,16].

92 SMR measurements at low temperatures have been very difficult so far. This is because, at  
93 low  $T$  and high  $B$ , weak anti-localization (WAL) effects appear in magnetoresistance and  
94 mask SMR signals in a four-probe resistance method [35]. Indeed, we observed a clear WAL  
95 signal at  $T = 2.5$  K in  $\Delta\rho_L(B_i) = [\rho_L(B_i) - \rho_L(0)]/\rho_L(0)$ , where  $i = x, y, z$  in Fig. 2(e) **and**  
96 **discussed in Appendix B**. To overcome the problem, we measured *transverse* resistivity of the  
97 Pt layer [see Fig. 2(d)], in which WAL does not appear even under  $B$ ; the setup allows us to  
98 investigate magnetoresistance free from WAL at low  $T$  and high  $B$ .

99 Figure 2(b) shows the field dependent magnetoresistance (FDMR) amplitude  $\Delta\rho_T(B) =$   
100  $[\rho_T(B) - \rho_T(0)]/\rho_L(0)$  at 2 K with  $B$  at  $\alpha = 45^\circ$ , where the transverse SMR becomes the most  
101 prominent. The  $B$ -rotation angle  $\alpha$  is defined in Fig. 2(d). We observed clear  
102 magnetoresistance at  $\alpha = 45^\circ$ , in sharp contrast with the result at  $\alpha = 0$ . The observed  
103 magnetoresistance increases for  $|B| < 5$  T, while it is saturated for  $|B| > 5$  T. The  $B$  range, at  
104 which  $\Delta\rho_T(B)$  is saturated is similar to that of  $M$  [see Fig. 2(a)], suggesting the field-induced  
105 paramagnetism plays a dominant role.

106 SMR can be discussed in terms of the  $\alpha$  dependence, which is phenomenologically given by  
107  $\cos(\alpha)\sin(\alpha)$  for the transverse component [11,12]. Figure 3(b) shows the angular dependent  
108 magnetoresistance (ADMR) of  $\Delta\rho_T$  at 2 K by changing  $\alpha$  at  $|B| = 3.5$  T [see Fig. 3(d)].  $\Delta\rho_T(\alpha)$   
109 shows a clear  $\cos(\alpha)\sin(\alpha)$  feature, consistent with the transverse SMR scenario. Figure 3(f)  
110 shows the ADMR results at several  $B$  values, which are well described by

111  $S_{\text{SMR}}^{\text{ADMR}}(B)\cos(\alpha)\sin(\alpha)$  (except for  $B = 0$ ).  $S_{\text{SMR}}^{\text{ADMR}}(B)$  is plotted in Fig. 3(a) (purple circles),  
 112 showing good agreement with the FDMR result (blue solid line),  $S_{\text{SMR}}^{\text{FDMR}} = \Delta\rho_{\text{T}}(45^\circ) -$   
 113  $\Delta\rho_{\text{T}}(135^\circ)$ . The Hanle magnetoresistance (HMR) may cause a similar signal [36]. Figure 2(f)  
 114 shows the  $B$  dependence of HMR,  $L_{\text{HMR}}(B) = [\rho_{\text{L}}(B_x) - \rho_{\text{L}}(B_y)]/\rho_{\text{L}}(0)$  at 300 K. We confirmed  
 115 no meaningful signal from HMR at 300 K in our sample. The same claim can be made at 2 K  
 116 because HMR weakly depends on  $T$  [36,37] (see details in Appendix C). We thus conclude  
 117 that the observed FDMR and ADMR are the experimental signatures of the paramagnetic  
 118 SMR.

119 We found that the paramagnetic SMR manifests itself even in longitudinal resistivity  
 120 measurements. Figure 3(c) shows the ADMR amplitude  $\Delta\rho_{\text{L}}(\alpha) = [\rho_{\text{L}}(\alpha) - \rho_{\text{L}}(90^\circ)]/\rho_{\text{L}}(0)$  at 2  
 121 K and  $|B| = 3.5$  T [see Fig. 3(e)].  $\Delta\rho_{\text{L}}(\alpha) = [\rho_{\text{L}}(\alpha) - \rho_{\text{L}}(90^\circ)]/\rho_{\text{L}}(0)$  is described by  
 122  $L_{\text{SMR}}^{\text{ADMR}} \cos^2(\alpha)$ , consistent with the expected behavior of SMR, i.e., the higher (lower)  
 123 resistivity for  $\mathbf{J}_{\text{c}}\parallel\mathbf{B}$  ( $\mathbf{J}_{\text{c}}\perp\mathbf{B}$ ). Except for  $B = 0$ , similar  $\cos^2(\alpha)$  dependence was confirmed at  
 124 several  $B$  values [Fig. 3(g)], and  $L_{\text{SMR}}^{\text{ADMR}}(B)$  matches  $S_{\text{SMR}}(B)$  [Fig. 3(a)]. Therefore, even  
 125 from the longitudinal FDMR results, we successfully discerned the paramagnetic SMR from  
 126 the WAL background signals (see Appendix D for further discussion).

127 We briefly argue the  $\alpha$ ,  $\beta$ , and  $\gamma$  dependence of  $\Delta\rho_{\text{L}}$  in Figs. 4(a) and (b). In contrast to  
 128  $\Delta\rho_{\text{L}}(\alpha)$ , large WAL signals appear in  $\Delta\rho_{\text{L}}(\beta)$  and  $\Delta\rho_{\text{L}}(\gamma)$ , which deviate from a  $\cos^2$   
 129 dependence. The phenomenology of SMR and WAL explains the results as  $\Delta\rho_{\text{L}}(\alpha)$ : SMR  
 130 only,  $\Delta\rho_{\text{L}}(\beta)$ : SMR + WAL, and  $\Delta\rho_{\text{L}}(\gamma)$ : WAL only. We indeed found  $\Delta\rho_{\text{L}}(\beta) - \Delta\rho_{\text{L}}(\gamma) \sim$   
 131  $\Delta\rho_{\text{L}}(\alpha)$ . Therefore, all the ADMR results are ascribable to WAL and the paramagnetic SMR.

132 Figure 4(c) shows  $S_{\text{SMR}}^{\text{ADMR}}(T)$  at  $|B| = 3.5$  T.  $S_{\text{SMR}}$  shows the maximum value at 2 K and  
 133 monotonically decreases with increasing  $T$ , resembling  $M$ - $T$  of GGG [the inset to Fig. 4(c)].  
 134 The results again show the field-induced  $M$  is important to generate  $S_{\text{SMR}}$ , consistent with the  
 135 paramagnetic SMR scenario.

136 Figure 2(c) shows  $\Delta\rho_T(B)$  measured with applying  $B||z$  [sketch in the inset to Fig. 2(c)].  
 137 After subtracting the  $B$ -linear ordinary Hall effect (OHE) component, we found a small  
 138  $B$ -nonlinear signal  $S_{\text{SHAHE}}$  for  $|B| < 5$  T at 2 K. For positive (negative)  $B$ , a positive (negative)  
 139 signal appears; this  $B$ -odd dependence is characteristic of SHAHE [12,15,16,18]. With  
 140 increasing  $B$ ,  $S_{\text{SHAHE}}$  increases and is saturated at around 5 T, concomitant with the saturation  
 141 of  $M$  in GGG [Fig. 2(a)]. We confirmed the higher-order SHAHE [16] is negligible (see  
 142 Appendix E).

143 We apply a microscopic SMR theory [26] valid for NM/PI with the  $B$ -dependent  
 144 magnetization instead of the phenomenological SMR theory [12] for NM/FM with the  
 145 spontaneous  $B$ -independent magnetization, leaving the  $B$  dependence of SMR unexplained.  
 146 We describe the spin current  $\mathbf{J}_s$  at the NM/PI interface resulting from the interfacial exchange  
 147 interaction by using the boundary condition [9,26,28] written as

$$148 \quad -e\mathbf{J}_s = G_r\mathbf{n} \times (\mathbf{n} \times \boldsymbol{\mu}_s) + G_i\mathbf{n} \times \boldsymbol{\mu}_s + G_s\boldsymbol{\mu}_s, \quad (1)$$

149 where  $e$  is the elementary charge,  $\mathbf{n}$  the unit vector of  $\mathbf{B}$ ,  $\boldsymbol{\mu}_s$  the spin accumulation in the NM  
 150 side,  $G_{\uparrow\downarrow}=G_r+iG_i$  the spin-mixing conductance, and  $G_s$  the effective spin conductance. The  
 151 first and second terms in the right-hand side of Eq. (1) correspond to the spin-transfer and  
 152 field-like torque, respectively, and the third indicates the spin-flip (electron-magnon)

153 scattering, which accounts for the magnon-related unidirectional SMR [38-40]. We calculate  
 154 the spin conductances in Eq. (1) for the NM/PI interface as

$$155 \quad G_r(B) = A_1 \left\{ S(S+1) - \left[ \coth(\xi/2) + \frac{\xi}{4\sinh^2(\xi/2)} \right] SB_S(S\xi) \right\}, \quad (2)$$

$$156 \quad G_t(B) = A_2 SB_S(S\xi), \quad (3)$$

$$157 \quad G_s(B) = -A_1 \frac{\xi}{2\sinh^2(\xi/2)} SB_S(S\xi), \quad (4)$$

158 where  $B_S(x)$  is a Brillouin function of spin- $S$  as a function of  $x$ ,  $\xi(B) = C_1 B [T / (T - \Theta_{\text{CW}}^{\text{eff}})]$ ,  
 159  $\Theta_{\text{CW}}^{\text{eff}}$  the effective Curie-Weiss temperature, which contains  $\Theta_{\text{CW}}$ ,  $S = 7/2$  the electron spin of  
 160 a  $\text{Gd}^{3+}$  ion, and  $C_1$  a numerical constant.  $A_{1,2}$  are fitting parameters, which contain the  
 161 interface spin density  $n_{\text{PI}}$  and dimensionless interfacial  $s$ - $f$  exchange interaction  $J_{\text{int}}$ . Finally,  
 162 the magnetoresistance as a function of  $B$  is given by:

$$163 \quad S_{\text{SMR}}(B) = D_1 \{ \mathcal{R}(G_s) - \text{Re}[\mathcal{R}(G_s - G_{\uparrow\downarrow})] \}, \quad (5)$$

$$164 \quad S_{\text{SHAHE}}(B) = D_1 \text{Im}[\mathcal{R}(G_s - G_{\uparrow\downarrow})], \quad (6)$$

165 where  $\mathcal{R}(x) = (1 - D_2 x) / (1 - D_3 x)$ , and  $D_{1,2,3}$  are known numerical constants. **We refer**  
 166 **Appendices F to I for theoretical details.** We obtained the best fits using Eqs. (5) and (6)  
 167 simultaneously as shown in Fig. 5(a) with the values of  $n_{\text{PI}} = 6.94 \times 10^{16}$  Gd atom/m<sup>2</sup>,  $\Theta_{\text{CW}} =$   
 168 **-1.27** K, and  $J_{\text{int}} = -0.13$ . Although a direct fit to  $S_{\text{SMR}}(T)$  is not possible by simply considering  
 169  $M(T)$ , our model fully explains  $S_{\text{SMR}}(B, T)$ , in which  $T$  dependences of the spin-transport  
 170 parameters of the Pt film and effects from a paramagnetic subsystem are also taken into  
 171 account (see Appendix J for further discussion).

172 Figure 5(b) shows  $G_r(B)$ ,  $G_i(B)$ , and  $G_s(B)$  with the estimated parameter values. At zero  
 173 magnetic field,  $G_r$  and  $G_i$  vanish, while  $|G_s|$  takes the maximum value of  $8.7 \times 10^{12}$  S/m<sup>2</sup>. By  
 174 increasing  $B$ , both  $G_r$  and  $|G_i|$  monotonically increases, but  $|G_i|$  increases more rapidly than  $G_r$ ,  
 175 and  $G_r$  ( $|G_i|$ ) approaches the value of  $1.0 \times 10^{13}$  S/m<sup>2</sup> ( $7.4 \times 10^{12}$  S/m<sup>2</sup>) at around 5 T (3 T). On  
 176 the other hand,  $|G_s|$  monotonically decreases with  $B$  and approaches zero.

