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Density Functional Theory Modeling of Cation Diffusion in Bulk $\text{La}_{1-x}\text{Sr}_x\text{MnO}_{3\pm\delta}$ ($x=0.0-0.25$) for Solid Oxide Fuel Cell Cathodes

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ABSTRACT:

In this work, the A- and B-site cation migration pathways involving defect complexes in bulk $\text{La}_{1-x}\text{Sr}_x\text{MnO}_{3\pm\delta}$ at $x=0.0-0.25$ are investigated based on density functional theory (DFT) modeling for solid oxide fuel cell (SOFC) cathode applications. We propose a new dominant A-site cation migration mechanism which involves an A-site cation (*e.g.* La_A^x) hop into a V_A''' of a $V_A''' - V_B'''$ cluster, where La_A^x , V_A''' , and V_B''' are La^{3+} , A-site vacancy, B-site vacancy in bulk LSM, respectively, and $V_A''' - V_B'''$ is the first nearest neighbor V_A''' and V_B''' pair. This hop exhibits a ~ 1.6 eV migration barrier as compared to a ~ 2.9 eV of the La_A^x hop into a V_A''' . This decrease in the cation migration barrier is attributed to the presence of the V_B''' relieving the electrostatic repulsion and steric constraints to the migrating A-site cations in the transition state image configurations. The $V_A''' - V_B'''$ interaction energy is predicted to be weakly repulsive (0.2-0.3 eV) in bulk LSM, which enables the $V_A''' - V_B'''$ cluster to readily form. The predicted apparent activation energy of D_{La}^* in $\text{LaMnO}_{3\pm\delta}$ (LMO) for the new A-site migration pathway is about 1.4 eV, in good agreement with the experimental A-site cation impurity diffusivity measurements. By examining the A-site cation migration barriers among different metal cations (Zr^{4+} , Y^{3+} , Gd^{3+}) relevant for SOFC applications, it is demonstrated that migration barriers of the cation impurity in bulk LSM correlate with the ionic charge and ionic radius at a given formal cationic charge. The B-site cation migration barrier takes place by an analogous mechanism that involves a Mn_B^x (Mn^{3+} on the B-site) hop into a V_B''' via the $\text{Mn}_B^x - V_A''' \rightarrow V_B'''$ path with the same cation transport carrier of $V_A''' - V_B'''$. This diffusion pathway is found to have a barrier of ~ 1.6 eV, similar to the analogous A-site hop. However, hopping of the Mn_A^x antisite defect (Mn^{3+} on the A-site) to a nearest neighbor V_A''' ($\text{Mn}_A^x(V_A''')$ mechanism) has a barrier of only ~ 0.5 eV. Such a low $\text{Mn}_A^x(V_A''')$ migration barrier opens the possibility to activate Mn transport in bulk

LSM through the diffusion of the antisite $Mn_A^x(V_A''')$ pathway on the A-site lattice, particularly when the concentration of the Mn antisite defect can be altered upon varying the A/B ratio and the activity of MnO_y . The increase in Sr'_A doping concentration in bulk $La_{1-x}Sr_xMnO_{3\pm\delta}$ ($x=0.0-0.25$) was found to influence primarily the formation energies of cation transport carriers (cation vacancies) whereas the cation migration barriers only exhibit a weak dependence on the Sr'_A concentration.

I. INTRODUCTION

Solid oxide fuel cells (SOFCs) are alternative energy and power generation sources with significant advantages of being highly efficient, fuel flexible, modular, and scalable. After several decades of research and development, SOFCs are beginning to be commercialized as reliable backup power systems and as combined power/hot water systems for residential usage. Producing systems that can perform reliably for more than 50,000 hours, enhancing the cell performance and decreasing the long-term performance degradation rate are some of the major research and development goals in the SOFC program at National Energy Technology Laboratory (NETL)[1].

Understanding the factors governing compositional and microstructural changes in cathode materials and their interfaces with electrolytes during operation is a critical aspect to SOFC performances and their long-term stability, since changes in the surface and interfacial compositions and microstructures strongly influence the available surface area and the active triple phase boundaries necessary for oxygen reduction [2,3]. In particular, for the-state-of-the-art $\text{La}_{1-x}\text{Sr}_x\text{MnO}_{3\pm\delta}$ (LSM) SOFC cathode materials, cation transport plays a critical role in controlling reaction kinetics of the secondary phase formation [4,5], segregation and changes in surface composition [6], grain growth/sintering [7-10], creep deformation [11,12], and in creation of diffuse interfaces between cell components [13,14]. Despite many phenomenological observations of microstructure and compositional evolution of LSM cathodes and their interfaces with electrolytes that are directly or indirectly associated with cation transport, fundamental mechanistic understanding is still insufficient to fully describe the experimental cation diffusivities including their dependences on temperature (T), partial pressure of oxygen ($p\text{O}_2$), and applied potentials, in both bulk LSM and its interfaces under SOFC operating conditions [13,15-17]. Several experimental studies have reported the LSM and $\text{LaMnO}_{3\pm\delta}$ (LMO) bulk

cation diffusivities and their temperature dependences [13,15-17] and differences, ranging between 1.5-2 eV in the apparent activation energies for the cation diffusivities, were found among different experimental methods used (*e.g.* solid state reaction versus tracer diffusion and interdiffusion of diffusion couples). In addition, Sr substitution of about 20-30 atomic percent is generally introduced at the A-site of LMO as cathode materials for SOFCs in order to promote electronic conductivity, to enhance the oxygen reduction activity, and to increase chemical and mechanical stability with yttria stabilized zirconia (YSZ) electrolytes [18,19]. However, limited experimental cation diffusivities can be found in the literature for Sr-substituted LMO[13], and it remains unclear how cation diffusivities in LSM and their temperature dependencies couple to the Sr substitution level.

Due to the closed packed nature of perovskite lattice, which electrostatically and sterically hinders formation of cation interstitials, the cation diffusion in crystalline LSM primarily takes place *via* cation-vacancy mediated diffusion mechanisms [15-17,20]. Since nonstoichiometry and defect concentration (for both cation and anion vacancies) can be substantial in bulk LSM, understanding of the LSM bulk defect chemistry is critical to systematic interpretation of the experimental cation tracer diffusivity results [15,17,20,21]. Specifically, the cation vacancy concentration is up to 1~5% in LMO and LSM in air under the typical SOFC operating temperatures [15,17,20-22], a fact that can facilitate long range cation diffusion. Based on the experimental oxygen nonstoichiometry measurements and by solving a system of coupled nonlinear equations associated with metal conservation, lattice site balance, charge neutrality, and equilibrium constants of the major defect reactions, detailed information on point defect concentrations in LSM bulk versus T and pO_2 can be systematically modeled [23-27]. *Ab initio* based defect formation energies, defect interaction energies and entropies can

be further used to verify the model assumptions associated with the key defect reactions in LSM, thereby reducing the defect model uncertainty and yielding insight to defect interactions in bulk LSM [27].

In addition to the carrier concentrations for cation transport, activation barriers of cation migration also have to be determined to predict the rates of the cation diffusion. While several possible cation diffusion pathways have been proposed in the previous studies, including transport of cation vacancy complexes in bulk LMO/LSM [15,17,20,21,28,29] or related SOFC perovskites such as $\text{La}_{1-x}\text{Sr}_x\text{Ga}_{1-y}\text{Mg}_y\text{O}_{3-(x+y)/2}$ [30,31], only few theoretical studies were performed to date to simulate the cation migration barriers [20,29,30]. Energy differences of ~ 1 eV were found among the simulated A-site cation migration barriers mediated by an A-site vacancy in bulk LMO between the empirical potentials method as described in Ref. [20] versus the DFT results in Ref [29]. By incorporating the calculated migration barriers from the two studies in conjunction with kinetic Monte Carlo (kMC) simulations [29], it was further shown that significant differences in the magnitude of the predicted A-site cation diffusivities exist [29]. Nonetheless, in the absence of the experimental results specific to the simulated LSM compositions ($x=0.2-0.3$), the accuracy of the corresponding computed migration energies provided in Refs. [20,29] cannot be verified. Furthermore, both the simulated A-site cation migration barriers obtained using DFT modeling [29] and empirical potentials [20] are still at least 1-2 eV higher than the experimentally extracted apparent activation energies for Pr impurities on A-sites in LMO [32], which suggests that there may exist alternative lower-barrier cation migration pathways.

