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## Cooperative response of the magnetism and superconductivity in the magnetic superconductor RbEuFe<sub>4</sub>As<sub>4</sub>

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We present a study of the magnetic flux evolution in the magnetic superconductor RbEuFe<sub>4</sub>As<sub>4</sub> performed using magneto-optical imaging and magnetization-measurements during field cooling and warming and magnetic field cycling at temperatures above and below the magnetic transition point, T<sub>m</sub>. The vortex patterns emerging at T  $\leq$  T<sub>m</sub> reveal that the Eu-spin subsystem serves as internal pump of magnetic flux while the superconducting critical current controls the delivery of magnetic induction and vortex pinning attenuating the magnetic flux entry, results in a field and temperature dependent critical state that emulates a paramagnetic Meissner effect. The observed vortex dynamics corresponds to a nontrivial spatial current distribution and yields a self-consistent inhomogeneous enhancement of the sample magnetization.

#### I. INTRODUCTION

Spin symmetry distinguishes the macroscopic quantum coherence in conventional superconductors (SC) arising from opposite spin Cooper pairs (s-wave singlet state) from the spin alignment in ferromagnetic (FM) materials, and often makes these fundamental physical phenomena incompatible. However, coexistence of magnetic order and electron pairing has been discovered in antiferromagnetic and ferromagnetic superconductors such as the rareearth (RE) molybdenum sulphides (REMo<sub>6</sub>S<sub>8</sub>) and rhodium–borides (RERh<sub>4</sub>B<sub>4</sub>) with fine scale spiral or helical magnetic structures [1-7]. For example, in ErRh<sub>4</sub>B<sub>4</sub> and HoMo<sub>6</sub>S<sub>8</sub>, the ferromagnetic phase imitates the AFM state by forming oppositely magnetized domains smaller than the SC coherence length, which allows, as predicted in [8], FM-SC coexistence at temperatures below the magnetic transition, T<sub>m</sub>. Other examples of coexistence were found later in unconventional superconductors, UGe<sub>2</sub>, and URhGe, where electrons in the Cooper pairs have the same spin orientation (triplet state) [9,10]. In all these low-T<sub>c</sub> SCs the fragile FM-SC coexistence was observed in a very narrow window of parameters (temperature, pressure, and doping).

New interest in the problem of coexistence arose after the discovery of quaternary rare earth borocarbides (RENi<sub>2</sub>B<sub>2</sub>C) with T<sub>c</sub> ~6-11K and T<sub>m</sub>~1.5-11K [11]. These materials display large variety of magnetic structures, which coexist with superconductivity in a wider temperature range than for previously known ternary compounds. Lately, a robust concurrence of superconductivity and magnetism over a wide temperature range was discovered in the iron-based layered 122 and 1144 iron pnictides, doped EuFe<sub>2</sub>As<sub>2</sub> [12-15] and (AEu)Fe<sub>4</sub>As<sub>4</sub> (A = Rb, or Cs) compounds [16-20]. The advent of these magnetic superconductors with high T<sub>c</sub> (up to ~37K) and T<sub>m</sub> (~15-20K ) values, provides a new platform to investigate the physics of the coexistence of longrange magnetic order and superconductivity. Recent magnetic force microscopy (MFM) experiments [14,15] found that the Meissner state in EuFe<sub>2</sub>(As<sub>1-x</sub>P<sub>x</sub>)<sub>2</sub> coexists with smallscale stripe domains with a domain width smaller than the superconducting penetration depth. These domains represent ferromagnetically ordered Eu<sup>2+</sup> spins that are magnetized perpendicular to the superconducting FeAs - planes, which transform into larger domains carrying spontaneously induced vortices at lower temperature.

Previous magnetization [16, 17, 19] and Mössbauer [21] studies of RbEu-1144 revealed that below  $T_m$  the Eu-spins order ferromagnetically within the Eu-planes, while x-ray and neutron diffraction [22, 23] discovered that the spins display helical order along the c-axis with Eu-moments turning by 90 degrees in neighboring Eu-layers. Magneto-optical imaging [24] showed that cooling single-crystal samples in an in-plane magnetic field which polarizes the Eu-spins towards the field direction at T~ T<sub>m</sub>, results in a pronounced enhancement of magnetic flux inside the crystal deep within the superconducting state.

In the present work, we study this effect in more detail and analyze the magnetic flux behavior with application of an external field in different directions and at various temperatures. The magnetic flux distributions visualized by the magneto-optical imaging technique show a remarkable cooperative response of the magnetic and superconducting subsytems. The images depict the paramagnetic Meissner effect, whereby instead of diamagnetic screening, a substantial *enhancement* of the internal magnetic flux is observed upon approaching T<sub>m</sub>. This enhancement of the magnetization arises from the entry of Abrikosov vortices nucleated at the sample surface by the strongly increased magnetic susceptibility at T<sub>m</sub>. The vortices propagate into the bulk as regulated by vortex pinning, i.e. by the superconducting critical current. This simultaneous, self-consistent action of the Euions' magnetic moment and the superconducting currents results in a unique non-monotonic field and temperature response of the studied magnetic superconductor. Below, we present images of the magnetic flux distributions observed in field cooled, zero-field cooled, and field cycling experiments at different field orientations, and compare them with macroscopic magnetization measurements. We present a model of the self-organized critical state defined by the combined action of superconductivity and magnetism.

#### II. EXPERIMENT

The studies were carried out on platelet-shaped RbEuFe<sub>4</sub>As<sub>4</sub> single crystals that were grown in a RbAs flux [25]. The crystals had a few hundred micron sides parallel to the ab crystalline plane and were a few tens of microns thick.

The macroscopic characterization of the samples has previously been performed using SQUID magnetometry, magneto-transport and specific heat measurements [19, 25, 26], which revealed a sharp superconducting transition at  $T_c \sim 37K$  ( $\Delta T \sim 0.5K$ ) and a magnetic

ordering transition at  $T_m = 15$ K. The superconducting coherence lengths of RbEuFe<sub>4</sub>As<sub>4</sub> are  $\xi_c(0) = 0.92$ nm and  $\xi_{ab}(0) = 1.4$ nm, as deduced from measurements of the upper critical field,  $H_{c2}$ . High-field measurements revealed significant paramagnetic limiting of  $H_{c2}$  [27]. The Ginzburg-Landau parameters obtained from the jump in the specific heat and slopes  $dH_{c2}/dT$  are  $\kappa_c = \lambda_{ab}/\xi_{ab} \sim 67$  and  $\kappa_{ab} = [\lambda_c \lambda_{ab}/\xi_c \xi_{ab}]^{1/2} \sim 108$ , with penetration depths  $\lambda_{ab}(0) = 94$  nm and  $\lambda_c(0) = 160$  nm demonstrating that RbEuFe<sub>4</sub>As<sub>4</sub> is clearly a type-II superconductor [19].