177 The  $B$ -dependent spin transport at the interface is a unique feature of paramagnets, in sharp  
 178 contrast to FM where  $G_{\uparrow\downarrow}$  is almost independent of  $B$ . At the NM/PI interface, all the torque is  
 179 cancelled out with the randomized spin ( $\langle S_{\parallel} \rangle = 0$ ) at  $B = 0$ , resulting in  $G_r = G_i = 0$ . When the  
 180 PI acquires a net magnetization with applying  $B$ , a positive  $G_r$  and negative  $G_i$  appear; the  
 181 latter implies antiferromagnetic  $s$ - $f$  interaction at the interface. On the other hand,  $|G_s|$  decreases  
 182 with  $B$  due to the Zeeman gap ( $\propto g\mu_B B$ , where  $g$  is the  $g$ -factor and  $\mu_B$  the Bohr magneton).

183 At small  $B$ , the localized spin can be easily flipped by spin and energy transfer between the  
 184 conduction electron and localized spin. By applying  $B$ , the degeneracy of the paramagnetic  
 185 spin is lifted to split into different energy levels by the Zeeman effect. Because the energy  
 186 scale of the SHE-induced spin-flip scattering is governed by  $k_B T$ , where  $k_B$  is the Boltzmann  
 187 constant, at 2 K it can be suppressed by increasing  $B$  (9 T for electrons corresponds to the  
 188 energy scale of 25 K), leading to the reduction of  $G_s$ .

189 Our results clarify the mechanism of SMR and SHAHE in paramagnets. By comparing  $S_{\text{SMR}}$ ,  
 190  $S_{\text{SHAHE}}$ ,  $G_r$ , and  $|G_i|$ , we found  $S_{\text{SMR}}(B) \propto G_r(B)$  and  $S_{\text{SHAHE}}(B) \propto |G_i(B)|$  in Figs. 5(e) and (f),  
 191 respectively. Because  $G_r$  and  $|G_i|$  represent the efficiencies of the spin-transfer and field-like  
 192 torque, respectively [Figs. 5(c) and (d)], the agreement indicates that the spin-transfer

193 (field-like) torque is the mechanism of SMR (SHAHE) in Pt/GGG. Furthermore, the  
194 agreement between the experiment and theory clarifies that SMR is attributed to the ensemble  
195 of paramagnetic moments, consistent with the scenario in other magnetic ordered systems.  
196 This contrasts with the conclusions of Ref. 25, in which the MR observed in non-crystalline  
197 paramagnetic YIG/Pt was attributed to the total magnetic moment. Our results thus unify the  
198 description of SMR in compensated ferrimagnets [41,42], antiferromagnets [19-21,43],  
199 ferromagnets [18], and paramagnets, resolving the longstanding controversy for the origin of  
200 SMR.

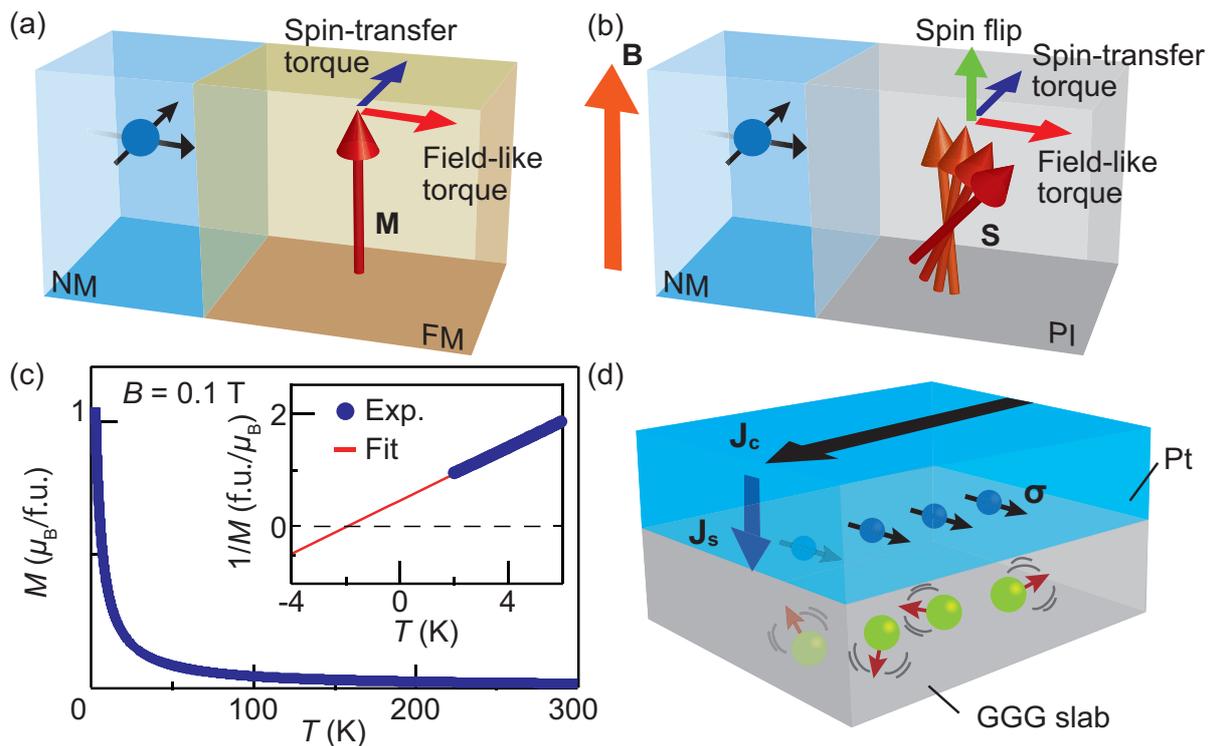
201 Finally, we discuss the interfacial parameters  $J_{\text{int}}$ ,  $n_{\text{PI}}$ , and  $\Theta_{\text{CW}}$ . We obtained a negative  
202 interfacial exchange interaction of about -2 meV (see Appendix I). This value has the same  
203 sign and order of magnitude as the one found in the Pt/EuS interface [18,44], -3~-4 meV,  
204 indicating the  $s$ - $f$  exchange coupling is antiferromagnetic in both systems. On the other hand,  
205 a negative  $G_i$  was found in W/EuO [45], corresponding to a positive (ferromagnetic)  $s$ - $f$   
206 exchange interaction. The sign of the exchange interaction in metallic compounds with  
207 rare-earth ions depends on the electron structure of the host metal and the type of the  
208 rare-earth ions [46], and so may do the interfacial exchange interaction. The estimated Gd  
209 atom density corresponds to only 1% of the bulk value for GGG. The depletion of Gd atoms  
210 at the interface is consistent with the smaller  $\Theta_{\text{CW}}$  of -1.27 K than the bulk value of -2 K,  
211 indicating the decrease of the exchange interaction among Gd atoms at the interface. The  
212 feature may be attributed to possible damage of the GGG surface crystallization during the Pt  
213 sputtering (see the TEM images in Appendix J).

214 In summary, we demonstrate the paramagnetic SMR in a Pt film on GGG at 2 K. The SMR

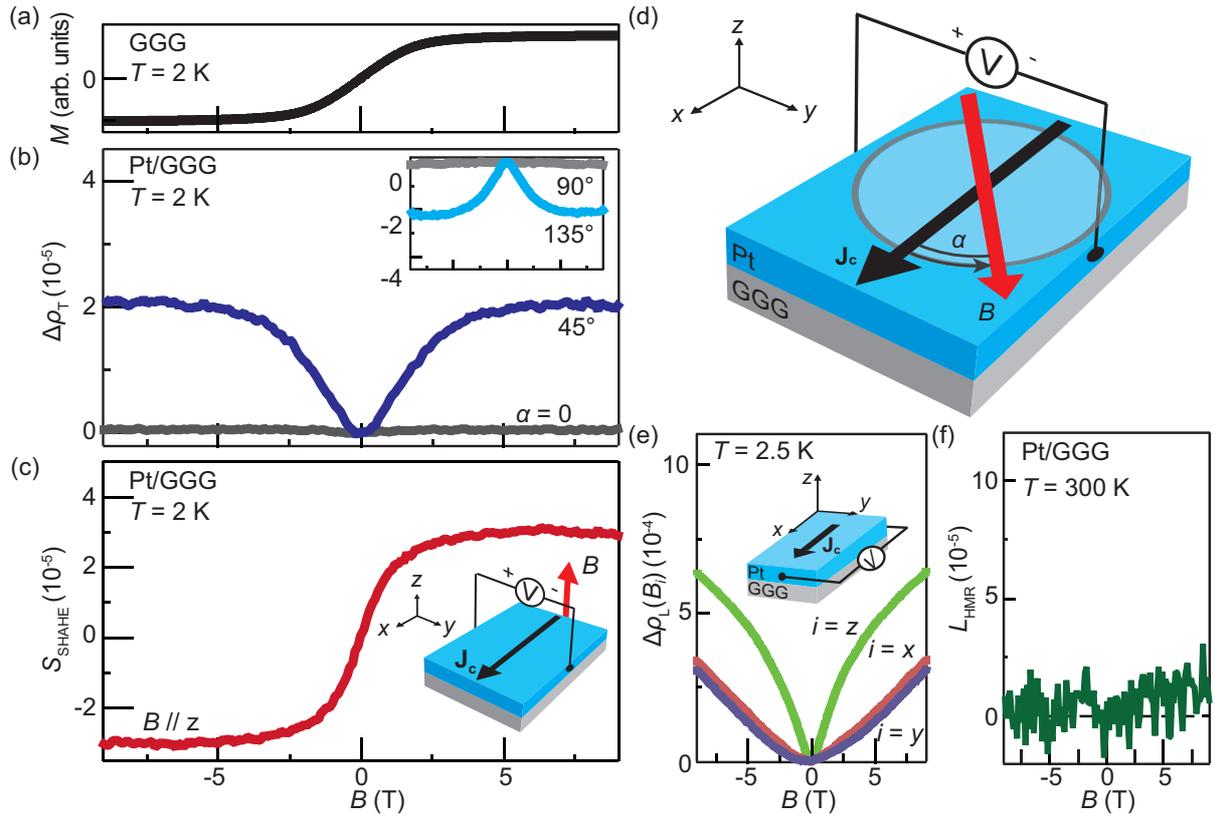
215 is induced with applying magnetic fields, and saturated above several tesla when all localized  
216 spins are aligned. The observed correlation between SMR/SHAHE and magnetization  
217 indicates that the field-induced magnetization plays a significant role in the spin transport at  
218 the Pt/GGG interface. Our microscopic theory well explains the SMR signals as a function of  
219 magnetic fields and quantifies the microscopic spin exchange parameters at the Pt/GGG  
220 interface. Our results indicate that the magnetoresistance measurements allow us to  
221 investigate spin transport at interfaces, essential for accelerating insulator-based spintronics.