As with A-site diffusion, the understanding of the B-site diffusion mechanisms in LSM is still quite poor. For example, an active Mn cation diffusion pathway was suggested to involve a

B-site metal hopping *via* an A-site-and-B-site vacancy cluster [16,21,28], but concentration of the A-site-and-B-site vacancy clusters in LSM is not directly available from solving the LSM bulk point defect models and consequently it is difficult to assess the predictive ability of this diffusion model. An energy difference of ~ 2.2 eV was found by Miyoshi *et al.* [16] by comparing the experimental apparent activation energies of the Mn tracer diffusivities in LMO with the reported migration barriers determined based on empirical potential simulations [20] and by taking into account the estimated effective formation enthalpy of the cation vacancies based on experimental oxygen nonstoichiometry measurements [23]. Miyoshi *et al.* hypothesized that the 2.2 eV difference could be compensated by a -2.2 eV attraction between an A-site vacancy and a B-site vacancy [16], but they also pointed out that justification of such a strong attraction interaction needed additional theoretical simulations or experimental measurements for validation.

In this work, the cation transport mechanisms and their migration barriers in bulk $\text{La}_{1-x}\text{Sr}_x\text{MnO}_{3\pm\delta}$ at $x=0.0-0.25$ under the SOFC operating conditions are investigated based on the density functional theory (DFT). Combining with the bulk LSM defect modeling, the cation diffusion coefficients are assessed from both the concentration of the transport carriers, including concentration of relevant defect clusters and their temperature dependences, as well as the migration barriers associated with the A-site and B-site cation transport in bulk LSM. The main goal of this study is to employ first principles DFT calculations to determine the cation transport mechanisms with a goal of resolving the existing discrepancies between the theoretical modeling and the available experimental LSM cation diffusivities, as well as to identify how such diffusion might be manipulated to improve LSM SOFC cathode stability. This work is organized as follows: Section II describes the computational modeling approaches used in this study, Section

III discusses the $\text{La}_{1-x}\text{Sr}_x\text{MnO}_{3\pm\delta}$ bulk defect modeling and the defect interactions used to extract transport carrier concentration *versus* T and $p\text{O}_2$, Section IV summarizes the theoretical results of the investigated cation migration mechanisms and the corresponding barriers in bulk LSM, Section V discusses the T dependences of the cation tracer diffusion coefficients in bulk LSM at $x=0.0$ and 0.3 based on a three-dimensional random walk diffusion model, and Section VI contains the summary and conclusions of this work.

II. COMPUTATIONAL MODELING APPROACHES

A. Density functional theory modeling methods

Spin-polarized DFT calculations were performed with the Vienna *Ab-initio* Simulation Package[33,34] (VASP) using the projector-augmented plane-wave (PAW) method [35]. Exchange-correlation is treated using the Perdew-Burke-Ernzerhof [36] (PBE) Generalized Gradient Approximation (GGA). The GGA+ U calculations [37] were performed with the simplified spherically averaged approach [38], where the U_{eff} ($U_{\text{eff}} = \text{Coulomb } U - \text{exchange } J$) was applied to the d -electrons of Mn with $U_{\text{eff}}(\text{Mn}) = 4.0$ eV [27,39,40].

The electronic configurations of the species and their names in the VASP supplied PAW potentials were La (5s2 5p6 6s2 5d1), Sr (4s2 4p6 5s2), Mn_{pv} (3p6 3d6 4s1), and O (normal oxygen) (2s2 2p4). The plane wave energy cutoff was 600 eV, and a Monkhorst-Pack [41] k-point mesh equivalent to $8 \times 8 \times 8$ for the primitive perovskite unit cell was used to sample the Brillouin zone.

An orthorhombic supercell ($\mathbf{a}_{\text{supercell}} = \mathbf{a}_{\text{orthorhombic}} - \mathbf{b}_{\text{orthorhombic}}$, $\mathbf{b}_{\text{supercell}} = \mathbf{a}_{\text{orthorhombic}} + \mathbf{b}_{\text{orthorhombic}}$, $\mathbf{c}_{\text{supercell}} = \mathbf{c}_{\text{orthorhombic}}$, where $\mathbf{a}_{\text{orthorhombic}}$, $\mathbf{b}_{\text{orthorhombic}}$, and $\mathbf{c}_{\text{orthorhombic}}$ are the lattice constants of the experimental orthorhombic LSM[42]) was first constructed based on the experimental symmetry[42] and then fully relaxed in the ferromagnetic state in the DFT

simulations. The lattice constants of the 20-atom supercell were then set to be equal to the cube root of the relaxed volume, and then by performing iterations between the internal relaxation and volume relaxation (with fixed atomic coordinate and shape). This approach allows to maintain the BO_6 octahedral rotation in the supercell during ionic relaxation while maintaining a cubic shape [27,40]. The constructed supercells are analogous to a $2a_{\text{cubic}} \times 2a_{\text{cubic}} \times 2a_{\text{cubic}}$ cubic perovskite supercell (a_{cubic} is the lattice constant of the cubic perovskite). These settings were used to approximate the geometric characteristics of the conductive cubic paramagnetic phases of LMO and LSM that occur at typical SOFC operating temperatures (600~800°C), and provide a consistent and tractable set of magnetic structures [27,40]. Larger supercells were further constructed based on the $2a_{\text{cubic}} \times 2a_{\text{cubic}} \times 2a_{\text{cubic}}$ pseudo-cubic perovskite supercell, including a 40-atom $2\sqrt{2}a_{\text{cubic}} \times 2\sqrt{2}a_{\text{cubic}} \times 2a_{\text{cubic}}$, a 80-atom $2\sqrt{2}a_{\text{cubic}} \times 2\sqrt{2}a_{\text{cubic}} \times 4a_{\text{cubic}}$, and a 320-atom $4a_{\text{cubic}} \times 4a_{\text{cubic}} \times 4a_{\text{cubic}}$ supercells for defect formation and cation migration barrier calculations. For the defect calculations, relaxation of the atomic positions was conducted until Hellmann–Feynman forces are below 1 meV Å⁻¹. All the LMO and LSM defect calculations in this work are performed using neutral supercells (without manual adjustment of the charge in the supercell), and therefore the introduced defect charge in the supercell is automatically accommodated. Cation migration energies were simulated using the climbing image nudged-elastic-band method (cNEB) at $x=0.25$ with at least three images per calculation[43].

For LSM, the Sr'_{A} dopant (Sr^{2+} dopant in an A-site lattice based on the Kröger-Vink notation [44]; the symbols of the ionic and defect species in bulk LSM adopted in this work are summarized in the Table S1 of the Supplemental Material (SM)[45]) are introduced in the simulated supercells at the concentration $x=0.25$, for calculating the defect energetics and cation migration energies. Considering the repulsive interaction between Sr'_{A} dopants, a Sr'_{A} ordering

with the farthest separation of all the Sr'_A dopants in the simulated supercells was used in the defect and migration barrier calculations (as shown in Figure S1 of SM[45]). Two additional Sr configurations were investigated to compare the energetic differences among different Sr configurations (Figure S1 of SM[45]). Our results indicate that the dependences of the cation migration barriers on Sr configuration in bulk $La_{0.75}Sr_{0.25}MnO_3$ are weak, as the migration barrier differences among the three Sr arrangements in bulk LSM are within 0.1 eV for the active La and Mn migration pathways, as shown in Figure S2 of SM[45]. The effect of the magnetic ordering on cation migration barriers of the energetically most favorable pathways was also examined. Comparing the results of the ferromagnetic and the stable A-type antiferromagnetic calculations, it was found that the differences in the barriers are ~ 0.1 eV, as shown in Figure S3 of SM[45]. This relatively small change between ferromagnetic and stable antiferromagnetic structures suggests that the migration barriers are only weakly affected by the magnetic state, supporting our use of a simple ferromagnetic structure in-place of the disordered paramagnetic structure. While the G-type antiferromagnetic ordering was previously adopted to simulate the oxygen vacancy formation energies vs. Sr concentration in LMO (between $x=0$ and $x=0.5$), in the case of high temperatures in the paramagnetic state[46], this particular G-type antiferromagnetic state has been shown to be an energetically unfavorable state in LMO using both the PBE and hybrid functional calculations as compared to the A-type and C-type antiferromagnetic ordering[47], and is therefore not included in our DFT cation migration simulation.