The field and temperature dependence of the magnetization in in-plane and out-ofplane applied fields was measured in a SQUID magnetometer. Fig. 1 shows representative field-cooled cooling, field-cooled warming and zero-field cooled M(T,H) data, as well as inplane magnetization hysteresis loops. Consistent with reported magnetization and X-ray magnetic scattering results [**19**, **22**], already small in-plane fields of the order of hundred Oersted induce a sizable magnetic moment which has a profound effect on the distribution of magnetic flux as described in detail below. The small in-plane saturation fields confirm that the exchange coupling along the c-axis is weak and that the in-plane magnetic anisotropy for the Eu<sup>2+</sup> ions is small. In contrast, the exchange coupling within the Eu-planes and the outof-plane magnetic anisotropy are large [**19**, **22**], inducing quasi-2D magnetism [**26**] as is also evidenced by a comparison of the data in Figs. **1a** and **1**c.

A qualitative distinction between the M(H) loops in Figs.1(b) and (d) is the minimum of magnetization on the descending branch at  $\mathbf{H}_a || \mathbf{c}$ , followed by a maximum near H=0. It can be explained by the decreasing contribution to the total magnetic moment from the magnetic subsystem at lowering H, and the increasing contribution from the critical currents due to the strong field dependence of J<sub>c</sub>. These contributions become equal around the minimum of M(H), which confirms a peculiar interplay between the magnetic and SC subsystems. An

additional factor causing a sharp shape of the M-maximum at H->0 should be the entry of negative vortices, often observed in the plate-like samples in the perpendicular field, which induces a loop of the increased Meissner current at the plate perimeter [28].



Fig.1 Magnetization measured under field-cooling (FC) and zero-field cooling (ZFC) conditions in (a)  $\mathbf{H}||\mathbf{ab}$  and (c)  $\mathbf{H}||\mathbf{c}$ . In (a), FC data on warming and cooling are shown. Inset in (a) displays a close-up of the FC curves near  $T_c$ . Note that FC data for  $\mathbf{H}||\mathbf{c}$  in (c) have been multiplied by a factor of 10 for display purposes. (b, d) Magnetization loops at different temperatures for  $\mathbf{H}||\mathbf{ab}$  and  $\mathbf{H}||\mathbf{c}$ . In (d) the 14K loop is presented only for +/-5000 Oe range.

The magnetic flux distributions were imaged with a magneto-optical indicator technique (MOI), which enables the visualization and quantitative analysis of the normal component of the magnetic induction,  $B_z$ , at the sample surface [29]. The flat ab-faces of some of the platelet crystals were glued between two aluminum blocks and their end faces were polished for imaging the flux patterns with field applied either along the ab-plane (**H**||**ab**) or

the c-axis ( $\mathbf{H}||\mathbf{c}$ ). The evolution of the flux structure was recorded during both field cooling and warming (from T>T<sub>c</sub> to 5K and back to T>T<sub>c</sub>) at different values of H<sub>a</sub>, and during warming following zero-field-cooling (ZFC) at different fields applied at 5K, and in the course of remagnetization (field cycling) at different temperatures.

#### **III. RESULTS AND DISCUSIION**

#### A. Field-Cooling (FC, H||ab) Magnetic Flux Evolution

Fig.2 illustrates the temperature changes of the spatial flux patterns on the end-face of the crystal cooled in the fields of 110, 220, and 330 Oe parallel to the ab-plane. The MOI images reveal the flux density,  $\mathbf{B}_{z} \mid \mid \mathbf{H}$ , in this case perpendicular to the end-face. The field was applied at 45K (T>T<sub>c</sub>) and cooling was down to 5K (T<T<sub>m</sub>). For fields H<40 Oe and at T<T<sub>m</sub>, the MOI image intensity is only slightly increased (not shown), indicating a small enhancement of the sample magnetization along the field direction. In contrast, for H<sub>a</sub> $\gtrsim$ 50 Oe, we observe a pronounced inhomogeneous enhancement of B<sub>z</sub> at temperatures approaching T<sub>m</sub>, induced by certain tilting of helically ordered Eu-spins towards **H**. Such a response highlights the relatively weak interplanar exchange coupling and corresponds to the paramagnetic macroscopic signal near T<sub>m</sub> (Fig.1a ).

Above  $T_c$ , the magneto-optical pictures, referenced by the 42K-image, demonstrate an indistinct homogeneous field distribution throughout the sample (not shown) due to the small magnetic susceptibility of the Eu-moments. With decreasing temperatures below  $T_c$ , a low-contrast contour line around the sample emerges (Fig.2A-C-27K). The contrast is slightly brighter along the sample perimeter indicating an enhancement of  $B_z$  near the sample surface. With further cooling, the overall contrast steadily increases (Fig.2A-C-18K), and at

temperatures close to the magnetic transition,  $T_m$ , the contrast sharply rises at the sample's left and right narrow ends (Fig.2A-C-15K).



Fig.2 Top panels: Comparison of the field patterns emerging during field cooling in magnetic fields of 110 (column A), 220 (column B), and 330 Oe (column C). Temperatures are indicated in the panels. The intensity of the MOI contrast is a measure to the strength of  $\mathbf{B}_{z} \parallel \mathbf{H}$ . All images are referenced to the 40K-image to decrease the optical noise and to improve the contrast. In (B) and (C), the average intensity of the images is depressed to emphasize changes in the flux penetration. Bottom panels: Evolution of the flux patterns during warming the sample in H=330 Oe after cooling to 5K in the same field. The experimental geometry sketched on the lower left shows the sample glued between two aluminum blocks and covered with the magneto-optical (MO) indicator. The scale bar in (A) is 100 µm. The sample width along the z direction is 500 µm.