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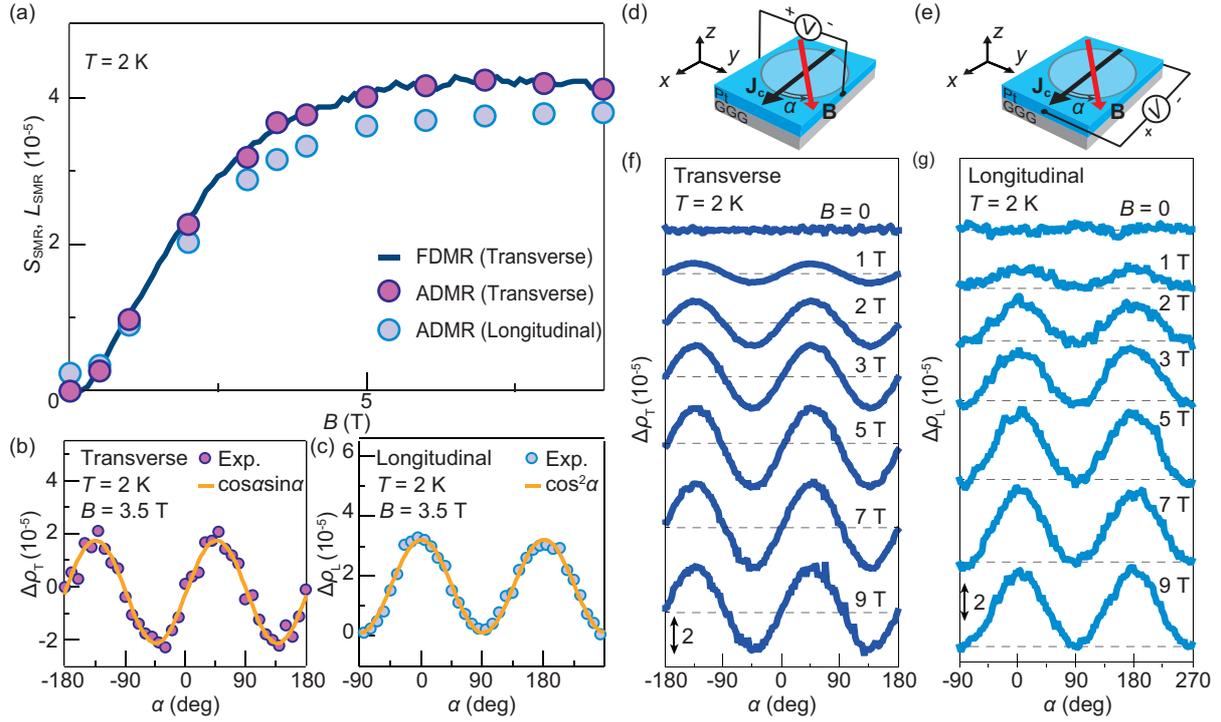
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241 FIG. 1. (a) NM/FM and (b) NM/PI interface with spin exchange. The blue, red, and  
 242 green arrows represent the directions of angular momentum related to the  
 243 spin-transfer torque, field-like torque, and spin-flip process, respectively. (c)  $M(T)$  of  
 244 GGG. The inset shows  $1/M$  (blue circles) and a linear fit (red solid line). (d) The  
 245 Pt/GGG interface.  $\mathbf{J}_s$  with  $\sigma$  is generated in Pt by SHE with the application of  $\mathbf{J}_c$ .



246  
 247 FIG. 2. (a)  $M(B)$  of GGG at 2 K. (b)  $\Delta\rho_T(B)$  at 2 K. The deep blue (grey) curve shows  
 248  $\Delta\rho_T$  with  $B$  at  $\alpha = 45^\circ$  ( $0^\circ$ ). The light blue (grey) curve in the inset shows  $\Delta\rho_T$  with  $B$  at  
 249  $\alpha = 135^\circ$  ( $90^\circ$ ). (c)  $S_{\text{SHAHE}}(B)$  with  $B \parallel z$  after subtracting the OHE component. The inset  
 250 shows the measurement setup for SHAHE. (d) Measurement setup for SMR. (e)  
 251  $\Delta\rho_L(B_i)$  in Pt/GGG at 2.5 K. The inset shows the measurement setup. (f)  $L_{\text{HMR}}(B)$  at  
 252 300 K in Pt/GGG.



253  
254

FIG. 3. (a)  $B$  dependence of the SMR signals obtained from FDMR and ADMR

255

measurements. The solid curve represents  $S_{\text{SMR}}^{\text{FDMR}}$ . The purple (blue) circles show

256

$S_{\text{SMR}}^{\text{ADMR}}$  ( $L_{\text{SMR}}^{\text{ADMR}}$ ) obtained via the fitting using  $S_{\text{SMR}}^{\text{ADMR}} \cos(\alpha)\sin(\alpha)$  [ $L_{\text{SMR}}^{\text{ADMR}} \cos^2(\alpha)$ ]. (b)

257

$\Delta\rho_T(\alpha)$  and (c)  $\Delta\rho_L(\alpha)$  at 2 K with rotating  $|B| = 3.5$  T. The orange solid curves in (b)

258

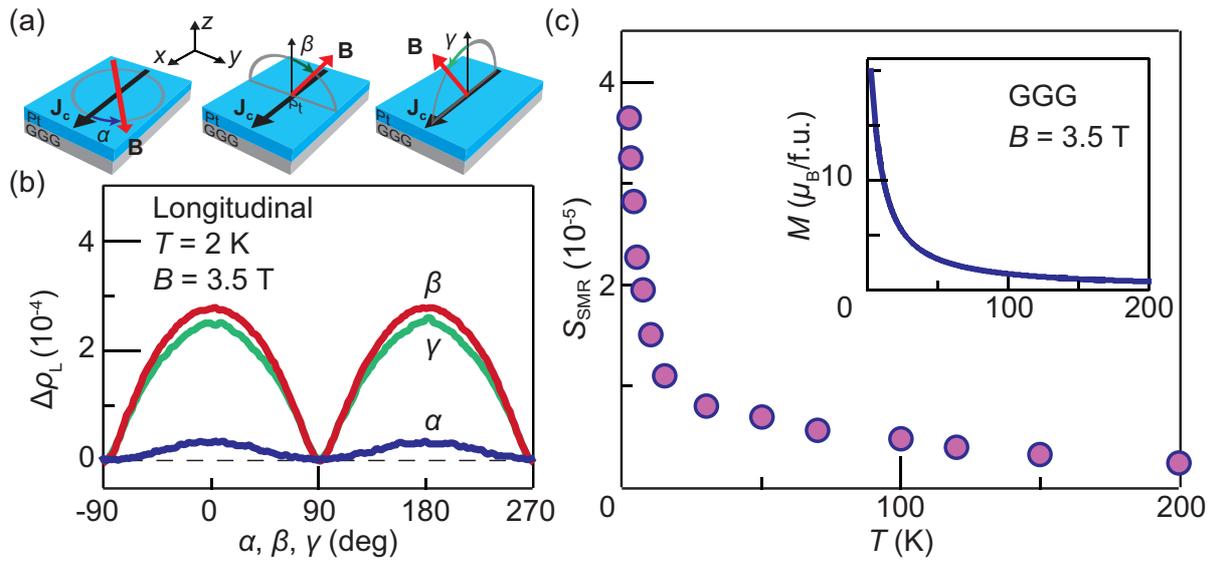
and (c) are a  $S_{\text{SMR}}^{\text{ADMR}} \cos(\alpha)\sin(\alpha)$  and  $L_{\text{SMR}}^{\text{ADMR}} \cos^2(\alpha)$  fit, respectively. (d),(e) **Schematic**

259

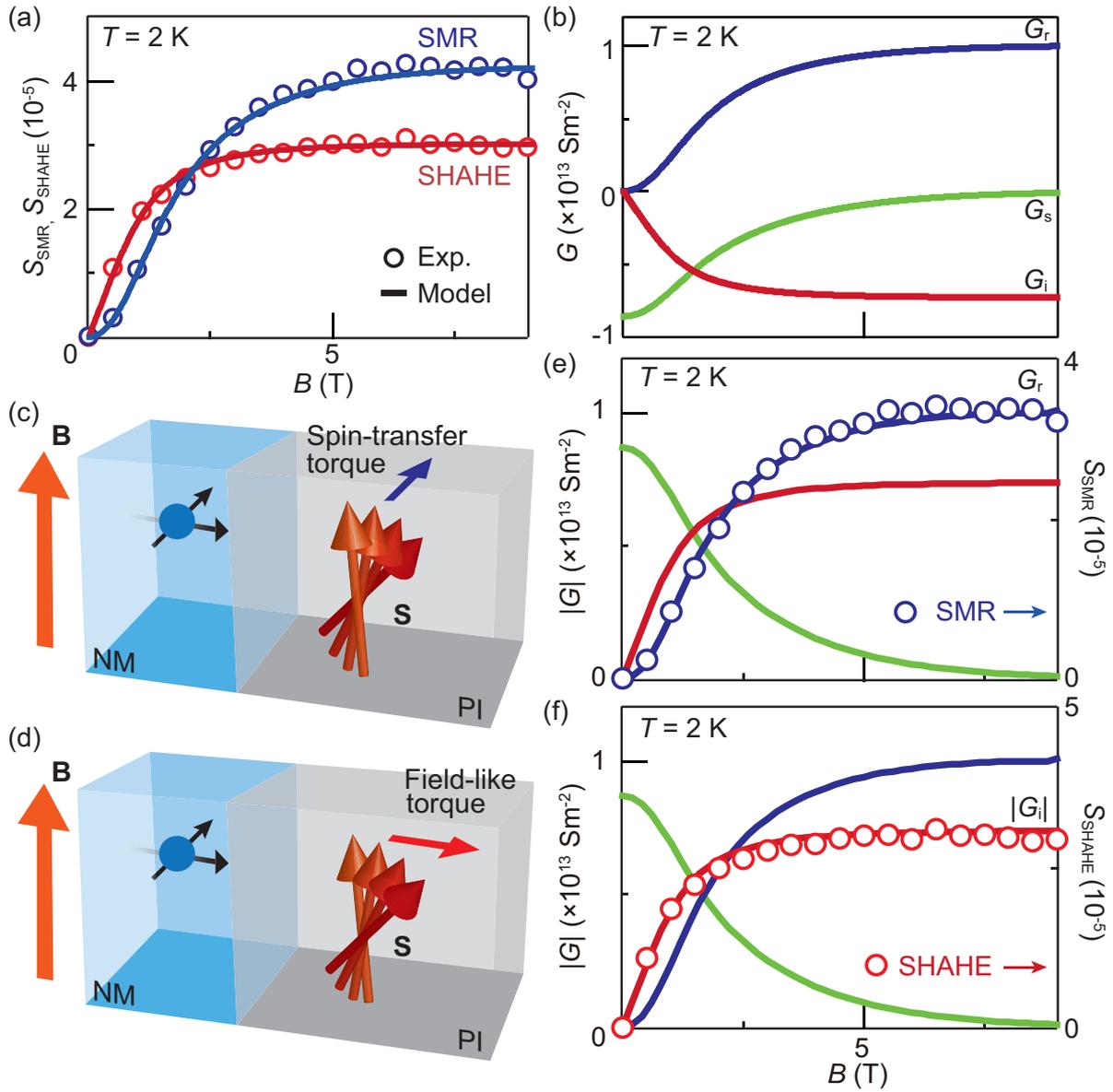
**illustrations of (d) the transverse and (e) longitudinal ADMR measurement setup. (f)**

260

**$\Delta\rho_T(\alpha)$  and (g)  $\Delta\rho_L(\alpha)$  at 2K for various  $B$ .**



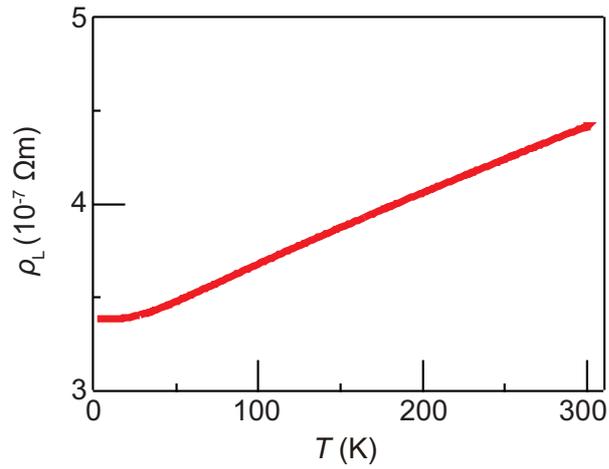
261 FIG. 4. (a) Schematic illustrations of the ADMR measurement setups. (b)  $\Delta\rho_L(\alpha)$ ,  
 262  $\Delta\rho_L(\beta)$ , and  $\Delta\rho_L(\gamma)$  data. (c)  $S_{SMR}^{ADMR}(T)$  at 3.5 T. The inset shows the  $M$ - $T$  curve of  
 263 GGG.