The calculated migration barriers exhibit a weak energy dependence on the supercell sizes (*i.e.* defect concentration, see Table S2 of SM[45]), with a difference of ~ 0.3 eV or less between the 80-atom, 160-atom, and 320-atom supercells. This range of the ~ 0.3 eV barrier variation

contains at least two types of defect concentration effects among different supercell sizes: 1. Nondilute cation vacancy concentration in bulk LSM at thermodynamic equilibrium for calculating the migration barriers - considering the high cation vacancy concentration in LSM at $x=0-0.25$ in air under SOFC operating temperature[23], it is desirable to use the supercell size with cation vacancy concentration close to equilibrated oxygen over-stoichiometry; 2. The self-interaction of the migrating cations in the finite size supercell where there is spurious defect interaction. The latter is considered to be a weaker contribution based on the first order correction term for the electrostatic interaction in the finite size supercell [48], due to moderately high dielectric properties under the SOFC conditions [49]. Although the supercell size dependences of the defect energetics and the migration barriers can be further performed to extrapolate to a dilute limit, a thorough investigation requires significant computation time and make the complex studies being developed here impractical. Therefore, in this work the cation migration barriers used for calculating cation diffusion coefficients are based on the results simulated with the $2\sqrt{2}a_{cubic} \times 2\sqrt{2}a_{cubic} \times 2a_{cubic}$ and $2\sqrt{2}a_{cubic} \times 2\sqrt{2}a_{cubic} \times 4a_{cubic}$ pseudo-cubic supercells, as shown in Figure S4(a) of SM[45]. These cell sizes likely produce errors of about ~ 0.2 eV in the calculated barriers due to the finite size effects based on the weak dependences to the Sr disorder configurations and supercell sizes.

B. $\text{La}_{1-x}\text{Sr}_x\text{MnO}_{3\pm\delta}$ bulk defect modeling

To calculate the concentration of transport carriers for cation diffusion in bulk LSM at $x=0$ and 0.2, we first solve the $\text{La}_{1-x}\text{Sr}_x\text{MnO}_{3\pm\delta}$ bulk defect model by combining the defect energetics simulated with *ab initio* modeling [27] and the defect formation entropies (estimated based on empirical thermodynamic free energy/entropy data of the O_2 gas phase and a simple Einstein model for the exchanged O^{2-} ions in the solid phase)[40]. The experimental $\text{LaMnO}_{3\pm\delta}$ and

$\text{La}_{0.8}\text{Sr}_{0.2}\text{MnO}_{3\pm\delta}$ oxygen nonstoichiometry versus $p\text{O}_2$ and T data measured by thermogravimetry analysis (TGA)[23,50] were then used to serve as empirical constraints for adjustment and validation of the *ab initio* based defect model parameters. TABLE I summarizes the defect formation energies, defect concentration-dependent nonideal terms, and defect formation entropies used in the defect modeling. Details of the LSM bulk defect modeling approach used in this work are described in Ref. [27] and in Section S1 of SM[45]. An additional artificial constraint requiring an equal amount of $[V_A''']$ and $[V_B''']$ in bulk LMO and LSM was also imposed in this defect model, which is based on the nominal A/B ratio of the LMO/LSM samples used in the experimental measurements [23,50]. It is also noted that in the discussions below, the DFT defect interaction energies of the bulk LSM simulated at $x=0.25$ are directly used to calculate the defect cluster concentrations at $x=0.2$ based on the bulk defect model that was fit with the experimental oxygen nonstoichiometry, as shown in Figure S5 of SI. Similarly, the cation migration barrier calculations simulated at $x=0.25$ are directly used in combination with the bulk defect model for assessing the T dependences of the cation diffusivities at $x=0.2$.

C. Simple random walk assessment of the cation self-diffusion coefficients

The relevant point and cluster defect concentrations, and the cation migration barriers of the possible diffusion pathways obtained using the methods described above have been further incorporated into a three-dimensional random walk diffusion formalism to assess the terms in an Arrhenius expression for the cation diffusion coefficients in bulk $\text{La}_{1-x}\text{Sr}_x\text{MnO}_{3\pm\delta}$ ($x=0.0$ and 0.2). Further optimization is then performed by fitting the Arrhenius expression prefactor, which is due to factors such as the migration entropy and the attempt frequency, to the experimental cation diffusivities. The generalized form of the cation tracer diffusion coefficients based on the three-dimensional random walk formalism can be described as the following [51]:

$$D_{cat}^* = \left[A \cdot \frac{Z}{6} \cdot d^2 \right] \cdot [def(T, pO_2)] \cdot \exp \left(-\frac{\Delta E_{mig}}{k_b T} \right)$$

Eqn. 1

where $[def(T, pO_2)]$ is concentration of defect carriers as a function of T and pO_2 for cation diffusion, Z is the number of neighboring sites to which the defect can migrate, d is the jump distance (*e.g.* lattice constant of LSM perovskites), ΔE_{mig} and ΔS_{mig} are the energy and entropy of migration, k_b is the Boltzmann constant, and T is temperature. The first bracket in Eqn. 1 is a constant $A = f^* \cdot \nu_0 \cdot \exp \left(\frac{\Delta S_{mig}}{k_b} \right)$, where f^* is the correlation factor and ν_0 is the attempt frequency, will be fit to experimental cation diffusivities. More details of the diffusion coefficient formalism are provided in Section S2 of the SM[45]. It is noted that for a cluster mechanism the correlation factor f^* can become a function of the individual defect jump frequencies and the defect concentrations[51]. In principle, the tracer correlation factors can be assessed by Monte Carlo simulations or analytic solutions with given jump frequencies and paths of the species. For example, Belova *et al.* [52] performed such an analysis on the La_{1-x}

$x\text{Sr}_x\text{Ga}_{1-y}\text{Mg}_y\text{O}_{3-(x+y)/2}$ perovskite and obtain the tracer correlation factor ratio as a function of the exchange frequency ratio for the vacancy cluster diffusion mechanisms proposed by Schultz *et al.*[31]. However, since the identified active cation diffusion pathways in LMO and LSM in this study are different from the cluster diffusion mechanisms in the LSGM perovskite oxides (as will be discussed in Section IV below), such an analysis has to be performed additionally for LMO/LSM based on the energy landscapes of the possible cation diffusion pathways. In the first approximation this study assumes that the tracer correlation factors exhibit no or weak temperature dependences in the temperature regime where the experimental cation diffusivity measurements were performed. Consequently, the temperature dependences in the calculated cation tracer diffusion coefficients following Eqn. 1 mainly come from the defect energetics of the transport carriers and the associated migration barriers of the cation migration mechanisms.

III. $\text{La}_{1-x}\text{Sr}_x\text{MnO}_{3\pm\delta}$ BULK DEFECT CHEMISTRY AND DEFECT INTERACTIONS

A. Point defect concentration in bulk $\text{La}_{1-x}\text{Sr}_x\text{MnO}_{3\pm\delta}$ versus T and $p\text{O}_2$

The point defect concentrations ($[\text{Mn}_B^x]$, $[\text{Mn}_B^\bullet]$, $[\text{Mn}_B']$, $[\text{V}_A''']$, $[\text{V}_B''']$, and $[\text{V}_O^{\bullet\bullet}]$ indicated using Kröger-Vink notation; description of the symbols used in this work is summarized in the Table S1 of SM[45]) *versus* $p\text{O}_2$ at T=1073 K, 1273 K, and 1473 K can be extracted by solving the $\text{LaMnO}_{3\pm\delta}$ and $\text{La}_{0.8}\text{Sr}_{0.2}\text{MnO}_{3\pm\delta}$ bulk defect model, and are provided in the Brouwer diagrams [53] of FIG. 1. The model predicted versus the experimental oxygen nonstoichiometry results are shown in Figure S5 of the SM[45]. Again, it is noted that an artificial constraint corresponding to an equal amount of $[\text{V}_A''']$ and $[\text{V}_B''']$ in bulk LMO and LSM was imposed in the defect model. The influence of varying A/B ratio of LSM on the bulk oxygen nonstoichiometry/defect chemistry[54,55] and ionic diffusivities[7,18] remains an open topic of

interest for further theoretical modeling and experimental measurements. In Section III B below, the extracted LSM bulk point defect concentration at the A/B ratio equal to 1 under SOFC operating conditions is utilized to assess the carrier concentration of the defect complexes that are involved in the cation transport mechanisms, based on the calculated defect interaction energies.

B. Defect interactions and concentration of defect clusters

For the investigated cation diffusion mechanisms (as will be discussed in more detail later in Section IV), the defect-complexes of $V_A''' - V_B'''$, $V_O^{\bullet\bullet} - V_A'''$, $V_O^{\bullet\bullet} - V_B'''$, and $V_O^{\bullet\bullet} - V_A''' - V_B'''$ are involved as the cation transport vehicles. To assess the LSM cation diffusion coefficients of these cation transport mechanisms, it is important to calculate the concentration of the defect-complexes as a function of T, to separate the contributions of the associated defect energetics from the migration barriers. For practical considerations[27], the concentrations of the defect complexes are calculated directly through the defect association reactions using the defect interaction energies obtained from DFT simulations (as detailed below), whereas other terms such as configurational and vibrational entropy are neglected. We note that even if such an approximation could introduce certain errors through neglecting the configurational entropy terms (estimated to be ~ 1 order of magnitude in concentration of the species) in the predicted defect cluster concentration, the main focus of this work is on the mechanistic information of the cation migration, which is less sensitive to the errors introduced in the absolute quantities of the cation diffusivities.