A further small decrease in temperature enables flux propagation from the ends into

the bulk forming bright channels along the midplane of the sample. At larger fields, these

channels start forming already slightly above  $T_m$  (Fig.2c-18K). The flux evolution slows down and saturates at lower temperatures (Fig.2A-C-10K and 5K) in accordance with leveling of the macroscopic FC M(T) curves in Fig.1-a. Since the MOI image intensity away from the sample corresponds to  $H_a$ , the increased contrast at temperatures near  $T_m$  reveals a strong inhomogeneous enhancement of the magnetic flux (B>H<sub>a</sub>) inside the crystal. The behavior is qualitatively the same for all  $H_a$  in Fig.2A-C. Quantitatively, with increasing field the concentration of the magnetic flux at the two ends of the crystal becomes stronger and the enhanced flux regions penetrate deeper into the bulk.

Warming the crystal after field-cooling to 5K with the same  $H_a$ , we observe similar flux changes in reverse order (Fig.2a-f), except that the enhanced flux regions survive up to higher temperatures above  $T_m$  (Fig.2c-e). With increasing temperature, the magnetic flux tends to spread from the high B regions into the neighboring areas and exit the sample, so that  $B_z$  decreases towards the edges (Fig.2c-e). The escape of flux from the sample is particularly visible along the centerline near the right and left ends where it appears as dark streaks (Fig.2d). At T~T<sub>c</sub> the internal B in the sample approaches H and the field contrast mostly disappears (Fig.2f).

Similar FC flux patterns were observed in several samples with different width-tothickness ratios. In **H**||**ab** they consistently demonstrated the enhancement of  $B_z$  near the surface at T~T<sub>m</sub>, which was especially strong near narrow ends of the crystals, and the anisotropic flux propagation into the bulk.

Fig.3 shows the variation of the flux density with temperature obtained by averaging the magneto-optical intensity in the area of maximum B near one of the ends of another crystal during the field cooling/warming cycle in H = 220 Oe. It confirms the strong enhancement of  $B_z$  near  $T_m$ , the saturation of  $B_z$  at lower T, and the hysteresis of  $B_z$  between cooling and warming the sample. These data resemble the macroscopic M(T) curves measured under similar conditions (Fig.1-a). However, as the MOI images show, the magnetization distribution at  $T \lesssim T_m$  is highly inhomogeneous, which should be considered in the treatment of the macroscopic M(T,H) data.

An interesting feature of the M(T) hysteresis loops measured during the field-cooling warming cycle is the kink emerging at T = T<sub>c</sub> (Fig.1-a, inset). Above T<sub>c</sub>, the descending and ascending branches coincide and show a small increase of M with decreasing T, following the paramagnetic response of the Eu-spins. At T<sub>c</sub>, the cooling branch of the M(T)-loop undergoes a downward kink (dM/dT>0) due to the appearance of the diamagnetic Meissner current. However, the warming M(T) branch has an upward kink (dM/dT<0) at T<T<sub>c</sub> corresponding to magnetization values that are enhanced above the extrapolated normal state signal. The latter is due to the vortices accrued during the initial field-cooling stage and trapped by paramagnetic critical currents upon warming. In addition, the trapped vortices induce an enhanced internal field causing a magnetization of the Eu-moments above that corresponding to the applied field.

Fig.3 Temperature dependence of the average induction near one end of the crystal during field-cooling-warming in the ab-field of 220 Oe . Inset shows magneto-optical image of the sample with the averaging area marked by the square. The scale bar is 100  $\mu$ m. The sample width along the z direction is 300 $\mu$ m.



#### B. Zero-Field-Cooling (ZFC, H||ab) Magnetic Flux Behavior

In this experiment the sample was cooled in zero magnetic field, followed by the application of **H**||**ab** at 5K. Subsequently, the flux distribution was recorded upon warming the sample in the constant applied field. With the application of H<sub>a</sub> at 5K, the magnetic field enters from the sample surface as is usually observed in traditional superconductors. Here, similar to the FC case, vortices enter preferentially from the two narrow ends along the adirection and form tapered regions of enhanced B<sub>z</sub> extending through the midplane of the sample (Fig.4a). The flux-free Meissner region is visible as dark areas in the bulk. Upon warming the sample towards T<sub>m</sub> at a chosen value of H, the high B<sub>z</sub> regions expand further into the sample (Fig4b-c). At T $\gtrsim$  T<sub>m</sub>, B<sub>z</sub> begins to decrease, with magnetic flux spreading into the dark Meissner regions and partially exiting the sample (Fig.4d-f). Up to temperatures close to T<sub>c</sub> the contrast over the sample is darker than outside indicating some degree of diamagnetic screening (Fig.4g). Finally, at T $\gtrsim$  T<sub>c</sub> the field distribution becomes homogeneous (Fig.4h) without any discernable signal from the sample.



Fig.4 ZFC flux patterns in the sample during warming in the ab-field of 441 Oe applied at 5K after cooling in H=0. Temperatures are shown in the panels. Pictures are referenced to the 42K-image and a weak contrast above the sample at 37K is not resolved.

#### C. Field-Cycling after zero-field-cooling (H || ab)

In this section we describe flux patterns observed in zero-field cooled samples upon ramping magnetic field up and down at different temperatures. At  $T_c > T > T_m$ , with increasing H|| ab, the magnetic flux penetration follows the typical superconducting scenario (column A and B in Fig.5). Namely, small applied fields are screened by the sample and concentrate at the sample boundaries due to diamagnetic Meissner currents (Fig.5-top panels). At larger H<sub>a</sub>, vortices enter the sample from the surface and disperse inside the bulk due to the Lorentz force induced by the diamagnetic critical currents. The flux density is stronger and penetrates deeper from the narrow left and right ends of the crystal revealing the pinning anisotropy. Similar to the FC and ZFC case, channels of the distinctly enhanced flux density form along the horizontal centerline of the sample. These channels can be due to the weak link for the easy vortex entry created from compositional inhomogeneity that is often observed in flux grown layered samples. However, our EDS analysis did not reveal any compositional changes within the experimental accuracy of 3%. Alternatively, such flux channel could result from the current instability expected in anisotropic superconductors [30]. With decreasing H<sub>a</sub>, the flux exits towards the sample ends, resulting in areas of reduced B<sub>z</sub> along the centerline (dark regions marked by arrows in the bottom panels of Fig.5).