264 FIG. 5. (a)  $B$  dependence of SMR and SHAHE together with the fitting of Eqs. (5) and  
 265 (6) at 2 K. (b)  $B$  dependence of  $G_r$ ,  $G_i$ , and  $G_s$ . (c) Spin-transfer and (d) field-like  
 266 torque in a NM/PI system. (e),(f) The comparison (e) between  $G_r$  and SMR, and (f)  
 267 between  $|G_i|$  and SHAHE.

268 **APPENDIX A: TEMPERATURE DEPENDENCE OF PT RESISTIVITY**

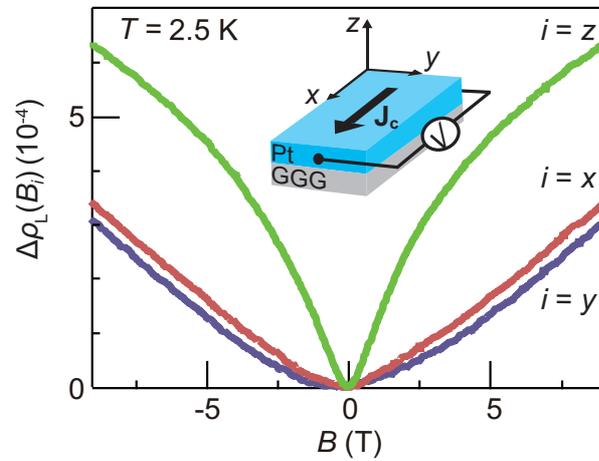
269 Figure 6 shows the temperature  $T$  dependence of the resistivity  $\rho_L(B = 0) = \rho_D$  of the Pt film  
270 on the GGG slab. We measured  $\rho_L$  by the conventional four-probe method with applying  
271 charge current of 200  $\mu\text{A}$ . Down to around 20 K,  $\rho_L$  linearly decreases with decreasing  $T$ .  
272 Below 10 K,  $\rho_L$  starts to increase, which is a signature of the weak anti-localization (WAL)  
273 effect [35].



274  
275 FIG. 6.  $T$  dependence of  $\rho_L$  of Pt. The resistivity  $\rho_L$  is measured in a 5-nm thickness Pt Hall bar on the  
276 GGG slab.

277 **APPENDIX B: WEAK ANTI-LOCALIZATION IN PT FILM**

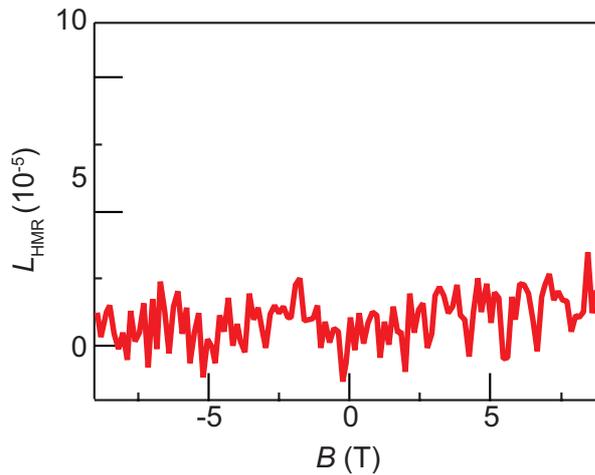
278 We measured magnetoresistance in the longitudinal configuration [35] for  $T < 50$  K to show  
 279 the weak anti-localization (WAL) effects in the Pt film. Figure 7 shows the normalized  
 280 longitudinal resistivity change  $\Delta\rho_L(B_i) = [\rho_L(B_i) - \rho_L(B_i = 0)]/\rho_L(B_i = 0)$  as a function of  $B$   
 281 in the  $i = x, y,$  and  $z$  directions (see the inset to Fig. 7) at 2.5 K.  $\Delta\rho_L(B_i)$  increases with  
 282 increasing  $B$  for all  $i$ , but their shapes differ with each other.  $\Delta\rho_L(B_z)$  increases more rapidly,  
 283 while  $\Delta\rho_L(B_x)$  and  $\Delta\rho_L(B_y)$  show similar trends. The largest value of  $\Delta\rho_L(B_z)$  at 9 T is two  
 284 times greater than those of  $\Delta\rho_L(B_x)$  and  $\Delta\rho_L(B_y)$ . Note that the difference between  $\Delta\rho_L(B_x)$  and  
 285  $\Delta\rho_L(B_y)$ ,  $\sim 4 \times 10^{-5}$  at 9 T, corresponds to the paramagnetic SMR (we discuss it in Appendix  
 286 D).  
 287



288 FIG. 7.  $B$  dependence of  $\Delta\rho_L(B_i)$  at 2.5 K. The red, blue and green curves indicate the  $B$  dependence of  
 289  $\Delta\rho_L(B_i)$  for  $B$  in the  $x, y$  and  $z$  directions, respectively. The inset shows the sample with the applied  
 290 current  $\mathbf{J}_c \parallel \mathbf{x}$ .

291 **APPENDIX C: HANLE MAGNETORESISTANCE IN PT FILM**

292 We here show that the Hanle magnetoresistance (HMR) [36] is negligibly small in our  
293 Pt/GGG sample. As shown in Refs. 36 and 37, the HMR may show  $B$ -direction dependence  
294 similar to the SMR [i.e., HMR appears (disappears) under  $B$  in the  $x$  and  $z$  ( $y$ ) directions] and  
295 may show up in a wide temperature range from 300 K to 2 K, but weakly depends on  $T$ . To  
296 investigate the HMR in our sample, we measure the  $B$  dependence of the longitudinal  
297 resistivity at 300 K, where the HMR, if present in our sample, may only be detected, while the  
298 paramagnetic SMR is suppressed because of the negligibly small paramagnetic moment in  
299 GGG at such high temperatures. Figure 8 shows the  $B$  dependence of  $L_{\text{HMR}} = [\rho_L(B_x) -$   
300  $\rho_L(B_y)]/\rho_L(B = 0)$  at  $T = 300$  K. We found no magnetoresistance, indicating that the HMR is  
301 undetected in the present Pt/GGG system. We thus conclude that the HMR can be neglected  
302 in our sample in all the  $T$  range. The absence of the HMR in our Pt/GGG sample may be  
303 attributed to the Pt growth condition, the detail of which is discussed in Ref. 36.  
304



305 FIG. 8.  $B$  dependence of  $L_{\text{HMR}}$  at 300 K.

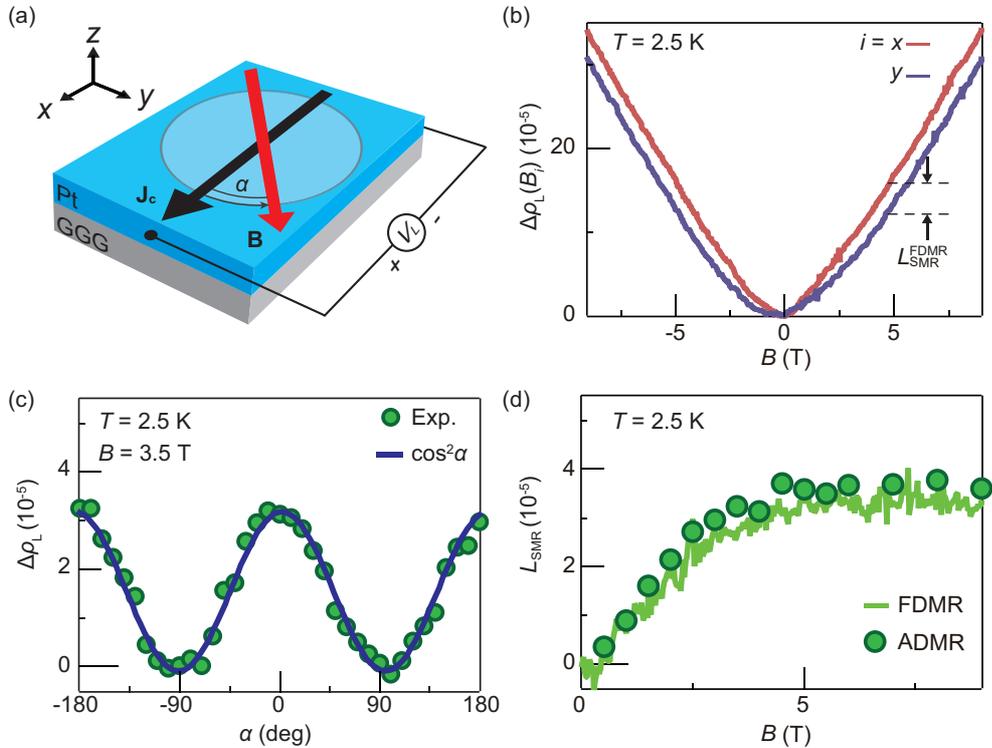
## 306 APPENDIX D: SMR IN LONGITUDINAL MEASUREMENTS IN PT/GGG

307 We show the paramagnetic SMR in the longitudinal configuration. We performed field  
308 dependent magnetoresistance (FDMR) measurements in the  $x$  and  $y$  directions and angular  
309 dependent magnetoresistance (ADMR) measurements in the  $x$ - $y$  plane [see Fig. 9(a)].

310 Figure 9(b) shows the  $B$  dependence of  $\Delta\rho_L(B_i) = [\rho_L(B_i) - \rho_L(B_i = 0)]/\rho_L(B = 0)$ , where  $i =$   
311  $x, y$  at 2.5 K. The overall behavior is ascribable to the WAL as discussed in Appendix B. We  
312 here address the small difference between  $\Delta\rho_L(B_x)$  and  $\Delta\rho_L(B_y)$ , defined as  $L_{SMR}^{FDMR}(B) =$   
313  $[\rho_L(B_x) - \rho_L(B_y)]/\rho_L(B = 0)$ . We plot the  $B$  dependence of  $L_{SMR}^{FDMR}$  as a green curve in Fig.  
314 9(d).  $L_{SMR}^{FDMR}(B)$  gradually increases and approaches to  $\sim 3 \times 10^{-5}$  at 5 T, similar to the  $B$   
315 dependence of  $M$  in GGG and the FDMR result in the transverse configuration shown in Figs.  
316 2(a) and 3(a).

317 Next, we investigate ADMR of the longitudinal resistivity in the  $x$ - $y$  plane. Figure 9(c) shows  
318 the  $\Delta\rho_L = [\rho_L(\alpha) - \rho_L(\alpha = 90^\circ)]/\rho_L(B = 0)$  as a function of  $\alpha$  at  $B = 3.5$  T and  $T = 2.5$  K.  
319  $\Delta\rho_T$  shows a clear  $L_{SMR}^{ADMR} \cos^2\alpha$  dependence, consistent with the behavior of the paramagnetic  
320 SMR. We extracted  $L_{SMR}^{ADMR}$  at various  $B$  and obtained the  $B$  dependence of the ADMR result  
321 shown in Fig. 9(d).  $L_{SMR}^{FDMR}$  and  $L_{SMR}^{ADMR}$  agree well with each other. All experimental findings  
322 in the longitudinal measurements are consistent with the observed SMR in the transverse  
323 measurements, showing that the difference between  $\Delta\rho_L(B_x)$  and  $\Delta\rho_L(B_y)$  [Fig. 9(b)] can be  
324 attributed to the paramagnetic SMR.