Taking the reaction to form a $V_A''' - V_B'''$ defect complex as an example, a defect association reaction can be written as:



where the equilibrium constant of the defect association reaction can be calculated as:

$$K_{\text{association}} = \exp \left(- \frac{\Delta E_{\text{association}}}{k_b T} \right) = \frac{[V_A''' - V_B''']}{[V_A'''][V_B''']} \quad \dots \text{Eqn. 3}$$

$\Delta E_{\text{association}}$ is obtained from total energy differences between a $4a_{\text{cubic}} \times 4a_{\text{cubic}} \times 4a_{\text{cubic}}$ perovskite supercell with a first nearest neighbor $V_A''' - V_B'''$ defect pair versus that with a

farthest neighbor defect pair in the DFT simulations. More details of the defect configurations and defect interaction energy calculations are provided in the Figure S4 of SM[45]. Therefore, the concentration of the defect complex $[V_A''' - V_B''']$ in $\text{La}_{1-x}\text{Sr}_x\text{MnO}_{3\pm\delta}$ can be calculated as

$$[V_A''' - V_B'''] = [V_A'''] \cdot [V_B'''] \cdot \exp\left(\frac{-\Delta E_{\text{association}}}{k_b T}\right) \quad \dots \text{Eqn. 4}$$

where $[V_A''']$ and $[V_B''']$ can be obtained from the bulk defect model (FIG. 1). It is noted Eqn. 4 implicitly assumes $[V_A''' - V_B'''] \ll [V_A'''] (= [V_B'''])$ and before calculating the corresponding association (interaction) energy $[V_A''' - V_B''']$ cannot be known. The obtained $[V_A''' - V_B''']$ from Eqn. 4 is further used to calculate the concentration of $[V_O^{\bullet\bullet} - (V_A''' - V_B''')]$, following the same derivation as described above and using the calculated DFT interaction energies from a first nearest neighbor $V_O^{\bullet\bullet} - (V_A''' - V_B''')$, relative to the separate $V_A''' - V_B'''$ and $V_O^{\bullet\bullet}$ systems in a $4a_{\text{cubic}} \times 4a_{\text{cubic}} \times 4a_{\text{cubic}}$ pseudo-cubic supercell. For Sr'_A diffusion, the $\text{Sr}'_A - V_A'''$ defect cluster is also regarded as the transport carrier, and the $\text{Sr}'_A - V_A'''$ interaction is estimated to be +0.2 eV based on the $\text{Sr}'_A - V_A'''$ interaction energy versus the pair distance profile reported in Ref. [29], and by assuming the 2nd nearest neighbor $\text{Sr}'_A - V_A'''$ pair (~ 5.6 Å) is the stable configuration in LSM.

TABLE II summarizes the calculated DFT defect interaction energies of $V_A''' - V_B'''$, $V_B''' - V_O^{\bullet\bullet}$, $V_A''' - V_O^{\bullet\bullet}$, $V_A''' - V_B''' - V_O^{\bullet\bullet}$, and $\text{Sr}'_A - V_A'''$ in bulk $\text{La}_{1-x}\text{Sr}_x\text{MnO}_3$ at $x=0.0$ and 0.25. The defect interaction energies are calculated by taking the total energy difference of the nearest neighbor defect pair versus the separated defect pair (at least 8 Å) in a 320-atom LSM bulk supercell, with sampling of three or more defect pairs for each defect-pair type on different lattice sites. A range of the calculated defect interaction energies is provided in TABLE II based on the sampled configurations, which considers the range of the calculated defect interaction

energies among the sampled defect configurations. More details of the defect configurations used to calculate the defect interactions are provided in Figure S4(b) of SM[45]. We note that the defect interaction energy assessment performed here is mainly to evaluate the relative energy scale of the defect interactions for the different types of defect clusters involved in the cation transport. Lattice Monte Carlo simulations based on the cluster expansion approach can be further performed to obtain more detailed descriptions of the potential energy profiles[56].

FIG. 2 shows the calculated concentration of the defect complex, $V_A''' - V_B'''$, $V_A''' - V_O^{\bullet\bullet}$, $V_B''' - V_O^{\bullet\bullet}$, and $V_A''' - V_B''' - V_O^{\bullet\bullet}$ versus $1/T$ ($T=1073-1473$ K) at $pO_2=0.2$ atm for $La_{1-x}Sr_xMnO_{3\pm\delta}$ at $x=0.0$ and 0.2 based on the point defect concentration extracted from the bulk LSM defect model and the defect interaction energies in TABLE I. The effective formation energies of the defect complexes are also extracted from the slopes of log concentration versus $1/T$. These results suggest:

1. **Weak repulsive interaction energies exist between V_A''' and V_B'''** – The slopes of log $[V_A''']$ (or $[V_B''']$) versus $1/T$ suggest slightly negative effective formation energies, which can be explained by the oxygen over-stoichiometry versus $1/T$ of LSM at $x=0.0$ and 0.2 in the temperature range of $1073-1473$ K in air (the cation vacancy content can be calculated based on the oxygen over-stoichiometry). More specifically, since the calculated $V_A''' - V_B'''$ interaction energies are $+0.34$ eV at $x=0.0$ and $+0.17$ eV at $x=0.25$, they have a relatively weak repulsive interaction compared to their overall formation energies, so the temperature dependences of $[V_A''' - V_B''']$ is close to $[V_A''']*[V_B''']$ (Eqn. 4).
2. **Moderate attractive interaction energies for the $V_O^{\bullet\bullet} - V_A'''$, $V_O^{\bullet\bullet} - V_B'''$, and $V_O^{\bullet\bullet} - (V_A''' - V_B''')$ defect clusters** – The DFT simulations suggest there is a moderate attractive interaction ($0.5-1.3$ eV) between $V_O^{\bullet\bullet}$ and V_A''' , V_B''' , as well as the $V_O^{\bullet\bullet} - (V_A''' - V_B''')$

cluster in bulk LSM, in comparison with the weak repulsive interaction energy between V_A''' and V_B''' . Such an attractive interaction between $V_O^{\bullet\bullet}$ and the cation vacancies further results in a higher population of the $V_O^{\bullet\bullet}$ containing defect cluster (including $V_O^{\bullet\bullet} - V_A'''$ and $V_O^{\bullet\bullet} - V_B'''$ in FIG. 2) relative to the isolated $V_O^{\bullet\bullet}$ (red lines in FIG. 2) in air between $T=1073-1473K$. This result indicates that modeling of oxygen diffusion in over-stoichiometric LMO and LSM has to take into account the associated $V_O^{\bullet\bullet} - V_A'''$, $V_O^{\bullet\bullet} - V_B'''$, and $V_O^{\bullet\bullet} - (V_A''' - V_B''')$ species and their potential energy profiles (defect interactions as a function of the defect pair distances) and migration barriers, which requires further computational modeling studies and simulations (not a focus of this work). The influences of the defect interactions to the oxygen diffusivity in bulk LSM can also be supported by the experimental results of similar oxygen diffusivities in the LSM with different A-site deficiency and Sr doping[57], where a different $V_O^{\bullet\bullet}$ concentration is expected from the bulk defect models.

Upon assessment of concentration of the defect complexes in LSM based on the calculated *ab initio* interaction energies and point defect concentration extracted from the bulk defect model, multiple A-site and B-site cation migration pathways and their barriers are simulated based on the DFT modeling, as will be discussed in Section IV below, which can be incorporated into the random walk diffusion model formalism to assess the T dependences of the A-site and B-site cation diffusivities in bulk LSM.

IV. CATION DIFFUSION MECHANISM AND MIGRATION BARRIERS

A. A-site cation diffusion mechanisms and migration barriers

The A-site cation diffusion has been previously simulated by De Souza *et al.* [20] using empirical potentials, for a straight-line hop between two nearest-neighbor A-sites mediated by a V_A''' (see FIG. 3(a)). The calculated La_A^x (Sr_A') migration energy is about 3.9 eV (2.9 eV) for LSM at $x=0$ and increases to 5.3 eV (3.9 eV) at $x=0.3$. The linear increase in activation energies with increasing Sr_A' concentration was attributed to a combination of steric, electrostatic and ion polarizability factors. It was pointed out by De Souza *et al.* [20] that a strong correlation exists between the shortest oxygen–oxygen separation versus the calculated A-site migration barriers in the LSM at the orthorhombic/rhombohedral symmetry, suggesting that the distance of octahedral oxygen interstice is a critical parameter which influences the calculated A-site migration barriers.