At  $T=T_m$ , we observe a strong enhancement of the flux density, with  $B_z$  values noticeably exceeding that of the applied field due to flux penetration from the narrow ends of the sample (Fig.5, column C). With increasing H the resulting flux patterns become similar to those observed near  $T_m$  in the FC case illustrated in Fig.2. At T well below  $T_m$ , the magnetization behavior (not shown) is similar to those at  $T=T_m$ , albeit the same depth of the flux entry is achieved at much larger  $H_a$  due to the enhancement of vortex pinning at lower temperatures.



Fig.5 Comparison of the flux patterns emerging during ramping the field  $\mathbf{H} \| \mathbf{ab}$  up and down at  $T > T_m$  (columns A, B) and  $T = T_m$  (C). Field values are shown on the panels. Down arrows near the values of H correspond to decreasing applied field. The enhanced flux regions with bright contrast (B > H) penetrate into the bulk from the sample perimeter anisotropically with increasing field. At  $T < T_m$ , patterns similar to those at  $T = T_m$  form at larger H (see e.g. Fig.4a) due to increased pinning at lower temperatures. Long arrows in the bottom panels, at H=0, mark channels of advanced flux exit (darker contrast).

#### D. Imaging the ab-surface with Field-Cooling in H||ab

Here, the MO indicator film was placed on top of the wide ab-face of the crystal, the magnetic field was applied in the ab-plane, and the normal field, B<sub>z</sub>, on the ab-surface of the sample was monitored during field cooling. In this geometry, the imaged normal fields reveal

tilting of the magnetic flux lines towards the c-axis due to the fields of the superconducting currents and the stray fields of the regions where Eu-spins are polarized along **H**.

A typical set of  $B_z$  patterns in one of the samples cooled in H=278 Oe is presented in Fig.6. Intriguingly, with decreasing temperature, we observe a double dark and bright contrast band at the horizontal sides of the plate that are perpendicular to **H** (Fig.6a). At T~T<sub>m</sub> the dark/bright contrast increases and becomes especially strong near the corners of the crystal (Fig.6b), but then changes only slightly with further cooling. After removing the field at T=5K, instead of the double dark/bright contrast band at the bottom, as is generally observed in superconducting plates with in-plane trapped flux. The colors of the described contrasts are inverted when the field direction is changed for opposite.

The unusual double dark/bright contrast bands at the perimeter of the crystal can be explained with the sketch in Fig.7. During field-cooling, the magnetic flux first enters into the corner regions of the sample as illustrated in Fig.7a by small corner triangles (dark) with dash-line boundaries. Due to the increased magnetic susceptibility, these regions carry enhanced magnetic flux and yield stray fields similar to long magnetic prisms polarized across their length (Pr in Fig.7a). They have Down (blue arrow) and Up (red arrow) components of the normal field  $H_z$  near the top sample surface. In combination with the effect of diamagnetic supercurrents that tilt the field around the crystal edges (Fig.7d), the resulting field lines wiggle at the edges up-and-down as shown for the top sample surface in Fig.7a. Near  $T_{m_y}$  enhanced magnetic flux enters preferentially near the narrow ends, as discussed in the previous sections. These enhanced flux regions are equivalent to the longitudinally polarized magnetic prisms inside the sample (Tr in Fig.7b), which yield additional stray fields

shown by blue and red arrows. At  $T \sim T_m$  and below, the stray fields of these enhanced flux regions dominate, negating the double contrast bands and resulting in a strong dark or bright contrast at the sample corners (long vertical arrows near the corners in Fig.7b) as we observe in the experiment (Fig.6b). With decreasing H at low T, the superconducting currents change direction and support the field of the penetrated magnetic flux (Fig.7c). The picture (Fig.6c) then becomes similar to the trapped flux pattern in a nonmagnetic superconductor (Fig.7e) or in an in-plane polarized magnetic plate.



Fig.6 a-b Images of the fields normal to the ab-plane during field cooling in the ab-field H =278 Oe. In (d) the external field is switched off at 5K. Dark contrast corresponds to the down-component of the field, bright - to the up-component. (e) geometry of the experiment. The right side of the sample has smaller thickness. The contrast in (a) is increased to emphasize the emergence of the double bright/dark  $B_z$ -image at the sample sides. Scale bar in (a) is 100 µm. The sample thickness is 80 µm in the left and 45µm in the right part, as sketched in (e).



Fig.7 Field lines near the top surface of the field-cooled magnetic superconductor yield double contrast at the sample edges perpendicular to **H**. Mirror symmetric picture forms at the bottom surface. Dashed lines in (a) outline narrow corner regions where the flux enters due to the increased magnetic susceptibility upon approaching  $T_m$ . Outside the plate, the field lines tilt down into these regions (blue arrows at the left and red arrows at the right sample side). Curvature of the field lines can be approximated by adding stray fields of transversely polarized prisms (Pr) in the corner regions to the fields of the diamagnetic currents sketched in (d). When a strong flux enters from the narrow ends (large "triangular prisms", Tr, are added to (a)) the stray fields of these high B regions enhance the normal field components near the plate corners (long vertical blue and red arrows near the plate corners in (b)). Switching off  $H_a$  yields typical field pattern of a magnetized bar. Bending of field lines in a usual superconducting plate with increasing and decreasing field is shown in (d) and (e).

#### E. Imaging the ab-surface with Field-Cycling in H||c

Fig.8 illustrates the magnetization process for  $\mathbf{H}||\mathbf{c}$  perpendicular to the ab-surface of the crystal at  $T \ge T_m$ . At these temperatures, similar to non-magnetic–superconducting samples, the flux smoothly penetrates from the edges upon increasing field and then exits towards the edges with decreasing field to zero. At H=0 (after application of H<sup>max</sup>= 827 Oe), near the edges of the sample, the flux reverses sign (dark contrast in the bottom panels of Fig.8) due to the stray fields of the trapped vortices. Contrary to the **H**||**ab** case, there is no enhanced flux entry at T<sub>m</sub>, but rather a more shallow flux penetration than at larger temperatures. Nevertheless, in the vortex occupied areas, the induction is stronger at  $T_m$  than at  $T>T_m$ .