325



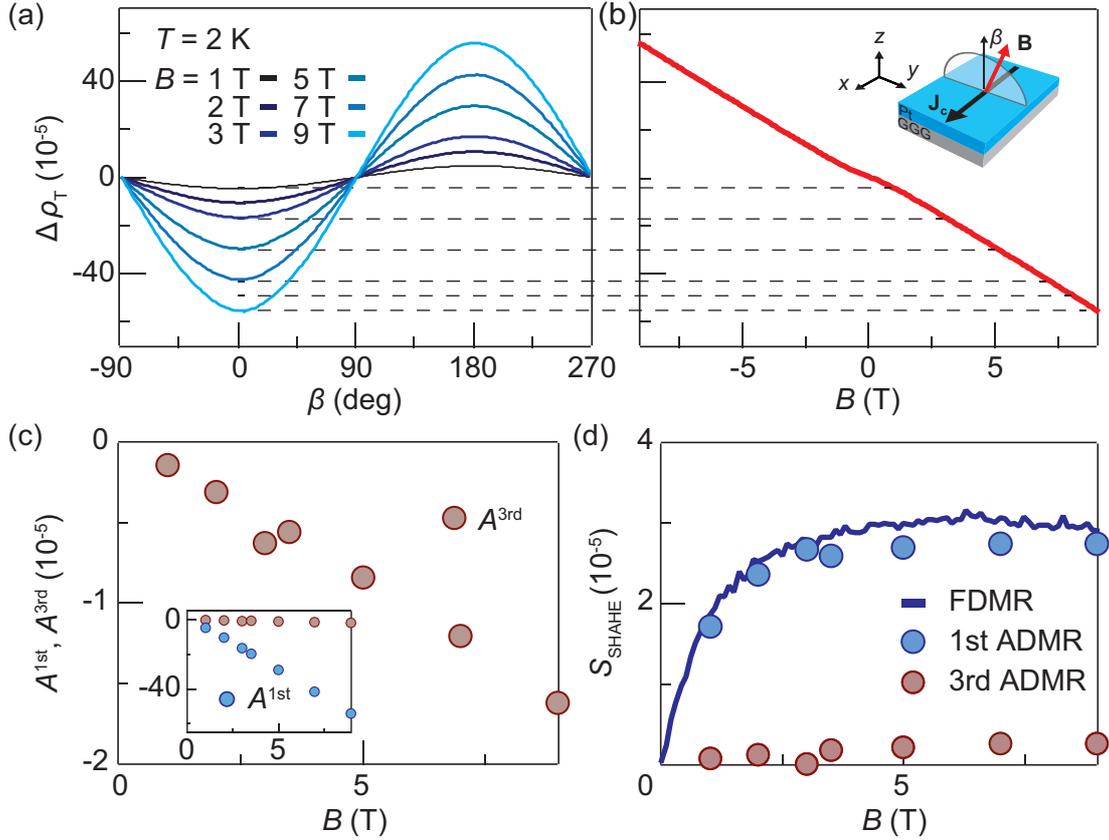
326 FIG. 9. (a) A schematic illustration of the longitudinal resistivity measurement. A charge current  $\mathbf{J}_c$  is  
327 applied in the  $x$  direction and the longitudinal voltage is measured.  $\mathbf{B}$  indicates the spatial direction of

328 the magnetic field, and the angle between  $\mathbf{J}_c$  and  $\mathbf{B}$  is defined as  $\alpha$ . (b) The field dependent  
329 magnetoresistance (FDMR) in the longitudinal measurement at 2.5 K. The red (blue) curve indicates  
330  $\Delta\rho_L$  under  $B$  in the  $x$  ( $y$ ) direction.  $L_{\text{SMR}}^{\text{FDMR}}(B)$  is defined as  $L_{\text{SMR}}^{\text{FDMR}}(B) = [\rho_L(B_x) - \rho_L(B_y)] / \rho_L(B = 0)$ . (c)  
331 The field angular dependent magnetoresistance (ADMR)  $\Delta\rho_L$  in the  $xy$ -plane. The green circles show  
332 the  $\alpha$  dependence of  $\Delta\rho_L$  at 2.5 K. The blue curve indicates a  $L_{\text{SMR}}^{\text{ADMR}} \cos^2\alpha$  fitting to the experimental  
333 result. (d) FDMR and ADMR results as a function of  $B$  at 2.5 K. The green curve (circles) shows the  
334 FDMR (ADMR) result of  $L_{\text{SMR}}$ .

## 335 APPENDIX E: SHAHE MEASUREMENT RESULT

336 Figure 10(a) shows the  $B$  dependence of the normalized Hall resistivity  $\Delta\rho_T(B)$  at 2 K for  
 337 Pt/GGG.  $\Delta\rho_T$  increases linearly with increasing  $B$  due to the ordinary Hall effect (OHE). We  
 338 estimated the slope of the OHE  $A_{\text{OHE}}$  as  $-6.5 \times 10^{-5}$  (1/T), using a linear fitting to  $\Delta\rho_T$  for the  $|B|$   
 339  $> 5$  T range and averaged the obtained slopes for  $-9 \text{ T} < B < -5 \text{ T}$  and  $5 \text{ T} < B < 9 \text{ T}$ . **The**  
 340 **obtained  $A_{\text{OHE}}$  in the 5-nm-thick Pt film is almost the same as that obtained in the 30-nm-thick**  
 341 **Pt film on GGG at low and high  $T$  [47]. The absence of the Pt thickness and  $T$  dependence of**  
 342  **$A_{\text{OHE}}$  indicates that the contribution from the other Hall effects induced by the influence of the**  
 343 **interface found in Pt/YIG is negligibly small [16,35,47].** After subtracting the OHE  
 344 component, we found the spin Hall anomalous Hall effect (SHAHE) signal shown in Fig.  
 345 2(c).

346 Here we show that the higher-order contribution of SHAHE [16] is negligible small in our  
 347 sample. Figure 10(b) shows the transverse ADMR at 2 K and selected magnetic fields. We  
 348 clearly observe a  $\cos\beta$  dependence of  $\Delta\rho_T$  because of the OHE [see Fig. 10(a)]. To evaluate  
 349 the higher-order contribution, we carried out the same analysis procedure used by Meyer et al.  
 350 [16]: fitting a  $A^{1\text{st}}\cos\beta + A^{3\text{rd}}\cos^3\beta$  function to the ADMR results shown in Fig. 10(b), where  
 351  $A^{1\text{st}}(B) = S_{\text{SHAHE}}^{1\text{st}}(B) + A_{\text{OHE}}^{1\text{st}} \cdot B$ ,  $S_{\text{SHAHE}}^{1\text{st}}(B)$  is the first-order SHAHE contribution as a  
 352 function of  $B$ ,  $A_{\text{OHE}}^{1\text{st}}$  is the coefficient of the OHE, and  $A^{3\text{rd}}(B) = S_{\text{SHAHE}}^{3\text{rd}}(B) + A_{\text{OHE}}^{3\text{rd}} \cdot B$  is the  
 353 higher-order contribution of the same Hall terms. Figure 10(c) shows the  $B$  dependence of  $A^{1\text{st}}$   
 354 (blue solid circles) and  $A^{3\text{rd}}$  (red solid circles).  $A^{1\text{st}}$  and  $A^{3\text{rd}}$  monotonically increase with  
 355 increasing  $B$  mainly due to the OHE,  $A_{\text{OHE}}^{1\text{st}}$  and  $A_{\text{OHE}}^{3\text{rd}}$ , respectively. We estimate the slope of  
 356 the OHE in the first- and high-order contribution as  $A_{\text{OHE}}^{1\text{st}} = -6.3 \times 10^{-5}$  (1/T) and  $A_{\text{OHE}}^{3\text{rd}} =$   
 357  $-2.1 \times 10^{-6}$  (1/T) using the results at  $B = 7$  T, and 9 T.  $A_{\text{OHE}}^{1\text{st}} = -6.3 \times 10^{-5}$  (1/T) is similar to that  
 358 estimated from the FDMR results [ $\sim -6.5 \times 10^{-5}$  (1/T)]. After subtracting the OHE, we show the  
 359  $B$  dependence of  $S_{\text{SHAHE}}^{1\text{st}}(B)$  and  $S_{\text{SHAHE}}^{3\text{rd}}(B)$  in Fig. 10(d). We found the first-order SHAHE  
 360 contribution [ $S_{\text{SHAHE}}^{1\text{st}}(B) \sim 2.7 \times 10^{-5}$  at 9 T] is about 10 times larger than the higher-order one  
 361 [ $S_{\text{SHAHE}}^{3\text{rd}}(B) \sim 0.26 \times 10^{-5}$  at 9 T] in our system. Furthermore,  $S_{\text{SHAHE}}^{1\text{st}}(B)$  from the ADMR  
 362 results is consistent with  $S_{\text{SHAHE}}(B)$  from the FDMR results [deep blue curve in Fig. 10(d),  
 363 and shown in the manuscript]. Therefore, we can accurately obtain the amplitude of the  
 364 first-order SHAHE from the FDMR result by subtracting the OHE component, justifying our  
 365 analysis described as above.



366 FIG. 10. (a)  $B$  dependence of  $\Delta\rho_T$  in the Hall measurement.  $\mathbf{J}_c$ ,  $\mathbf{B}$ , and  $\beta$  denote the spacial direction of  
 367 the charge current and magnetic field, and relative angle, respectively. The Hall resistivity is measured  
 368 at  $\beta = 0$  and  $T = 2$  K. (b) ADMR results of SHAHE at  $T = 2$  K and selected  $B$ . (c)  $B$  dependence of  $A^{3\text{rd}}$ .  
 369 The inset shows the  $B$  dependence of  $A^{1\text{st}}$  and  $A^{3\text{rd}}$ . The amplitude of  $A^{1\text{st}}$  and  $A^{3\text{rd}}$  are obtained by  
 370 fitting a  $A^{1\text{st}}\cos\beta + A^{3\text{rd}}\cos^3\beta$  function to the ADMR results shown in (b). (d)  $B$  dependence of the first-  
 371 and third-order SHAHE. The blue (red) plots show the first-order (third-order) SHAHE,  $S_{\text{SHAHE}}^{1\text{st}}$   
 372 ( $S_{\text{SHAHE}}^{3\text{rd}}$ ), obtained from the ADMR. The deep blue curve indicates  $S_{\text{SHAHE}}$  obtained from the FDMR  
 373 results.

374 **APPENDIX F: MOLECULAR FIELD APPROXIMATION FOR MAGNETIZATION**  
 375 **OF GGG**

376 GGG is an ideal Curie-paramagnet with a weak exchange interaction between spins of  
 377 neighboring Gd ions. Using the molecular field approximation, the thermal average of spin  
 378  $\langle m \rangle$  is calculated by the self-consistent equation [48]

$$379 \quad \langle m \rangle = -SB_S(SC_1B_{\text{eff}}/T), \quad (\text{F1})$$

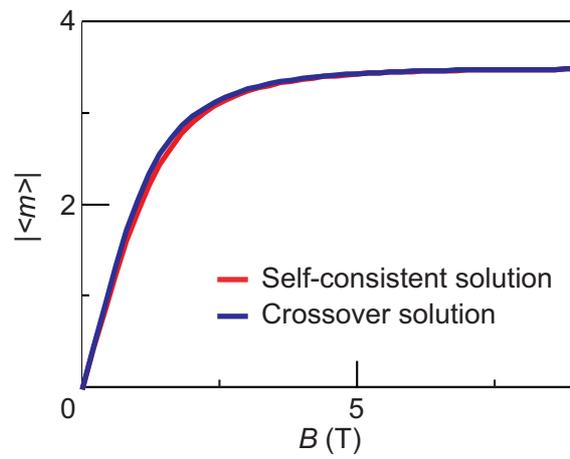
380 where  $S$  is the electron spin angular momentum of Gd ions,  $B_S(x)$  is the Brillouin function of  
 381 spin  $S$  as a function of  $x$ ,  $C_1 = g\mu_B/k_B$ ,  $g$  is the  $g$ -factor,  $\mu_B$  is the Bohr magneton,  $B_{\text{eff}} = B +$   
 382  $N_{\text{PI}}\langle m \rangle J_{\text{ex}}/g\mu_B$  is the effective field including the applied magnetic field  $B$  and the Weiss  
 383 molecular fields,  $k_B$  is the Boltzmann constant,  $T$  is the temperature,  $N_{\text{PI}}$  is the number of the  
 384 nearest neighbor of the interfacial magnetic moments and  $J_{\text{ex}}$  is the strength of the  
 385 antiferromagnetic exchange interaction among Gd ions.