Explicit A-site cation diffusivities based on the direct V_A''' hopping mechanism in $La_{1-x}Sr_xMnO_{3\pm\delta}$ was further modeled by Puchala *et al.* using kMC simulations in combination with the *ab initio* (A-site) migration energies and defect interaction energies between Sr_A' and V_A''' as a function of defect pair distances [29]. The *ab initio* calculations provided migration barriers of 2.96 eV and 2.42 eV, for La and Sr in LSM, respectively, which are consistently lower than the empirical potential results. Similar observation is also reported in a very recent DFT based modeling work of cation diffusion in bulk YSZ[58].

Despite the fact that the A-site cation migration barriers of the direct V_A''' hops in the DFT modeling[29] are lower than those of the empirical potential models [20], these DFT barriers are still 1.0-1.5 eV higher than the experimental apparent activation energy of the A-site cation (Pr^{3+}) impurity diffusion (~ 1.3 eV in Ref.[32]). Such a barrier difference between the theoretical

values and the experimental measurements raises the question of whether there exist alternative A-site diffusion mechanisms that are more favored than the traditional straight-line V_A''' hop. Indeed, mechanisms regarding cation migration in perovskite oxides have been suggested to involve defect clusters [21,31], whereas theoretical modeling on the barriers of the proposed pathways involving the defect clusters remain to be investigated. Therefore, in this work we consider several possible combinations of a V_A''' with other point defects as the A-site cation transport carriers, including three additional A-site cation migration pathways with hopping of V_A''' in the presence of a nearest neighbor V_B''' , $V_O^{\bullet\bullet}$, or $V_B''' - V_O^{\bullet\bullet}$ cluster, as schematically shown in FIG. 3(b)-(d). The A-site cation migration pathway of FIG. 3(d) may be considered as a part of the $V_A''' - V_B''' - V_O^{\bullet\bullet}$ cluster migration mechanism previously proposed by Schulz *et al.* [31] for the $\text{La}_{0.9}\text{Sr}_{0.1}\text{Ga}_{0.9}\text{Mg}_{0.1}\text{O}_{2.9}$ perovskite. Nonetheless, theoretical barriers for the hopping steps of these cations were not reported in the previous work [31]. Also, the A-site cation migration pathways involving the exchange of an A-site cation with a nearest neighbor V_B''' are not included in this work, as formation of such a B-site antisite defect is energetically highly unfavorable (~ 4 eV, see FIG. 1 of Ref. [29]) due to the fact that the ionic radii of the A-site cations are too large for occupying the B-site in the B-O octahedral environment. The calculated DFT La_A^x migration barriers in bulk LMO are summarized in TABLE III. It can be seen that the La_A^x migration barriers of the pathways FIG. 3(b) $(V_A''' - V_B''')_A$ and FIG. 3(d) $(V_A''' - V_B''' - V_O^{\bullet\bullet})_A$, both of which involve a nearest neighbor V_B''' , are at least 1 eV lower than that of the previously explored direct V_A''' hopping mechanism – FIG. 3(a). In contrast, the A-site cation migration barriers of the diffusion pathways FIG. 3(c) $(V_A''' - V_O^{\bullet\bullet})_A$ and FIG. 3(d) $(V_A''' - V_B''' - V_O^{\bullet\bullet})_A$, both of which contain a nearest neighbor $V_O^{\bullet\bullet}$ in the cation transport carrier, only show a few hundred meV difference as compared to those of the migration pathways

without a nearest $V_O^{\bullet\bullet}$ (FIG. 3(a) (V_A''') _A and FIG. 3(b) $(V_A''' - V_B''')$ _A, respectively), indicating that the presence of a nearest neighbor $V_O^{\bullet\bullet}$ has a relatively weak influence on the La_A^x migration barriers. The significant reduction in the La_A^x migration barriers in the presence of a nearest neighbor V_B''' and the weaker influence of the nearest neighbor $V_O^{\bullet\bullet}$ suggest a reduced electrostatic repulsion between the migrating La (La_{mig}^x) and the nearby Mn_B^x cations (reduced from $4Mn_B^x$ to $3Mn_B^x$ in the presence of a nearest-neighbor V_B''')[59], as well as better accommodation of the La_{mig}^x - Mn_B^x repulsion with a nearest neighbor V_B''' (La_{mig} - Mn_B^x distances increase from $\sim 3.0\text{\AA}$ to $3.1\text{-}3.4\text{\AA}$ with a nearest neighbor V_B''') in the saddle image configurations (as shown in FIG. 4). All these contributions are causing the decrease of the A-site cation migration barriers in bulk LMO among the investigated A-site cation migration pathways.

In addition to the weak influence in the A-site cation migration barriers, formation of $V_O^{\bullet\bullet}$ in bulk LSM is energetically unfavorable under SOFC conditions ($V_O^{\bullet\bullet}$ has a 3-4 eV formation enthalpy)[27], hence the A-site cation transport in bulk LSM involving a nearest neighbor $V_O^{\bullet\bullet}$ will not be active in the pO_2 region close to the air due to low transport carrier concentration (see above), which also leads to greater apparent activation energies in the predicted A-site cation diffusivities (larger slopes in FIG. 2). Nevertheless, a transition in the A-site cation transport mechanism from the defect complexes without $V_O^{\bullet\bullet}$ in air to the defect complexes with $V_O^{\bullet\bullet}$ is expected when the oxygen chemical potential conditions change such that the population of the $V_O^{\bullet\bullet}$ containing defect complexes become greater than those without $V_O^{\bullet\bullet}$ (e.g., a sufficiently low pO_2 or under high cathodic overpotential).

To summarize, among the investigated pathways, the A-site diffusion pathway of FIG. 3(b) $(V_A''' - V_B''')$ _A, where the A-site cation migration takes place by exchanging a V_A''' of a $V_A''' - V_B'''$

cluster with a nearest neighbor A-site cation, is the most active A-site cation diffusion mechanism in air at the SOFC operating temperature.

B. The effects of Sr doping on the A-site cation migration barrier

The effects of Sr substitution to the A-site cation migration barriers are summarized in FIG. 5. It can be seen that the DFT-based La_A^x and Sr'_A migration barriers of the traditional straight-line V_A''' hop (*i.e.*, Path 1(V_A''')_A) and the most active A-site cation migration pathway of the V_A''' hop of a $V_A''' - V_B'''$ cluster (*i.e.*, ($V_A''' - V_B'''$)_A) exhibit a weaker dependence on the Sr_x concentration ($x=0.0-0.25$) than the empirical potential results reported in Ref. [20]. A similar trend is also found in the calculated B-site cation migration barriers below (see TABLE IV in Section IV.D). The weaker Sr concentration dependence in the A-site cation migration energies in this study may be attributed to a more delocalized charge description in DFT modeling than that provided by empirical potentials[20].

C. Trends in the A-site cation migration barriers versus metal types

In addition to the La_A^x and Sr_A' migration barriers, several other metal cations used in solid electrolyte materials for the SOFC applications such as Y_A^x , Gd_A^x , and Zr_A^\bullet , were also investigated to understand the trends of the cation migration barriers versus cation types in bulk LSM/LMO. These metal cations not only possess different ionic radii, but also different ionic charges, both of which may lead to differences in the calculated A-site cation migration barriers. Here we focus on distinguishing these fundamental factors through the trends of the A-site cation migration barriers versus the metal cation types in bulk LMO, based on the most active $V_A''' - V_B'''$ migration pathway shown in FIG. 2(b) and the traditional V_A''' hop mechanism shown in FIG. 2(a).

As discussed previously in Section III.A, there is at least a ~ 1 eV difference in the calculated A-site cation migration barriers between the most active V_A''' hop of a $V_A''' - V_B'''$ cluster pathway (FIG. 3(b)) and the traditional V_A''' hop mechanism (FIG. 3(a)). When comparing the trends of the migration barriers among various metal cations, these two A-site cation migration pathways show similarity in their correlations. Specifically, the barriers increase with (1) increasing cationic charge; and (2) increasing the ionic radii at a given ionic charge, as shown in FIG. 6. The ionic charge dependence of the migration barriers further supports the role of the electrostatic repulsion between the migrating A-site cations (A_{mig}) and the nearby Mn_B^x s in the saddle point image to be a main factor governing the A-site cation migration barriers, since the calculated migration barriers correlate with the formal charge states of the cations Zr_A^\bullet , La_A^x , and Sr_A' (*i.e.*, 4+, 3+, and 2+, respectively). In addition, due to the different charge doping of the cations, local charge redistribution (and hence modification of the nearby Mn-O bonds) occurs near the migrating cation, leading to different degrees of relaxation

for the compressive strain imposed to the A_{mig} -O- Mn_B^x shell in the saddle point configuration. Specifically, upon hole doping (e.g. Sr_A'), local charge rehybridization shortens the Mn-O bonds around the A_{mig} impurity, which relieves the strain to the A_{mig} -O bonds in the saddle point image, and *vice versa* for the Zr_A^\bullet in the case of electron doping. For a given charge state and different radii (*i.e.*, La_A^x , Gd_A^x , and Y_A^x), the trend in the migration barrier is attributed to different degree of steric hindrance (or strain) imposed to the A_{mig} -O bonds in the saddle point image, and the slight differences in the A_{mig} -O hybridization only result in insignificant modification of the nearby Mn-O bonds[60]. It is noted that the opposite trend of cation migration barriers versus the ionic radii exists between the group of Zr_A^\bullet , La_A^x , and Sr_A' and the group La_A^x , Gd_A^x , and Y_A^x which suggests that the electrostatic (ionic charge) factor overrides the steric (ionic radius) factor when the formal cationic charge is varied.