These flux patterns reveal a major role of the bulk critical currents (i.e. vortex pinning) and a marginal contribution of the magnetic subsystem in the magnetic response at moderate  $\mathbf{H}||\mathbf{c}$ . Obviously, the Eu-spins are easily polarized in the **ab**-plane but require larger polarizing fields in the **c**-direction due to the magnetic anisotropy of RbEuFe<sub>4</sub>As<sub>4</sub>. As a result, the superconducting critical currents locked in the ab-plane at  $\mathbf{H}||\mathbf{c}$  dominate the magnetic response. Clearly, the individual vortex structure is different for  $\mathbf{H}||\mathbf{ab}$ , when the Eu-spins turn towards the field partially unwinding the helical structure inside the vortex, than for  $\mathbf{H}||\mathbf{c}$ , when the Eu-moments tilt by a small angle away from the **ab**-plane at the same field values. As a result, the spatial field distribution of the vortex, scaled by the magnetic permeability of the anisotropic spin system, should depend on the field direction.

In purely FM materials the magnetic anisotropy can be easily determined from M(H) measurements in differently oriented fields. However, in RbEuFe<sub>4</sub>As<sub>4</sub> the tandem action of both magnetic and superconducting subsystems makes the decoupling of their contributions very difficult, allowing only approximate estimates of the magnetic anisotropy constant, K<sub>a</sub>. At the same time, the easy-plane character of the anisotropy (**ab**-plane alignment of the Euspins) clearly follows from the comparison of the M(H) curves for **ab**- and **c**-fields at T $\lesssim$ T<sub>m</sub>. It is directly confirmed by neutron scattering experiments [22, 23]. Our observations of different flux distributions emerging at **H**||**ab** and **H**||**c** show that the easy-plane magnetic anisotropy has a strong effect on the vortex structure and dynamics. At the same time, the moderate superconducting anisotropy ( $\Gamma$ =1.7 [19]) should have a smaller influence on the vortex motion.



Fig.8 Flux entry and exit at T=35 (A), 20 (B), and 15K (C) in the increasing (top panels) and decreasing (bottom panels with down-arrows near H<sub>a</sub> values) perpendicular field, **H** ||**c**. Maximum applied field was 827 Oe. Flux patterns for this sample field-cooled in **H**||**ab** are shown in Fig.6. The depth of the vortex entry is larger at higher T due to reduced pinning, but the flux patterns are qualitatively similar. Unlike in **H** ||**ab**, there are no peculiarities at T<sub>m</sub> (15K) due to the large magnetic anisotropy restricting the tilt of the Eu<sup>2+</sup>-spins from the ab-planes and thus their susceptibility  $\chi_{Eu}$ ||c. The effect of the superconducting critical currents is dominating and the magnetic subsystem contribution is minor. Scale bar in (a) is 100 µm. Black arrow in (C)-662 Oe points to the position of a crack allowing easy flux entry and exit. To the right of the crack the crystal has smaller thickness as sketched in Fig.6e.

#### F. Imaging the ab-surface with Field-Cooling in H||c

The field-cooled MOI measurements with **H**||**c** confirms the small susceptibility of the Eu-spins along the c-axis. Flux images obtained under these conditions reveal an enhanced contrast emerging along the edges of the samples which increases upon approaching T<sub>m</sub> (Fig.9A, B). The strength of this contrast (the flux density) is much weaker than during fieldcooling in **H**||**ab** (Fig.2), due to the small magnetic contribution arising from slightly tilted Eu<sup>2+</sup>-spins from the **ab**-plane. Similar increased edge field is typical for perpendicularly magnetized FM plates. This field distribution resembles electric field pattern at the perimeter of a charged flat capacitor, where the stray fields are absent in the main capacitor area and appear only near the edges over a width close to the capacitor thickness. However, in RbEuFe4As4 the picture is modified by the entry of vortices supporting the edge field enhancement. The temperature dependence of the maximum edge field, measured from  $B_z(x)$ profiles taken across the edge of the sample field-cooled in  $H_a$ =330 Oe, is shown in Fig.9C. The enhanced edge field increases upon cooling towards T<sub>m</sub> and saturates at T<T<sub>m</sub>. This behavior confirms that the edge contrast is due to the polarization of the Eu-ions. The enhancement of the edge field is in sharp contrast to observations in nonmagnetic superconducting plates cooled in perpendicular magnetic fields, whence during field-cooling, vortices exit near the sample boundaries due to the Meissner effect and the edge fields become smaller. In our case additional vortices are also generated at the sample perimeter but they remain in a narrow edge rim due to the critical currents which increase upon cooling and restrict the vortex propagation.



Fig.9 Flux patterns on the ab-surface of the sample during field-cooling in  $\mathbf{H} \| \mathbf{c}$  at field values of 110 Oe (left column) and 220 Oe (middle column). The bright contrast is noticeably weaker in the right part of the sample which is thinner as shown in Fig.6e. Temperature variations of the maximum edge field,  $B_z^{max}$ , at H=330 Oe are shown in the right plot. The rectangle in the inset above the plot outlines the strip along which the field profile,  $B_z(x)$ , was measured. The scale bar shown in (A) is 100 µm.

#### G. Short summary of the MOI observations

The main results of our experiments can be recapped as follows. During field-cooling of the magnetic superconductor RbEuFe<sub>4</sub>As<sub>4</sub> in fields parallel to the **ab**-plane, a strong enhancement of the induction inside the sample emerges at temperatures near and below the magnetic transition point T<sub>m</sub>. In the zero-field cooled case, when the sample is warmed after the application of the field **H**||**ab** at low T, the enhanced entry of magnetic flux occurs as T approaches T<sub>m</sub> from below. Similarly, when ramping up the field **H**||**ab**, the advanced penetration of magnetic flux appears at temperatures close and below T<sub>m</sub>. In all these cases the flux enhancement occurs due to the anisotropic entry of additional vortices. Our observations show that in the ordered state, the Eu<sup>2+</sup>-spin system adds to the effect of the applied magnetic field, resulting in an increase of the internal magnetic induction. The additional flux induced by the large magnetic susceptibility ( $\chi_{ab}$ ) of the crystal appears in the shape of the Abrikosov vortices at the sample surface, while their propagation into the bulk is controlled by the superconducting critical currents. Thus, the cooperation of the magnetic and superconducting subsystems creates a peculiar inhomogeneous flux structure in RbEuFe<sub>4</sub>As<sub>4</sub>. The contribution of the magnetic subsystem appears distinctly in **H**||**ab**, where the field drives the Eu spins that are polarized in the ab-planes and helically ordered along the c-axis, towards the direction of **H**. These applied fields should be larger than the relatively weak interplanar exchange coupling field responsible for the helical ordering of the ferromagnetic Eu-sheets and can be estimated as **H**||**ab** ~ 50-100 Oe at T $\leq$ T<sub>m</sub>.