386 We used the effective (renormalized) Curie-Weiss temperature  $\Theta_{\text{CW}}^{\text{eff}}$  for taking all the  
 387 correlation effects on a Gd ion into account, which gives the effective field as  $B_{\text{eff}} =$   
 388  $BT/(T - \Theta_{\text{CW}}^{\text{eff}})$ . The  $\Theta_{\text{CW}}^{\text{eff}}$  should recover the bare Curie-Weiss temperature  $\Theta_{\text{CW}}$  in the limit  
 389  $B \rightarrow 0$  and  $3T\Theta_{\text{CW}}/[C_1(S+1)B]$  in the limit  $B \rightarrow \infty$ , respectively. For practical purposes it is  
 390 convenient to match these limiting cases into a crossover function for the effective  
 391 Curie-Weiss temperature:

$$392 \quad \Theta_{\text{CW}}^{\text{eff}}(B) = \frac{3\Theta_{\text{CW}}B_S(S\xi)}{S+1\xi} \approx \begin{cases} \Theta_{\text{CW}} & (g\mu_B B/k_B T \ll 1) \\ \frac{3T}{C_1(S+1)B} \Theta_{\text{CW}} & (g\mu_B B/k_B T \gg 1) \end{cases}, \quad (\text{F2})$$

393 with the ansatz  $\xi = -a_0 + a_1|B| + \sqrt{a_0^2 + (a_2B)^2}$ , where  $a_0 = -3\Theta_{\text{CW}}/(S+1)T$ ,  $a_1 = C_1/(T - \Theta_{\text{CW}})$ ,  
 394 and  $a_2 = C_1/T(1 - T/\Theta_{\text{CW}})$ .

395 Figure 11 shows the plots of Eq. (F1) solved self-consistently (red line) and using with  $\Theta_{\text{CW}}^{\text{eff}}$   
 396 given as Eq. (F2) (the blue line). We find a good agreement between both curves, justifying  
 397 the use of  $\Theta_{\text{CW}}^{\text{eff}}$ . In the following discussion and the main text, the approximate form of  
 398  $B_{\text{eff}} = BT/(T - \Theta_{\text{CW}}^{\text{eff}})$  is used to analyze the data.



399 FIG. 11.  $B$  dependence of  $|\langle m \rangle|$ . The red and blue lines represent the self-consistent solution and the  
 400 approximation with the effective Curie-Weiss temperature solution for Eq. (F2), respectively.

401 **APPENDIX G: THEORY OF PARAMAGNETIC SMR**

402 Chen et al. formulated the spin Hall magnetoresistance (SMR) and spin Hall anomalous Hall  
 403 effect (SHAHE) in a normal metal (NM)/ferromagnetic insulator (FM) bilayer system in Ref.  
 404 12. They considered the NM/FM structure shown in Fig. 12(a) and solved a spin diffusion  
 405 equation with a boundary condition which describes spin transfer between a conduction  
 406 electron in NM and magnetization in FM at the interface. The longitudinal ( $\rho_L$ ) and transverse  
 407 resistivity ( $\rho_T$ ) of NM is given as

$$408 \quad \rho_L \approx \rho_D + \Delta\rho_0 + \Delta\rho_1(1 - n_y^2), \quad (\text{G1})$$

$$409 \quad \rho_T \approx \Delta\rho_1 n_x n_y + \Delta\rho_2 n_z, \quad (\text{G2})$$

410 with

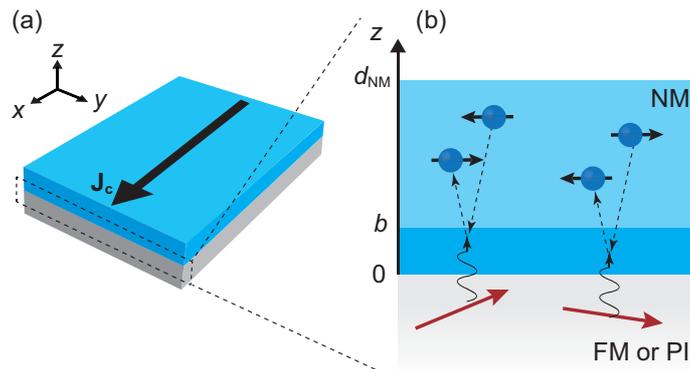
$$411 \quad \frac{\Delta\rho_0}{\rho_D} = -\theta_{\text{SH}}^2 \frac{2\lambda_{\text{NM}}}{d_{\text{NM}}} \tanh \frac{d_{\text{NM}}}{2\lambda_{\text{NM}}}, \quad (\text{G3})$$

$$412 \quad \frac{\Delta\rho_1}{\rho_D} = \theta_{\text{SH}}^2 \frac{\lambda_{\text{NM}}}{d_{\text{NM}}} \text{Re} \frac{2\lambda_{\text{NM}} G_{\uparrow\downarrow} \tanh^2 \frac{d_{\text{NM}}}{2\lambda_{\text{NM}}}}{\sigma_D + 2\lambda_{\text{NM}} G_{\uparrow\downarrow} \coth \frac{d_{\text{NM}}}{\lambda_{\text{NM}}}}, \quad (\text{G4})$$

$$413 \quad \frac{\Delta\rho_2}{\rho_D} = -\theta_{\text{SH}}^2 \frac{\lambda_{\text{NM}}}{d_{\text{NM}}} \text{Im} \frac{2\lambda_{\text{NM}} G_{\uparrow\downarrow} \tanh^2 \frac{d_{\text{NM}}}{2\lambda_{\text{NM}}}}{\sigma_D + 2\lambda_{\text{NM}} G_{\uparrow\downarrow} \coth \frac{d_{\text{NM}}}{\lambda_{\text{NM}}}}, \quad (\text{G5})$$

414 where  $\rho_D = 1/\sigma_D$  is the intrinsic electric resistivity of NM,  $\mathbf{n} = (n_x, n_y, n_z)$  is the unit vector of  
 415 the magnetization of FI,  $\theta_{\text{SH}}$  is the spin Hall angle of NM,  $\lambda_{\text{NM}}$  is the spin diffusion length of  
 416 NM,  $d_{\text{NM}}$  is the thickness of NM, and  $G_{\uparrow\downarrow} = G_r + iG_i$  is the complex spin mixing conductance  
 417 at the NM/FM interface. This formulation [G1 and G2] succeeded in describing the  
 418 experimental observation of SMR ( $\Delta\rho_1/\rho_D$ ) and SHAHE ( $\Delta\rho_2/\rho_D$ ) in NM/FM systems. They  
 419 modeled the coupling between conduction electron spin in NM and macroscopic  
 420 magnetization of FM, which is assumed to be independent of  $B$ .

421 In the following sections, we model the paramagnetic spin Hall magnetoresistance [26]. We  
 422 consider spin transfer at a paramagnetic insulator(PI)/NM interface via the interfacial  
 423 exchange interaction between a conduction electron spin in NM and localized spin (not  
 424 magnetization) in PI. As a result of the interaction, the spin relaxation time of the conduction  
 425 electron in NM becomes anisotropic, giving rise to the SMR and SHAHE as discussed below.  
 426 This approach clarifies the relation between the spin conductance and anisotropic spin  
 427 relaxation in NM, which is crucial to understand the paramagnetic SMR.



428 FIG. 12. (a) A schematic illustration of the NM/PI or NM/FM sample structure. We apply a charge  
 429 current,  $J_c$ , in the  $x$  direction. (b) A schematic side view of the interface. Conduction electron spins are  
 430 coupled to spins in PI in the deep blue region ( $0 < z < b$ ) with the thickness of  $b$ .  $d_{NM}$  is the thickness of  
 431 NM.

432 **APPENDIX H: CORRECTION FROM EFFECTIVE SPIN CONDUCTANCE AT THE**  
433 **INTERFACE**

434 First, we describe SMR with the boundary condition including the effective (longitudinal)  
435 spin conductance  $G_s$ .  $G_s$  characterizes the spin-flip process at the interface, which is neglected  
436 in a conventional NM/FM interface [12]. For the sake of completeness, we keep  $G_s$  in the  
437 boundary condition describing the spin current at the interface,

$$438 \quad -e\mathbf{J}_s = G_s \boldsymbol{\mu}_s + G_r \mathbf{n} \times (\mathbf{n} \times \boldsymbol{\mu}_s) + G_i \mathbf{n} \times \boldsymbol{\mu}_s, \quad (\text{H1})$$

439 where  $e$  is the elementary charge,  $\mathbf{J}_s$  is the spin current vector,  $\boldsymbol{\mu}_s$  is the spin accumulation  
440 vector at the NM/PI interface, and  $\mathbf{n} = \mathbf{B}/B$  is the unit vector of the applied magnetic field  $\mathbf{B}$ .  
441 By solving a one-dimensional spin diffusion equation in the  $z$  direction with the boundary  
442 condition [Eq. (H1)] at  $z = 0$  and the zero spin current at  $z = d_{\text{NM}}$ , we obtain the same form of  
443 the longitudinal and transverse resistivity with Eq. (G1) and (G2) but the different expressions  
444 of  $\Delta\rho_0/\rho_D$ ,  $\Delta\rho_1/\rho_D$ , and  $\Delta\rho_2/\rho_D$  as,

$$445 \quad \frac{\Delta\rho_0}{\rho_D} = 2\theta_{\text{SH}}^2 \left[ 1 - \frac{\lambda_{\text{NM}}}{d_{\text{NM}}} \tanh\left(\frac{d_{\text{NM}}}{2\lambda_{\text{NM}}}\right) \mathcal{R}(G_s) \right], \quad (\text{H2})$$

$$446 \quad \frac{\Delta\rho_1}{\rho_D} = \theta_{\text{SH}}^2 \frac{2\lambda_{\text{NM}}}{d_{\text{NM}}} \tanh\left(\frac{d_{\text{NM}}}{2\lambda_{\text{NM}}}\right) [\mathcal{R}(G_s) - \text{Re}[\mathcal{R}(G_s - G_{\uparrow\downarrow})]]$$

$$447 \quad = D_1 [\mathcal{R}(G_s) - \text{Re}[\mathcal{R}(G_s - G_{\uparrow\downarrow})]], \quad (\text{H3})$$

$$448 \quad \frac{\Delta\rho_2}{\rho_D} = \theta_{\text{SH}}^2 \frac{2\lambda_{\text{NM}}}{d_{\text{NM}}} \tanh\left(\frac{d_{\text{NM}}}{2\lambda_{\text{NM}}}\right) \text{Im}[\mathcal{R}(G_s - G_{\uparrow\downarrow})] = D_1 \text{Im}[\mathcal{R}(G_s - G_{\uparrow\downarrow})], \quad (\text{H4})$$

449 with

$$450 \quad \mathcal{R}(x) = \frac{1 - x\rho_D\lambda_{\text{NM}}\coth(d_{\text{NM}}/2\lambda_{\text{NM}})}{1 - 2x\rho_D\lambda_{\text{NM}}\coth(d_{\text{NM}}/\lambda_{\text{NM}})} = \frac{1 - D_2x}{1 - D_3x}, \quad (\text{H5})$$

451 where  $D_1 = \theta_{\text{SH}}^2 (2\lambda_{\text{NM}}/d_{\text{NM}}) \tanh(\lambda_{\text{NM}}/2d_{\text{NM}})$ ,  $D_2 = \rho_D \lambda_{\text{NM}} \coth(d_{\text{NM}}/2\lambda_{\text{NM}})$ , and  $D_3 =$   
452  $2\rho_D \lambda_{\text{NM}} \coth(d_{\text{NM}}/\lambda_{\text{NM}})$  are constants, which can be calculated using material parameters  
453 shown in the later.

454 Equations (H2)-(H4) describe the correction from  $G_s$ , and they are reduced to Eqs. (G3)-(G5)  
455 when  $G_s = 0$ , which corresponds to the same boundary condition used by Chen et al. [12].