D. B-site cation migration mechanisms and barriers

For the B-site cation transport in bulk LSM, six migration pathways are considered, as schematically illustrated in FIG. 7. The B-site cation migration mechanisms of the Paths 1-3 have been simulated with empirical potentials by De Souza *et al.*[20], and are investigated again in this work based on DFT modeling. The migration Path 4, $(V_O^{\bullet\bullet} - V_B''')$ _B is a first nearest neighbor V_B''' hop that is available when a $V_O^{\bullet\bullet}$ is formed in the middle of the direct V_B''' hopping pathway. The migration Paths 5 and 6, both of which contain the same defect complexes $V_A''' - V_B''' - V_O^{\bullet\bullet}$ as the B-site cation transport carriers, differ in their hopping pathways as follows: Path 5 is analogous to Path 1 with addition of a nearest neighbor $V_O^{\bullet\bullet}$, whereas Path 6 is analogous to Path 4 with addition of a nearest V_A''' . It is noted that the Path 5 has also been proposed by Schulz *et al.* as one hopping step of the $V_A''' - V_B''' - V_O^{\bullet\bullet}$ migration mechanism[31]. We note that there are no explicit theoretical barriers reported for this cation hopping step suggested originally in Ref. [31].

TABLE IV summarizes the calculated barriers of the six B-site cation migration pathways investigated in this work, along with those reported in Ref. [20] using empirical potentials method. Although the trend of the migration barriers for the Path 1- Path 3 is consistent between the two modeling methods, the DFT migration barriers are significantly lower than those simulated with empirical potentials. Comparing all the DFT based B-site cation migration barriers in TABLE IV it can be seen that among the six B-site cation migration pathways those exhibiting lower barriers are the following: Path 1 $(V_A''' - V_B''')$ _B, Path 5 $(V_A''' - V_B'''$ with $V_O^{\bullet\bullet})$ _B, and Path 6 $(V_B''' - V_O^{\bullet\bullet}$ with $V_A''')$ _B, all of which involve a nearest neighbor $V_A''' - V_B'''$ cluster as the cation transport carrier or a part of the transport defect complex. Again, for the pathways involving $V_O^{\bullet\bullet}$ as part of the B-site cation transport carrier, namely Path 5 $(V_A''' - V_B'''$ with

$V_O^{\bullet\bullet}$)_B, Path 6 ($V_B''' - V_O^{\bullet\bullet}$ with V_A''')_B, and Path 4 ($V_O^{\bullet\bullet} - V_B'''$)_B, an additional energy cost for oxygen vacancy formation in bulk LSM needs to be added in evaluation of apparent activation energies of the cation tracer and self-diffusivities in air, since the large $V_O^{\bullet\bullet}$ formation energy cannot be fully offset by its binding energy to the cation vacancies. Consequently, under typical SOFC operating conditions, the DFT energetic results suggest that the Path 1 ($V_A''' - V_B'''$)_B is the most active B-site cation migration pathway in bulk LSM among the six investigated mechanisms.

Considering Mn_B^x migration to the neighboring B-sites, the Path 1 ($V_A''' - V_B'''$)_B can have three distinct migration passages, which are labeled as 1NN, 2NN, and 3NN in FIG. 7(a). These three passages have the same Mn migration distances along the paths, while the resulting Mn_B^x positions are distinct in terms of their distances to the original Mn_B^x in the initial state. The results suggest that the 1NN Mn_B^x migration of the Path 1 ($V_A''' - V_B'''$)_B has a higher barrier (1.9-2.0 eV), whereas 2NN and 3NN Mn_B^x migration barriers are comparable (1.5-1.6 eV), as shown in Figure S6 of SM[45]. The states of the two energy peaks (with the higher one defined as the saddle point configuration) in the potential energy profiles of the Path 1 ($V_A''' - V_B'''$)_B are associated with a trigonal planar Mn-O configuration in which the migrating Mn (Mn_{mig}) is located at the center of three nearest oxygens that originally formed one of the faces of the Mn-O octahedra, as shown in FIG. 8. The 1.5-2.0 eV Mn migration barriers result from the low (trigonal) Mn-O coordination in the saddle point configuration as well as from the steric hindrance to the Mn_{mig} when crossing the smallest oxygen triangle (*i.e.* a face of the Mn-O octahedra) in the perovskite lattice. Removal of one of the trigonal plane oxygens does not lead to decrease of the migration barriers (*i.e.* Path 5), due to destabilization of the Mn_{mig} when placed in a two oxygen-coordinated environment, which counter balances the relieved steric

hindrance. The 0.3-0.5 eV higher migration barriers of the 1NN Mn_B^x migration (Table S2 of SM[45]) are associated with the spatial arrangement of the V_B''' and the Mn_{mig} , which leads to a terminal oxygen hybridized with one Mn_{mig} (and a short Mn-O bond of $\sim 1.8\text{\AA}$) in the initial state, thereby causing enhanced steric hindrance to the Mn_{mig} due to the shorter O-O distances of the trigonal face of the Mn-O octahedra. Therefore, these DFT modeling results suggest that Mn_B^x Path 1 $(V_A''' - V_B''')$ migration between the second and the third nearest neighbor B-sites is intrinsically more active than between the first nearest neighbor B-sites.

The local minimum with an energy of 1.0 eV, and respectively 1.5 eV, relative to the initial and final states between the two energy peaks in the potential energy profile corresponds to the Mn_A^x state (the Mn A-site antisite defect). The stability and concentration of the Mn_A^x defect can be dependent on the A/B ratio and the Mn_3O_4 activity[54,55] but is confined in the adopted LSM bulk defect model with the artificial constraint of a fixed A/B ratio (equal to 1). Variation of the Mn_A^x population can potentially result in alternative active pathways for the Mn transport on the A-site lattice in bulk LSM, a topic which will be further discussed in the next section.

Overall, at the cation stoichiometry of the A/B ratio equal to 1, these DFT modeling results show that among the six migration pathways investigated in this work the lowest barrier for Mn corresponds to Path 1 $(V_A''' - V_B''')$. This result also supports a previously proposed active Mn migration mechanism in over-stoichiometric LSM[15,32]. Our results also demonstrate that migration of Mn between the first nearest neighbor B-sites for the Path 1 $(V_A''' - V_B''')$ is not as active as those between the second and the third nearest neighbor B-sites, due to the presence of an undercoordinated terminal oxygen that causes enhanced steric hindrance to the Mn_{mig} . Given that the DFT-based $Mn_B^x(V_A''' - V_B''')$ migration barriers (1.5-1.6 eV) are comparable to the $La_A^x(V_A''' - V_B''')$ migration barriers, ~ 1.6 eV, and that both pathways involve the same

cation transport carriers of $V_A''' - V_B'''$, the corresponding apparent activation energies of the $Mn_B^x (V_A''' - V_B''')$ and $La_A^x (V_A''' - V_B''')$ diffusion coefficients are predicted to be comparable based on the three dimensional random walk formalism, *i.e.* ~ 1.4 eV (as shown in FIG. 10). However, the experimentally values provided in Refs. [16,17] for Mn diffusion are lower in activation energy by ~ 1 eV, suggesting that the existence of alternative Mn diffusion pathways not presently described in the $Mn_B^x (V_A''' - V_B''')$ diffusion model. Below, we discuss the transport of the Mn_A^x species as an active pathway for the Mn diffusion in bulk LSM/LMO which might explain the very low measured activation energy [16,17].