For  $\mathbf{H}_a$ ||**c**, the magnetic susceptibility is much smaller,  $\chi_c(T) << \chi_{ab}(T)$ , due to the easyplane anisotropy of the Eu-spins, and the effect of the magnetic subsystem on the FC, ZFC, and field ramping behavior is much weaker. Here, the magnetization process (at least in moderate fields) is dominated by superconducting currents and is similar to those of nonmagnetic superconductors.

#### H. Model of the Self-induced Critical State

Here, we will discuss the peculiar magnetic flux structure emerging in the vicinity of  $T_m$  in terms of the self-induced critical state, which describes a specific induction and current distribution in the magnetic superconductor. Clearly, the observed magnetic flux enhancement during field cooling of RbEuFe<sub>4</sub>As<sub>4</sub> crystals is in stark contrast with the standard Meissner effect behavior expected for a conventional superconductor. In a regular SC cooled in a constant magnetic field, vortices exit near the sample surface due to the diamagnetic Meissner current but some remain trapped by the pinning defects in the bulk. The resulting induction profile  $B_z(x)$  across the sample should resemble an inverted letter M

with minima at the surface and smooth changes of the slope towards the center of the sample, following the cooling history of the sample J<sub>c</sub> (Fig.10a).



Fig.10 Induction and current distribution in field-cooled plate of (a) a regular superconductor at T<T<sub>c</sub>, and (b) in a magnetic superconductor at T<T<sub>m</sub><T<sub>c</sub>. Changing slope of B(x) proportional to J<sub>c</sub> inside the FC SC plate in (a) follows history of J<sub>c</sub>(T) during cooling as shown by dashed lines.

In contrast, our RbEuFe<sub>4</sub>As<sub>4</sub> crystals show that  $B_z$  is enhanced near the edges and decreases towards the interior, yielding an induction profile opposite to  $B_z(x)$  of conventional superconductors. It can be described by the model sketched in Fig.10b. At the surface, the magnetic induction is enhanced to a value determined by the susceptibility  $\chi_{Eu}(T)$  of the Euspins,  $B_z = H (1+ 4\pi\chi_{Eu})$ , which is valid in the applied fields that are much smaller than the field of saturation. Away from the surface,  $B_z$  drops rapidly by  $\Delta B_M$  over a distance of the penetration depth or smaller due to the diamagnetic Meissner current  $J_M(T)$ . This feature is not resolved in our images. Further into the bulk,  $B_z$  decays smoothly due to the diamagnetic critical currents  $J_c(T)$ , while in the middle of the plate the induction remains at the level defined by  $\chi_{Eu}(T_c)$ .

For a thin isotropic magnetic superconducting plate of thickness d cooled in a parallel field H<sub>a</sub>, and assuming that  $\chi_{Eu}(T) > 0$  varies much faster than J<sub>c</sub>(T), a simple estimate of the penetration depth x<sub>c</sub><sup>FC</sup> for additional vortices generated at the surface yields [24]:

$$x_{c}^{FC} = \frac{[\mu(T) - \mu(T_{c})]H - \Delta B_{M}}{\frac{4\pi}{c}\mu(T)j_{c}(T)}$$
(1)

Here,  $\mu=1+4\pi\chi_{Eu}$  is the magnetic permeability. In a zero-field cooled sample, when the field is applied at low temperature, the flux entry into the sample interior is delayed by the Meissner currents and the critical currents. In this case, the depth of Bean profile

$$x_c^{ZFC} = \frac{H - \frac{\Delta B_M}{\mu(T)}}{\frac{4\pi}{c} j_c(T)}$$
(2)

is weakly influenced by the magnetic response. The field of full flux penetration, H<sub>p</sub>, at which flux reaches the center of the plate,  $x_c^{ZFC} = d/2$ , can be obtained from (2) as:

$$H_p = \frac{2\pi}{c} j_c(T)d + \Delta B_M / \mu(T) \quad (3)$$

For fields below  $H_p$ , the sample is in a heterogeneous magnetic state in which a partially polarized helical magnetic structure in the penetrated region coexists with an unperturbed helix in the central parts. Accounting that the Meissner contribution,  $\Delta B_M$ , strongly decreases with field,  $H_p$  is primarily defined by the SC critical current.

The above simplified model gives a qualitative picture of the flux distribution due to the field enhancement by the magnetic subsystem. A more realistic model should account for the anisotropic critical currents and the nonlocal character of the magnetic susceptibility resulting in an integral magnetic response.

An approach similar to ours was used to explain the magnetization curves in grain aligned powders of HoBa<sub>2</sub>Cu<sub>3</sub>O<sub>7</sub> (0.14K = T<sub>N</sub> << T << T<sub>C</sub> = 91K) which contain a large magnetic contribution from the Ho-ions [**31**]. Following [**32**, **33**], it was admitted in [**31**] that due to the effect of magnetic ions, the effective penetration depth  $\lambda_{eff}$  should be renormalized by a factor of  $\mu^{-1/2}$ . As a result, vortices carrying the magnetic flux quantum  $\Phi_0$  become slimmer, with insignificant change in their energy and the first critical field. At the same time,  $\mu$ >1 introduces a distinct paramagnetic background to the magnetization curves and increases the induction gradient  $\mu$ -times (without increasing the critical current J<sub>c</sub>).

It is interesting to compare the observed FC flux patterns in RbEuFe<sub>4</sub>As<sub>4</sub> with results of the neutron experiments in field cooled crystals of  $ErNi_2B_2C$  [34]. The latter revealed a shorter intervortex spacing and decreased intensity of the vortex-lattice diffraction peaks below the transition into the weak-ferromagnetic phase,  $T_{WF}$ <T<sub>c</sub>. The shorter spacing between vortices corresponds to the enhancement of the flux density and the decreased peak intensity may be related to the increased nonuniformity of the vortex lattice. Our picture of the self-organized FC critical state with locally increased and spatially inhomogeneous vortex distribution explains this behavior.