456 **APPENDIX I: ANISOTROPIC SPIN RELAXATION DUE TO INTERFACIAL SPIN**  
 457 **EXCHANGE INTERACTION**

458 Next, we explain the relation between the interface spin conductances and the spin relaxation  
 459 times calculated for the conduction electron in the NM in close vicinity of the NM/PI  
 460 interface. We model the interface by introducing an auxiliary intermixing layer between the  
 461 NM and the PI with the thickness  $b$  and taking a  $b \rightarrow 0$  limit for calculation [26,49] of  $G_n$  and  
 462  $G_s$ . In such layer, dark blue region in Fig. 12(b), conducting electrons couple to the localized  
 463 spins in the PI via an interfacial exchange interaction. This interaction is described by the  
 464 effective Hamiltonian:

$$465 \quad \mathcal{H}_{\text{int}} = -J_{\text{int}} \sum_i \mathbf{S}_i \cdot \mathbf{s}(\mathbf{r}_i), \quad (11)$$

466 where  $J_{\text{int}}$  is the coupling constant,  $\mathbf{S}_i$  is the localized spin operator and  $\mathbf{s}(\mathbf{r}_i)$  is the spin  
 467 density of conduction electrons at position  $\mathbf{r}_i$ . The continuity equation for the spin current in  
 468 the interaction region  $0 < z < b$  reads

$$469 \quad \partial_t \mu_s^\alpha - \frac{1}{e v_F} \partial_i j_{s,i}^\alpha - \omega_L(\mathbf{r}) \epsilon_{\alpha\beta\gamma} n_\beta \mu_s^\gamma = -\Gamma_{\alpha\gamma} \mu_s^\gamma, \quad (12)$$

470 where the superscript Greek indices denote spin projections ( $\alpha, \beta, \gamma = x, y, z$ ), subscript Latin  
 471 ones (such as  $i = x, y, z$  but not the descriptor index "s") denote current directions,  $\mu_s^\alpha$  is the  
 472 spin accumulation polarized in the  $\alpha$  direction,  $v_F$  is the density of states at the Fermi level,  
 473  $j_{s,i}^\alpha$  is the spin current flowing in the  $i$  direction and spin-polarized in the  $\alpha$   
 474 direction,  $\omega_L = \omega_B - \delta_b(z) \langle \hat{S}_{\parallel} \rangle (n_{\text{PI}} J_{\text{int}} / \hbar)$  is the effective (renormalized) Larmor frequency,  
 475  $\omega_B = g \mu_B B / \hbar$  is the bare Larmor frequency,  $g$  is the  $g$ -factor,  $\mu_B$  is the Bohr magneton,  $\hbar$  is  
 476 the Dirac constant,  $\delta_b(z) = 1/b$  ( $0 < z < b$ ),  $0$  ( $z > b$ ),  $\langle \hat{S}_{\parallel} \rangle$  is the expectation of spin parallel to  
 477  $\mathbf{B}$ ,  $n_{\text{PI}}$  is the number of localized spins per unit area at the surface of the PI, and  $\Gamma_{\alpha\gamma}$  is the spin  
 478 relaxation tensor. Here,  $\omega_L$  is renormalized by the interfacial exchange fields [18] due to  
 479  $\langle \hat{S}_{\parallel} \rangle$ .

480 For the case with uniaxial symmetry set by  $\mathbf{B}$ ,  $\Gamma_{\alpha\gamma}$  has the general form:

$$481 \quad \Gamma_{\alpha\gamma}(r) = \frac{\delta_{\alpha\gamma}}{\tau_s} + \delta_b(z) \left[ \frac{\delta_{\alpha\gamma}}{\tau_{\perp}} + \left( \frac{1}{\tau_{\parallel}} - \frac{1}{\tau_{\perp}} \right) n_{\alpha} n_{\gamma} \right], \quad (13)$$

482 where  $\tau_s$  is the isotropic part of spin relaxation time induced by the spin-orbit coupling or  
 483 magnetic impurities in NM, and  $\tau_{\perp}$  and  $\tau_{\parallel}$  is the transverse and longitudinal spin relaxation  
 484 time per unit of thickness in the interaction region, respectively.

485 By combining Eq. (12) with Eq. (13), we obtain the spin current in the region where the  
 486 exchange interaction takes place [dark blue region in Fig. 12(b)] as

$$487 \quad -\frac{1}{e v_F} j_{s,z}^\alpha \Big|_{z=0}^{z=b} = b \omega_L \epsilon_{\alpha\beta\gamma} n_\beta \mu_s^\gamma - \left( \frac{b}{\tau_s} + \frac{1}{\tau_{\perp}} \right) \mu_s^\alpha - \left( \frac{1}{\tau_{\parallel}} - \frac{1}{\tau_{\perp}} \right) n_{\alpha} (\mathbf{n} \cdot \boldsymbol{\mu}_s). \quad (14)$$

488 We take a  $b \rightarrow 0$  limit to describe the interface spin current, where  $\delta_b(z)$  becomes a delta  
 489 function. We compare Eqs. (H1) and (I4) and obtain the relation between the interfacial spin  
 490 conductances and anisotropic spin relaxation times,

$$491 \quad G_r = e^2 v_F \left( \frac{1}{\tau_{\perp}} - \frac{1}{\tau_{\parallel}} \right), \quad (I5)$$

$$492 \quad G_i = - \frac{e^2}{\hbar} n_{\text{PI}} J_{\text{int}} \langle \hat{S}_{\parallel} \rangle, \quad (I6)$$

$$493 \quad G_s = - e^2 v_F \frac{1}{\tau_{\parallel}}, \quad (I7)$$

494 where  $v_F J_{\text{int}} = J_{\text{int}}$  is the dimensionless interfacial exchange interaction.

495 In order to determine the anisotropic spin relaxation times  $\tau_{\perp}$  and  $\tau_{\parallel}$ , we use the  
 496 Born-Markov approximation [50] and obtain [26]

$$497 \quad \frac{1}{\tau_{\parallel}} = \frac{2\pi}{\hbar} \frac{n_{\text{PI}} J_{\text{int}}^2}{v_F} \zeta n_B(\zeta) [1 + n_B(\zeta)] |\langle \hat{S}_{\parallel} \rangle|, \quad (I8)$$

$$498 \quad \frac{1}{\tau_{\perp}} = \frac{1}{2\tau_{\parallel}} + \frac{\pi}{\hbar} \frac{n_{\text{PI}} J_{\text{int}}^2}{v_F} \langle \hat{S}_{\parallel}^2 \rangle, \quad (I9)$$

499 where  $n_B(\zeta) = 1/(e^{\zeta}-1)$  is the Bose-Einstein distribution as a function of  $\zeta = g\mu_B B_{\text{eff}}/k_B T =$   
 500  $C_1 B_{\text{eff}}/T$ , and  $B_{\text{eff}}$  is the effective magnetic field of the PI (see [Appendix F](#)). In a paramagnetic  
 501 phase,  $|\langle \hat{S}_{\parallel} \rangle|$  and  $\langle \hat{S}_{\parallel}^2 \rangle$  in Eqs. (I8) and (I9) can be determined as [26],

$$502 \quad \langle \hat{S}_{\parallel} \rangle = -SB_S(S\zeta), \quad (I10)$$

$$503 \quad \langle \hat{S}_{\parallel}^2 \rangle = S(S+1) - \coth(\zeta/2) SB_S(S\zeta), \quad (I11)$$

504 where  $S$  is the spin of  $\text{Gd}^{3+}$  in GGG.

505 Importantly, the difference between the longitudinal and transverse spin relaxation times  
 506 appears only for a finite  $|\langle \hat{S}_{\parallel} \rangle|$ . At the zero magnetic field, Eqs. (I8) and (I9) become the same,  
 507 then

$$508 \quad \frac{1}{\tau_{\parallel}} = \frac{1}{\tau_{\perp}} = \frac{2\pi}{3\hbar} \frac{n_{\text{PI}} J_{\text{int}}^2}{v_F} S(S+1). \quad (I12)$$

509 Substituting the above results into Eqs. (I5)-(I7), we obtain the magnetic field dependence of  
 510 the spin conductances at a NM/PI interface:

$$511 \quad G_r = \frac{\pi}{\hbar} n_{\text{PI}} (eJ_{\text{int}})^2 \left\{ S(S+1) - \left[ \coth(\zeta/2) + \frac{\zeta}{4\sinh^2(\zeta/2)} \right] SB_S(S\zeta) \right\}$$

$$512 \quad = A_1 \left\{ S(S+1) - \left[ \coth(\zeta/2) + \frac{\zeta}{4\sinh^2(\zeta)} \right] SB_S(S\zeta) \right\} \quad (I13)$$

$$513 \quad G_i = \frac{e^2}{\hbar} n_{\text{PI}} J_{\text{int}} S B_S(S\xi) = A_2 S B_S(S\xi), \quad (\text{I14})$$

$$514 \quad G_s = -\frac{\pi}{\hbar} n_{\text{PI}} (eJ_{\text{int}})^2 \frac{\xi}{2\sinh^2(\xi/2)} S B_S(S\xi) = -A_1 \frac{\xi}{2\sinh^2(\xi/2)} S B_S(S\xi), \quad (\text{I15})$$

515 where  $A_1 = (\pi/\hbar)n_{\text{PI}}(eJ_{\text{int}})^2$  and  $A_2 = (\pi/\hbar)n_{\text{PI}}(e^2J_{\text{int}})$ .

516 From the fitting to the experimental data we determine three free parameters,  $\Theta_{\text{CW}}$ ,  $n_{\text{PI}}$ , and  
517  $J_{\text{int}}$ .  $\Theta_{\text{CW}}$  is obtained from the effective Curie-Weiss temperature  $\Theta_{\text{CW}}^{\text{eff}}$ , while  $n_{\text{PI}}$  and  $J_{\text{int}}$  from  
518 the values of  $A_1$  and  $A_2$ . The Pt resistivity of  $3.4 \times 10^{-7} \Omega\text{m}$  predicts the following parameters  
519 [51]:  $\theta_{\text{SH}} = 0.104$ ,  $\lambda_{\text{Pt}} = 2 \text{ nm}$ . We fit Eqs. (H3) and (H4) to the measured transverse FDMR  
520 results of SMR and SHAHE and obtain  $n_{\text{PI}} = 6.94 \times 10^{16} \text{ atom/m}^2$ ,  $J_{\text{int}} = -0.13$ , and  $\Theta_{\text{CW}} = -1.26$   
521 K. The lower Curie-Weiss temperature than the bulk value of  $-2 \text{ K}$  suggests the local  
522 moments on the surface of GGG have a lower coordination number than the bulk. This is  
523 consistent with the lower concentration of spins at the GGG/Pt interface than in bulk GGG,  
524  $n_{\text{PI}} = 6.9 \times 10^{18} \text{ atom/m}^2$ . Taking a typical value of density of state for a metal [52],  $\nu_{\text{F}} \approx$   
525  $3.5 \times 10^{28} \text{ m}^{-3}\text{eV}^{-1}$ , the corresponding **antiferromagnetic**  $s$ - $f$  exchange coupling is about **-2 meV**,  
526 which is similar to the obtained for a Pt/EuS interface [18,44], **-3~-4 meV**. **Our theoretical**  
527 **framework describing the spin transport at the NM/PI interface and the analysis of SMR**  
528 **established here can be applied to results in other magnets including para-, ferri-, ferro-, and**  
529 **antiferromagnets [26].**

## 530 APPENDIX J: TEMPERATURE DEPENDENCE OF THE EXPERIMENTAL AND 531 THEORETICAL RESULTS

532 Here we discuss the  $T$  dependence of SMR in our system by comparing the experimental and  
533 theoretical results. Figure 13(a) shows the detailed  $T$  dependence of  $S_{\text{SMR}}$ . If one assumes that  
534 in Eqs. (H2)-(H5) the charge and spin-transport parameters of the Pt film (such as  
535 conductivity, spin diffusion length and spin Hall angle) are  $T$ -independent, our theoretical  
536 model with the used parameters predicts a  $1/T^2$  dependence for high temperatures,  $T \gg$   
537  $Sg\mu_B B$  (which in our case corresponds to  $\sim 15$  K). However, a direct fit to the measurement  
538 shows a slower power-law decay,  $\sim 1/T^{0.5}$  in the discussed  $T$  range.