E. Mn_A^x cation migration mechanism and barriers

The existence of the Mn_A^x species has been suggested in the literature based on structural characterizations, magnetic measurements, and oxygen nonstoichiometry, particularly for the A-site deficient LSM [54,55,61,62]. Nakamura[54] revised the bulk LMO defect model and suggested that Mn_A^x concentrations of 0.01 and 0.03 can exist in the A-site deficient LMO with the A/B ratio of 0.96 and 0.92, respectively. Grundy *et al.*[55] used the CALPHAD approach to model oxygen nonstoichiometry of LMO at varying A/B cation ratios, and concluded that inclusion of the Mn_A^x species in the CALPHAD model is necessary to reproduce the experimental $La_{0.9}MnO_{3+\delta}$ oxygen non-stoichiometry at the SOFC operating temperature. In the first-principles based LMO defect modeling [27], it was also shown that stability of the Mn_A^x exhibits a low enough energy (~ 1 eV) that potentially plays a role in the LMO bulk defect chemistry. Since the A/B cation ratio in LSM may not be well-controlled in the experimental synthesis and measurements[63], deviation of the A/B cation ratio from 1 can lead to changes of the Mn_A^x concentration. Its influences on the overall Mn cation diffusivities are less clear.

As a first step to probe the Mn_A^x diffusivity, we calculate the Mn_A^x migration barrier of a first nearest neighbor $Mn_A^x - V_A'''$ hop. FIG. 9 shows the calculated potential energy profile of the Mn_A^x migration to a nearest neighbor V_A''' , as well as the initial state, saddle point image, and the final state configurations. The saddle point configuration is analogous to that of the simple V_A''' hopping for the A-site cation migration (FIG. 4(a)), and the O-O distances of the square-planar Mn-O are ~ 3.0 Å, which are shorter than those of FIG. 4(a), *i.e.* 3.2-3.3 Å. The calculated migration barrier of the $Mn_A^x - V_A'''$ hop is found to be ~ 0.5 eV, significantly lower than the barrier of the active $Mn_B^x(V_A''' - V_B''')$ migration pathway under the constraint of A/B ratio equal to 1, which suggests the $Mn_A^x(V_A''')$ pathway on the A-site lattice can potentially be

activated in parallel to the $Mn_B^x(V_A''' - V_B''')$ migration pathway when the population of Mn_A^x is increased in LSM (*e.g.* with A-site deficiency). In the Mn tracer diffusion study reported by Miyoshi *et al.*[16], a tracer layer of the radio-active isotope ^{54}Mn is added to the surface of the LMO substrate (the LMO substrate has a nominal composition of $\text{LaMnO}_{3\pm\delta}$ with the A/B ratio equal to 1), which causes a perturbation to the A/B ratio in the shallow region near the surface. Therefore, one may expect an increase of Mn_A^x concentration due to the A-site deficiency, leading to a low experimental apparent activation energy of 0.6 eV in the extracted Mn tracer diffusion coefficients. To quantify the influences of the A-site deficiency to the Mn diffusivities in bulk LSM, further work is needed to develop an improved diffusion modeling which includes the Mn_A^x species in the bulk defect model and the associated defect energetics and migration barriers of all possible Mn migration pathways in LSM at varying A/B ratios. Careful experimental cation diffusivity measurements with characterization of the cation nonstoichiometry are also needed for making comparison with such theoretical modeling.

V. TEMPERATURE AND STRONTIUM DOPING DEPENDENCES OF LSM CATION SELF-DIFFUSION COEFFICIENT

In this section, the DFT based defect energetics and migration barriers of the most active cation migration pathways in bulk LSM are incorporated in a three-dimensional random walk formalism to assess the temperature dependences of the cation diffusion coefficients. It is noted that the A/B cation ratio is fixed in the LSM bulk defect model. The absolute quantities of the modeled cation diffusion coefficient shown below are based on fitting to the experimental cation diffusion coefficients in the Arrhenius expression with the prefactor A , as described in Section II.C. The fitted value is $A=5.17\times 10^{12}$, which is physically reasonable for the parameters involved in A [51]. Specifically, the fitting is performed only to the experimental A-site cation diffusivities, as the experimental Mn diffusivities may be sensitive to variation of the A/B cation ratio. The fitted parameters of the D_{La}^* are then directly transferred to calculate the D_{Mn}^* . In principle, the refinement of the tracer correlation factors may be assessed by Monte Carlo simulations or analytical formulation with frequencies for relevant vacancy jumps of the diffusion pathways. However, given the complex energy landscapes and the new active cation diffusion pathways uncovered in this study, such an assessment is beyond the scope of this work and an assumption is made in the cation tracer diffusivity analysis below that the tracer correlation factor exhibits a weak temperature dependence and therefore the major temperature dependences in the tracer cation diffusivities come from the defect energetics for the associated transport carriers as well as the corresponding migration barriers. The main purpose of this analysis is to convert the DFT based energetics and migration barriers of the active cation migration pathways into estimates of D_{La}^* and D_{Mn}^* , to allow direct comparison of the temperature dependences with the available experimental results.

A. Apparent activation energies of the $\text{LaMnO}_{3\pm\delta}$ cation self-diffusion coefficients

FIG. 10 shows the calculated LMO cation tracer diffusion coefficients of D_{La}^* and D_{Mn}^* as a function of $1000/T$, along with the experimental cation diffusivity results reported in the literature [15-17,32]. Upon incorporation of the 1.5-1.6 eV migration barrier of $La_A^x(V_A''' - V_B''')_A$ pathway, the obtained apparent energy of the D_{La}^* is 1.4 eV which agrees very well with the experimental apparent activation energy of the Pr impurity diffusivity in bulk LMO (1.3 eV) [32]. The calculated DFT migration barrier of $Pr_A^x(V_A''' - V_B''')_A$ is close to that of $La_A^x(V_A''' - V_B''')_A$ (~ 1.6 eV), due to their similar ionic radii [64]. It is noted that the apparent activation energy of 1.4 eV of D_{La}^* is comparable to the calculated $La_A^x(V_A''' - V_B''')_A$ migration barrier, ~ 1.5 eV (Path 2 of Table III). This is due to the slightly negative effective formation energy of $[V_A''' - V_B''']$ shown in FIG. 2(a). Furthermore, the D_{Mn}^* is slightly higher than D_{La}^* in the diffusivity modeling, which is a result of greater hopping distance along the 2NN and 3NN hops of the migration pathways of $Mn_B^x(V_A''' - V_B''')_B$ than those of $La_A^x(V_A''' - V_B''')$.

In addition to the experimental apparent activation energy of LMO D_{Mn}^* reported in Ref. [16], two other experimental studies are also included in FIG. 10 for comparison, *i.e.* the solid state reaction between La_2O_3 and Mn_3O_4 [15] and the diffusion couple of LMO and LaCoO_3 [17]. A significantly higher activation energy of 2.9 eV for the Mn diffusion coefficients from Ref. [15] versus the 0.6 eV of Ref. [16] and 0.8 eV of Ref. [17] was suggested by Palcut *et al.*[17] to be due to different defect population in the perovskite phase formed in the solid state reaction (with unequal cation vacancy concentrations) versus the sintered LMO in the tracer diffusion or diffusion couple experiments. The D_{Mn}^* extracted from the solid state reaction results [15] may not be well-described by the modeled bulk D_{Mn}^* , as factors such as the chemical inhomogeneity

in LMO or participation of grain boundary transport are not included in the current bulk diffusion model. The D_{Mn}^* extracted from the diffusion couple measurements[17] are the extrapolated values to the LMO end-member, and their magnitudes are about 1 order higher than those of Ref. [16], whereas the apparent activation energy of 0.8 eV is close to that of the 0.6 eV reported by Miyoshi *et al.* [16]. The experimental apparent activation energies of 0.6-0.8 eV for D_{Mn}^* are now within the range of the two active Mn migration mechanisms discussed in Sections IV: 1.5-1.6 eV for the $Mn_B^x(V_A''' - V_B''')_B$ pathway and 0.5 eV for the $Mn_A^x(V_A''')_A$ pathway. Note that only the D_{Mn}^* of the $Mn_B^x(V_A''' - V_B''')_B$ pathway is included in FIG. 10, which can be regarded as a lower bound of the modeled D_{Mn}^* for the scenario of the A/B cation ratio equal to 1. The potentially more active pathway $Mn_A^x(V_A''')_A$ would require further in-depth modeling, due to the experimental uncertainty in the A/B ratio and the coupling of the $La_A^x(V_A''' - V_B''')_A$ transport. Still, by comparing the lower bound D_{Mn}^* results predicted in this work with the experiments, the extracted activation energy of D_{Mn}^* for the $Mn_B^x(V_A''' - V_B''')_B$ pathway is now in better agreement than the previous empirical potentials simulation results[20].