#### I. Structure of single vortices in H<sub>a</sub>||ab

As mentioned above, the main change in the vortex structure due to the magnetic subsystem is the contraction of the vortex diameter  $\lambda_{eff} \sim \lambda/\mu^{1/2}$ . A new feature appears at large  $\mu$ , when the reduction of  $\lambda_{eff}$  may result in the sign inversion of the vortex field, Hv(r), at some distance r from the vortex core. In the London approximation this yields the long-range attraction of vortices and type-I-like superconducting behavior [32, 33]. The same conclusion was made in [35] from the analysis of the generalized Ginzburg-Landau functional with material parameters approximating the magnetic superconductor ErRh<sub>4</sub>B<sub>4</sub>. It was reported that both SC and FM components are weakened compared to their independent values,  $\lambda_{eff}$  decreases, and H<sub>v</sub>(r) reaches a negative minimum at some r. Interestingly, the magnetic order induced by H<sub>v</sub> (Fig.1 in [35]) may expand over scales larger than  $\lambda_{eff}$ , so that

already at relatively small vortex density, the magnetization distribution should become rather homogeneous, with only weak modulations.

A useful analytical analysis of the Abrikosov vortex structure in the ordered FM/SC state was presented in [36]. This work considers vortices perpendicular to the periodic multilayer of FM and SC components, which simulates the ferromagnetic superconductor with the easy-plane magnetic anisotropy in the normal field. It was shown that the vortex field  $H_v(r)$  depends on both the modified effective SC penetration depth  $\lambda_{eff}=\lambda\mu^{-1/2}$  and the characteristic FM length  $L=(\alpha/K)^{1/2}$ . Here  $\alpha$  and K are magnetic exchange and anisotropy constants (as defined in [37]), so that *L* is a characteristic FM domain wall width. The vortex field induces a linear tilt of magnetization towards the vortex axis, M(||H\_v)=H/K, so that  $\mu=1+4\pi/K$ , which in a certain range of K ,  $\alpha$  , and  $\lambda$  , causes the sign change of H<sub>v</sub> at some distance from the vortex core.

In our samples, at **H**||**ab**, the Eu-spins comprising the helical structure twist towards  $H_{a}$ , which can be approximated by a linear response, M=H/K<sub>eff</sub>, over relatively wide range of fields (as in a non-SC magnetic helical systems [**38**, **39**]). Here K<sub>eff</sub> depicts the magnetic anisotropy, although its origin is the interplanar exchange field which maintains the helical spin structure. Note, that in magnetic superconductors the helical spin order is not defined solely by the magnetic subsystem but results from the competition between the FM and SC components, so that even with purely ferromagnetic exchange, the magnetic system can transform into the spiral configuration [**40**, **41**]. Independently of the nature of the helical spin structure in RbEuFe4As4, admitting the linear magnetic response of the Eu-spins, we can roughly estimate the value of  $\mu$  from the slope of the averaged magnetization loops, M(H), at T  $\leq T_m$  [**19**]. For **H**||**ab** this gives  $\mu$ =1+4 $\pi$ /K<sub>eff</sub> ~3 at T~15K, so that K<sub>eff</sub> ~2 $\pi$ . By adopting

the formula for cubic ferromagnets, the exchange constant  $\alpha$  can be estimated from the magnetic ordering temperature  $T_m \sim 0.7 J/k_B$  (here *J* is the exchange integral and  $k_B$  - Boltzmann constant) and the saturation magnetization of the sample  $M_0=g\mu_BSn/V_c$  (g=2, S=7/2,  $\mu_B$ -Bohr magneton, n=4 - number of Eu-spins per the unit cell volume  $V_c=abc$ , with lattice parameters a=b=3.882 Å and c=13.273 Å). This yields  $\alpha=2nJS^2/aM_0^2=4.4 \ 10^{-12} \ cm^2$ , so that  $L=(\alpha/K_{eff})^{1/2}=8.4$  nm. Neglecting the SC anisotropy and assuming an average penetration depth  $\lambda=(\lambda_{ab}\lambda_c)^{1/2}=122$ nm [19], we estimated the distribution of  $H_v(r)$  and  $B_v(r)$  following [35], but with modified  $\mu_{zz}(q)=1+4\pi/(K+\alpha q^2)$ , which appears due to an additional term,  $2\pi M^2$ , omitted in eq.4 of [36]. This changes some formulas of [36] (eq.8 for  $q_i^2$  and eq.10 for  $H_v(r)$ ), but leaves the equation for  $B_v(r)$  intact. As Fig.11 shows, for the chosen constants of RbEuFe<sub>4</sub>As<sub>4</sub> yielding  $L<<\lambda$ , neither B<sub>v</sub> nor H<sub>v</sub> change sign.



Fig.11 Single vortex field,  $H_V(r)$  (blue), and induction,  $B_V(r)$  (red), calculated for H||ab following modified formulas of [36] with magnetic and superconducting parameters estimated for RbEuFe<sub>4</sub>As<sub>4</sub> as described in the text.

In the field  $\mathbf{H}||\mathbf{c}$  the magnetic permeability is smaller than for  $\mathbf{H}||\mathbf{ab}$  due to the easyplane anisotropy of the Eu-spins, and the effect of the magnetic subsystem on the vortex structure will be weaker. Exact calculations of  $B_v(\mathbf{r})$  and  $H_v(\mathbf{r})$  accounting for the anisotropy of the SC parameters and accurate estimates of the magnetic constants of RbEuFe<sub>4</sub>As<sub>4</sub> will be reported elsewhere [42].

#### J. Anisotropy of the self-organized critical state

In the cuprate high-T<sub>c</sub> superconductors, anisotropic flux dynamics is caused by the layered crystal structure inducing a large anisotropy of the superconducting parameters,  $\Gamma$  =  $\xi_{ab}/\xi_c$ , and affecting the pinning of vortices. In RbEuFe<sub>4</sub>As<sub>4</sub>,  $\Gamma$  is small (~1.7), while we see highly anisotropic flux penetration i.e. large pinning anisotropy, especially at  $T \leq T_m$ . A possible explanation of the large vortex motion anisotropy could be a specific defect structure of RbEuFe<sub>4</sub>As<sub>4</sub>, as was seen e.g. in a sister material CaKFe<sub>4</sub>As<sub>4</sub>, where nanometer intergrowth platelets randomly form parallel to the ab-plane [43]. However, we suggest that in our crystals the source of the anisotropy could be a self-induced magnetic contribution to pinning. At H=0, the Eu-spin planes order helically with a period of 4 lattice spacings along the c-axis and coexist with superconducting FeAs layers. However, within the vortices oriented along the ab-plane, the Eu-spins twist towards the field direction. This partially polarized spin state can yield ancillary pair breaking effects in the SC layers (from an average polarization of the conducting electron spins) thus introducing a self-induced vortex pinning. Such a magnetic contribution to pinning in the presence of the layered spin structure and sharp changes of B<sub>v</sub> near the vortex center (Fig.11) could affect the critical current anisotropy.