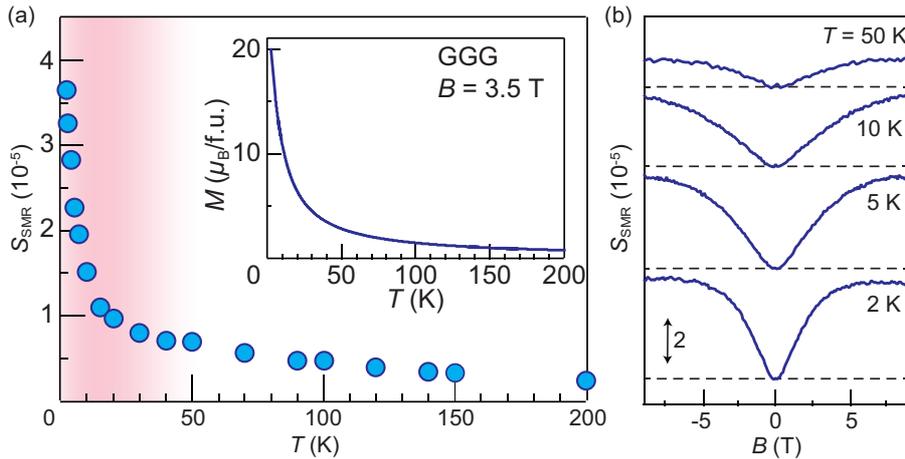
539 First of all, to reconcile the experiment and theory, we take the  $T$ -dependence of the  
540 parameters into account. From the  $T$  dependence of the Pt resistivity (see Fig. 6), we extract  
541 their values at each  $T$  based on the scaling law in Ref. 51. After substituting these values into  
542 Eqs. (H2)-(H5), we obtained a good agreement between the experiment and theory for the  
543 power-law decay of SMR with  $T$ . However, the amplitude of the measured signal at large  $T >$   
544 50 K is larger than the one obtained from the theoretical model.

545 According to the theory, the paramagnetic SMR dominates  $S_{\text{SMR}}$  below 50 K [the shaded  
546 region in Fig. 13(a)] and a strong reduction of  $S_{\text{SMR}}$  at high  $T$  is expected. In contrast, a sizable  
547 signal is observed up to 200 K with a weaker  $T$  dependence. Most likely, this spurious signal  
548 stems from a spin subsystem with a much broader  $T$  dependence than the paramagnetic SMR.  
549 To confirm this, we subtract this "background" signal from  $S_{\text{SMR}}$  below 50 K. Figure 14(a)  
550 shows the  $T$  dependence of  $U_{\text{SMR}}(T) = S_{\text{SMR}}(T) - S_{\text{SMR}}(T = 50 \text{ K})$  as blue solid plots.  
551 Interestingly, after this "background" subtraction, the amplitude of the SMR signal is in very  
552 good agreement with the theory. This indicates that at large  $T$  when the paramagnetic SMR  
553 becomes negligible, we clearly detect another SMR-like magnetoresistance with a weaker  $T$   
554 dependence.

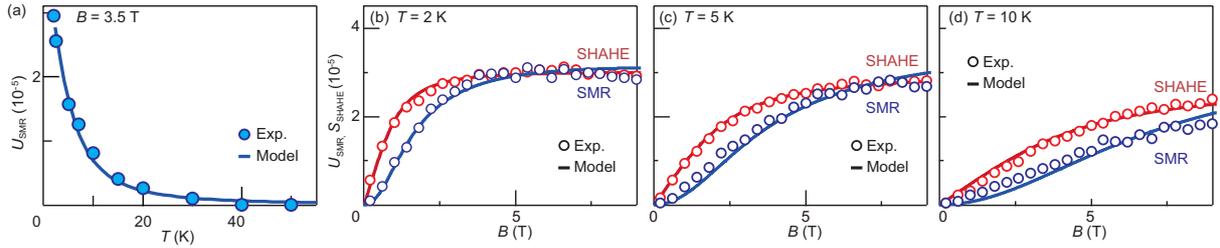
555 This finding, together with the good agreement between the model and experiment on the  $B$   
556 dependence, confirms that at low  $T (< 50 \text{ K})$  the observed magnetoresistance is attributed to  
557 the paramagnetic SMR. Figures 14(b), (c), and (d) show the best fits of our model to  $U_{\text{SMR}}(B)$   
558 and  $S_{\text{SHAHE}}(B)$  at  $T = 2 \text{ K}$ ,  $5 \text{ K}$ , and  $10 \text{ K}$ , respectively.  $U_{\text{SMR}}(B)$  is obtained by subtracting  
559  $S_{\text{SMR}}(B)$  at 50 K presented in Fig. 13(b). The model again reproduces  $U_{\text{SMR}}(B)$  at all  $T$ . In  
560 Table 1, we summarize the value of the parameters obtained from the best fitting to  $U_{\text{SMR}}$  and  
561  $S_{\text{SHAHE}}$ . Our model can explain the  $B$  dependence of  $U_{\text{SMR}}$  at different  $T$  in the low  $T$  regime  
562 ( $T < Sg\mu_B B \sim 15 \text{ K}$ ) with similar parameters, which indicates that the origin of  $U_{\text{SMR}}$  is the  
563 paramagnetic SMR. The long tail observed at high  $T$  is clearly not the effect we are focusing  
564 on and, as demonstrated, a simple subtraction of such background can reveal the  
565 paramagnetic SMR.

566 From our transport experiments, we cannot infer the origin of the "background" signal. This  
567 requires an investigation which is beyond the scope of this manuscript. Nevertheless, the data  
568 suggest the existence of a paramagnetic subsystem with broader  $T$ -dependence. Plausibly, it  
569 could be composed of a small amount of Gd atoms absorbed into Pt during its deposition on

570 the GGG surface by sputtering. These Gd atoms couple much stronger to electrons in Pt than  
571 the ones at the interface, and their  $T$  dependence is expected to be broader than Gd ions in  
572 GGG with different characteristic scale  $Sg\mu_B B$ . To identify the absorbed Gd atoms, we  
573 performed scanning transmission electron microscopy (STEM) and energy-dispersive X-ray  
574 spectroscopy (EDX). Figure 15(a) shows the STEM image across the Pt/GGG interface.  
575 While the sample has a reasonably good interface, we found an amorphous layer with a very  
576 small thickness of about 0.5 nm, which was created by the Pt sputtering. Importantly, the  
577 EDX profile [Fig. 15(b)] shows the amorphous layer consists of Pt, Ga and Gd atoms,  
578 indicating a small amount of Gd atoms are absorbed into Pt. Besides, at the amorphous layer,  
579 the Ga atoms show broader distribution than Gd, and it makes the majority of Gd atoms at the  
580 surface separated from Pt. These findings support the existence of a paramagnetic subsystem.  
581 Other possible factors that, combined with the above effect, may contribute to the observed  
582 background signal is the renormalization of the effective  $s$ - $d$  coupling ( $J_{\text{int}}$ ) either by the  
583 Kondo effect that may be important in Pt [53], or phonons. Any of these effects may have a  
584 rather different  $T$  dependence with respect to SMR. Their studies are beyond the scope of our  
585 work, but definitely, it may be interesting to explore them using SMR in future experiments.  
586 It is important to remark that the above discussion does not change substantially the results  
587 and discussion in the main manuscript. The subtracted background signal,  $S_{\text{SMR}}(T = 50 \text{ K})$ ,  
588 amounts only to about 19% of  $S_{\text{SMR}}(T = 2 \text{ K})$ , indicating that the low-temperature  $S_{\text{SMR}}$  is  
589 dominated by the paramagnetic SMR. In addition, the obtained parameters at 2 K from  
590  $S_{\text{SMR}}(B)$  is consistent with that from  $U_{\text{SMR}}(B, T)$ . Therefore, we can confirm that our  
591 manuscript is adequately based on the results of the paramagnetic SMR.  
592



593 FIG. 13. (a)  $T$  dependence of paramagnetic SMR and magnetization of GGG.  $S_{\text{SMR}}$  is estimated by  
594 fitting a  $S_{\text{SMR}}\sin(\alpha)\cos(\alpha)$  function to the transverse ADMR results at  $|B| = 3.5 \text{ T}$  at various  $T$ . The inset  
595 shows the  $T$  dependence of  $M$  of GGG at  $|B| = 3.5 \text{ T}$ . The paramagnetic SMR dominates the signal in  
596 the shaded  $T$  region. (b) FDMR result of  $S_{\text{SMR}}$  at selected  $T$ . The solid blue curves represent  $S_{\text{SMR}}^{\text{FDMR}} =$   
597  $\Delta\rho_{\uparrow}(45^\circ) - \Delta\rho_{\uparrow}(135^\circ)$ .  
598

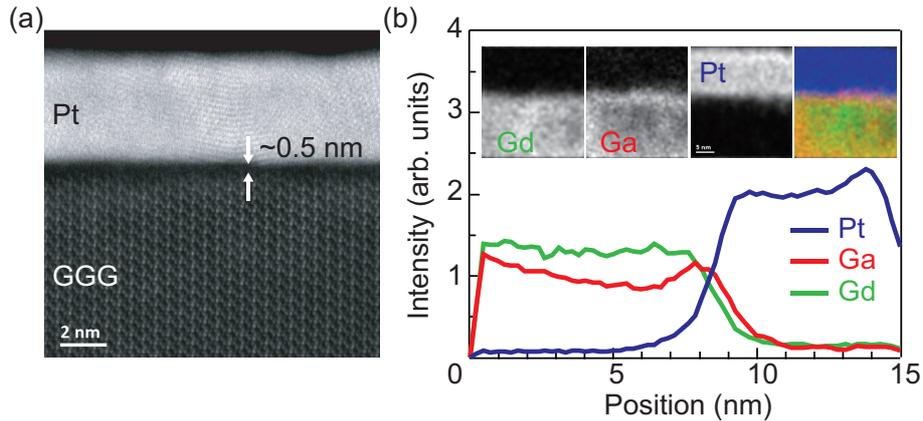


599 FIG. 14. (a)  $T$  dependence of SMR with the model result at  $|B| = 3.5$  T. We subtract  $S_{SMR}(T = 50$  K) from  
 600  $S_{SMR}(T)$  and obtain  $U_{SMR}(T) = S_{SMR}(T) - S_{SMR}(T = 50$  K). The solid curve shows the best fitting of Eq. (5)  
 601 as a function of  $T$ . (b)-(d)  $B$  dependence of  $U_{SMR}$ , and  $S_{SHAHE}$  at (b) 2K, (c) 5 K, and (d) 10 K with the  
 602 model results. We fit Eqs (5) and (6) to each experimental results shown as the unfilled plots.  
 603  
 604

TABLE 1. Parameter values for best fitting.

	$U_{SMR}(T)$	$U_{SMR}(B)$ (2 K)	$U_{SMR}(B)$ (5 K)	$U_{SMR}(B)$ (10 K)	$S_{SMR}(B)$ (2 K)
$n_{Pt}$ (Gd atm/m <sup>2</sup> )	$6.94 \times 10^{16}$	$9.12 \times 10^{16}$	$7.68 \times 10^{16}$	$6.47 \times 10^{16}$	$6.89 \times 10^{16}$
$\theta_{cw}$ (K)	-1.27	-0.77	-1.00	-1.27	-1.26
$J_{int}$	-0.25	-0.09	-0.10	-0.12	-0.13

605



606 FIG. 15. (a) STEM image of the Pt/GGG junction. (b) The spatial distribution of elements along the  
 607 Pt/GGG interface probed by EDX. The blue, red, and green lines indicate the intensity of Pt, Ga, and  
 608 Gd atoms, respectively. The inset is the image of the distribution of Pt, Ga, and Gd atoms, and the  
 609 color-coded image at the interface.

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