This conclusion recalls some earlier studies of vortex dynamics in magnetic superconductors. For example, it was predicted in [44] that in magnetic superconductors, the local magnetic polarization by the vortex field can substantially increase the viscosity of vortices and retard their motion. Experimentally, a clear effect of magnetic ordering on

vortex dynamics was found in single crystals of FM-SC borocarbides such as  $HoNi_2B_2C$  [45] and  $ErNi_2B_2C$  [46-48]. Here, the rapid increase of the bulk critical current was observed at the transition into the magnetically ordered state, which was referred to as the intrinsic pinning of vortices by the magnetic structure (see also [49]). Interestingly, in superconducting ferromagnets with  $T_c << T_m$  ( $Eu_{1.5}Ce_{0.5}RuSr_2Cu_2O_{10}$  [50] and UCoGe [51]) a sharp enhancement of the ferromagnetic coercivity was found upon transition into the SC state. This effect of delayed field penetration into the bulk arises due to increased vortex pinning. Unlike in our samples, where entering vortices enhance the bulk magnetization, in the ruthenate and UCoGe, the pre-existing M *generates* spontaneous bulk vortices which are involved in the remagnetization process below  $T_c$ . Nevertheless, in both cases, the total magnetic moment of the sample and the spatial flux distribution is defined by the selforganized critical state resulting from the cooperative response of the magnetic and superconducting systems.

In RbEuFe<sub>4</sub>As<sub>4</sub>, the anisotropy of the self-organized critical state could cause the formation of flux channels observed at H||ab (Figs.2-5) in the case of a strong field dependence of the critical current causing a positive feedback in the flux penetration. Although the intertwined action of the magnetic and SC subsystem does not allow the exact quantitative estimates of the separate magnetic constants and critical currents, it is possible to make a qualitative assessment of the field and temperature dependence of J<sub>c</sub> from the half-width of the macroscopic magnetization loops. In fact, the M(H) loops display a fast decay of J<sub>c</sub>(H) for H||ab (see supplemental info in [24]). Consequently, the enhancement of B<sub>z</sub> due to the vortex penetration engaging the internal M should suppress J<sub>c</sub> and promote additional vortex entry. In turn, this will initiate a further increase of B and the progressive suppression

of  $J_c$ , resulting in the extension of the flux occupied regions (see Fig.12) which can ultimately transform into flux channels.

In the case of  $\mathbf{H}||\mathbf{c}$ , the small  $\chi_{Eu}$  defined by the easy-plane anisotropy of the Eu-spins, strongly reduces the effect of the magnetic subsystem at low fields even below  $T_m$ . As a result, the SC critical currents circulating over large sample area dominate the magnetization at moderate fields  $\mathbf{H}_a||\mathbf{c}$  as in the case of non-magnetic superconductors.



Fig.12 Progressive extension of the flux occupied region. Increasing B in the shaded areas causes the field suppression of  $J_c$ , which allows more vortices to enter and move inside the sample, thus extending the flux front (from green to brown). Distances between the current lines in this sketch illustrate the decreasing  $J_c$ .  $B_2>B_1$  in the major extended area.

Note, that known predictions of various coexistence phases (domain structure, spiral, Meissner, and spontaneous vortices) in magnetic superconductors [33, 35, 40, 41, 52-57] are based on the mean field approximation assuming the *uniform system* state on the scale larger than the period of possible oscillations of the order parameter. In the applied magnetic field the whole system is supposed to uniformly respond to H<sub>a</sub>. Our observations point to the importance of the field induced nonuniformity for understanding the magnetic response of FM-SC. The coexisting state in the presence of H is *principally inhomogeneous* independently of the field application sequence. The applied magnetic field does not penetrate inside the entire sample at any T<T<sub>c</sub>, but has to be delivered into the bulk via the entry of Abrikosov vortices. They will actuate the local alignment of the spins in the crystal interior and induce critical currents supporting gradients of the magnetic induction.

#### **IV. CONCLUSIONS**

Our observations of the magnetic flux patterns under various field directions and field cycling scenarios at temperatures above and below the magnetic transition,  $T_m$ , reveal a remarkable cooperative response of the superconducting and magnetic subsystems in single crystals of RbEuFe<sub>4</sub>As<sub>4</sub>. At  $T \leq T_m$  the large magnetic susceptibility,  $\chi$ , induces an inhomogeneous enhancement of the internal magnetic flux in the samples. This occurs through the nucleation of Abrikosov vortices at the sample surface and their propagation into the bulk. This propagation is regulated by the superconducting critical currents resulting in an unusual self-organized critical state. Here, the magnetic subsystem acts as an internal stimulant for the magnetic flux while the superconducting subsystem works as a valve controlling the flux propagation into the sample.

Due to the specific structure of the magnetic subsystem, where Eu-spins order ferromagnetically and align within the **ab**-planes while maintaining a short-wavelength helical order along the c-axis, the magnetic response is strongly anisotropic. For **H**||**ab**, a relatively small **H** (few hundred Oe) twists the Eu-spins towards the field direction and noticeably enhances the magnetic subsystem's contribution. However, for **H**||**c** a larger field is required to tilt the Eu-spins towards **H**, as it works against the strong anisotropy that keeps the spins in the **ab**-plane. As a result, in moderate **H**||**c** (<2 kOe) the contribution of the magnetic subsystem is small and the magnetic response is dominated by the critical currents, as in regular superconductors.

The main origin of the critical current anisotropy in RbEuFe<sub>4</sub>As<sub>4</sub> is expected to be the core pinning. The maximum J<sub>c</sub> along the ab-planes may be due to the layered crystal structure of 1144 and the short coherence length of a few lattice spacings, and possible planar intergrowth defects like in CaKFe4As4. However, it is not excluded that there is a magnetic component to the pinning anisotropy, when in **H**||**ab** the helical arrangement of Eu-spins is untwisted towards a polarized state by the vortex field thus inducing additional pair breaking.

The intertwined action of the magnetic and superconducting subsystems resulting in the self-organized critical state causes intrinsic inhomogeneity in the spatial distribution of the FM and SC contributions, which should be accounted in the treatment of the macroscopic M(H,T), neutron, and other measurements in FM-SCs.

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