B.LSM cation self-diffusion coefficients versus Sr substitution level

FIG. 11 shows the predicted D_{La}^* in LSM at $x=0.0$ (thick green dashed lines), $x=0.2$ (thin light green dashed lines), and $x=0.3$ (olive dotted line) as well as their apparent activation energies, along with the experimental A-site cation diffusion coefficients reported in the literature (thick solid blue line) [32]. Assessment of D_{La}^* at $x=0.3$ is performed using the experimental oxygen over-stoichiometry data versus T at $P(O_2) \sim 1$ bar from Ref. [23], with the calculated $V_A''' - V_B'''$ interaction energy of 0.3 eV from TABLE II and a $La_A^x(V_A''' - V_B''')_A$ migration barrier of ~ 1.7 eV from Table S2 of SM[45] (the adopted experimental oxygen nonstoichiometry data and the predicted $V_A''' - V_B'''$ concentration is provided in Table S4 of SM[45]). The purpose of this assessment is to examine how the A-site cation diffusivities in bulk LSM are quantitatively influenced by change of the Sr substitution level. Here, the comparison is mainly focused on the A-site cation diffusivities, since the B-site cation diffusivities may vary depending on the A/B ratio.

In FIG. 11, D_{La}^* of LSM at $x=0.3$ (dotted olive line) are lowered by ~ 2.5 order, and D_{La}^* of LSM at $x=0.2$ (dotted olive line) are lowered by ~ 1 order, as compared to D_{La}^* of LSM at $x=0.0$. All the D_{La}^* between $x=0.0-0.3$ exhibit comparable apparent activation energies of 1.4-1.6 eV. It is noted that due to the use of the same $V_A''' - V_B'''$ defect interaction energy and the same migration barrier for $x=0.2$ and $x=0.3$ (based on the Sr doping concentration of the simulated LSM supercell at $x=0.25$), a 0.1 decrease of the apparent activation energy of D_{La}^* at $x=0.3$ versus $x=0.2$ is a result of the variation with temperature of the cation vacancy concentration and therefore of the equilibrium oxygen nonstoichiometry. It is likely there is a small increase ($\sim 0.1-0.2$ eV) in the migration barrier due to shortened Mn-O bond length upon increasing x from $x=0.2$ to $x=0.3$ (which results in an enhanced steric constraint to the migrating cations). This may

further lead to a slightly lower D_{La}^* with a slightly higher apparent activation energy for $x=0.3$, but it cannot be resolved here due to the coarse Sr concentration grid of the simulated supercells in the DFT modeling.

Since the effective formation energies (slopes of $1/T$ dependences) of V_A''' , V_B''' , and the defect clusters $V_A''' - V_B'''$ extracted from the LSM bulk defect models at $x=0.0-0.3$ are shown to be close to 0 (see FIG. 2(a) versus FIG. 2(e) in Section III.B, and Table S3 of SI), while their concentrations differ by 0.5-1 orders of magnitude. Therefore, the overall effects of Sr_A' doping to the D_{La}^* in bulk LSM shown in FIG. 11 can be attributed to decrease of the cation transport carrier concentrations, *i.e.* a lower concentration of the $V_A''' - V_B'''$ clusters with increasing x for the A-site cation migration mechanism $(V_A''' - V_B''')_A$, as well as a slight increase in the migration barriers upon increasing x . This conclusion is further supported by the correlations between the D_{La}^* versus the cation vacancy concentration and the $V_A''' - V_B'''$ concentration provided in Figure S7 of SM[45], where the reduction of the D_{La}^* with increasing x at a given T and $P(O_2)$ mainly results from a decrease in cation vacancy concentration and of the concentration of cation transport carriers.

Overall, based on the diffusion modeling results shown in FIG. 11, the apparent activation energies of D_{La}^* (slope of the diffusion coefficients versus $1/T$) in bulk LSM at $x=0.0-0.3$ are predicted to have a weak dependence on the Sr_A' substitution level, whereas the predicted D_{La}^* exhibit 1-3 order differences in the magnitude. This finding is mainly attributed to influence of Sr substitution on the concentration of cation transport carriers.

VI. CONCLUSIONS

In this work, we performed a DFT-based modeling study to investigate the LSM defect energetics and migration barriers of the A-site and B-site cation diffusion pathways involving defect clusters. Guided by a bulk defect model which combines the DFT interaction energies of the defect clusters as well as the migration barriers of the active cation diffusion pathways, the predicted cation tracer diffusion coefficients obtained using a three-dimensional random walk formalism were found to reasonably reproduce the experimental trends of the cation diffusivity versus T . We unveil a new active cation migration mechanism involving the $V_A''' - V_B'''$ cluster as the transport carrier for the A-site cation transport, which exhibits a low migration barrier with values in the range 1.5-1.6 eV in which are in good agreement with the apparent activation energies of the experimental cation diffusivity measurements. The active B-site cation migration pathway for LSM also involves the $V_A''' - V_B'''$ defect cluster, with a calculated barrier comparable to that of the active A-site migration mechanism. It is further identified that the Mn_A^x antisite migration *via* V_A''' exhibits a low barrier of 0.5 eV for the Mn diffusion in bulk LSM, which can lead to an alternative active Mn transport pathway through hopping of $Mn_A^x - V_A'''$ on the A-site lattice, depending on the A/B cation ratio. Upon examination of the saddle configurations of the active cation transport pathways, it is revealed that the cation migration barriers can be significantly influenced by the defect cluster configurations. The diffusion barriers were found to exhibit correlations versus the ionic charges (due to electrostatic repulsion) and ionic radii (due to steric effects) among various migrating cations. The reduction of cation diffusivities in LSM with increasing Sr substitution level are further shown to be mainly due to decreases of the transport carrier concentration (*i.e.* cation vacancy and the defect clusters) and slight increase in the migration barriers. Our diffusion modeling results, obtained

based on the DFT energetics and migration barriers along with a bulk LSM defect model and a three-dimensional random walk formalism, provide both the mechanistic and energetic details to uncover the active cation diffusion pathways responsible for the experimentally measured cation diffusivities. This mechanistic information, together with the energetic results obtained, provide a foundation for rationalizing phenomena associated with cation diffusion in bulk LSM at various synthetic compositions and under different operating conditions.

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This research was supported by the National Energy Technology Laboratory's on-going research in the area of property assessment of diffused interface modeling in Solid Oxide Fuel Cells.

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TABLE I. The main defect reactions and parameters used in the *ab initio* and empirical based bulk defect models for $\text{LaMnO}_{3\pm\delta}$ [27] and $\text{La}_{0.8}\text{Sr}_{0.2}\text{MnO}_{3\pm\delta}$. The interaction energy parameter in the unit of eV per defect is defined as change of the defect formation reaction energy as a function of defect concentration of $V_O^{\bullet\bullet}$ (for oxygen vacancy formation) and a separated $V_A^{\bullet\bullet}$ and $V_B^{\bullet\bullet}$ pair (for cation vacancy formation) in $\text{LaMnO}_{3\pm\delta}$ [27] and $\text{La}_{0.8}\text{Sr}_{0.2}\text{MnO}_{3\pm\delta}$.

Defect formation reaction	$\text{LaMnO}_{3\pm\delta}$ [27]			$\text{La}_{0.8}\text{Sr}_{0.2}\text{MnO}_{3\pm\delta}$		
	$\Delta E_{\text{reaction}}$, (eV)	Interaction (eV per defect)	Defect Reaction Entropy, $\Delta S_{\text{reaction}}^a$ (meV/K)	$\Delta E_{\text{reaction}}$, (eV)	Interaction (eV per defect)	Defect Reaction Entropy, $\Delta S_{\text{reaction}}^a$ (meV/K)
Oxygen vacancy formation $2\text{Mn}_B^x + \text{O}_O^x \rightarrow 2\text{Mn}_B^{\prime} + V_O^{\bullet\bullet} + \frac{1}{2} \cdot \text{O}_2^{\text{gas}}$	3.56	2.54	$-\Delta S_{\text{reaction}}^a$	2.91	1.2	$-\Delta S_{\text{reaction}}^a$
Cation vacancy formation $6\text{Mn}_B^x + \frac{3}{2} \cdot \text{O}_2^{\text{gas}} \rightarrow 6\text{Mn}_B^{\bullet} + V_A^{\bullet\bullet} + V_B^{\bullet\bullet} + 3\text{O}_O^x$	-4.07	16.10	$3\Delta S_{\text{reaction}}^a$	-3.92	59.2	$3\Delta S_{\text{reaction}}^a$
Charge disproportionation $2\text{Mn}_B^x \rightarrow \text{Mn}_B^{\bullet} + \text{Mn}_B^{\prime}$	0.06	0	0	0.00	0	0

^a $\Delta S_{\text{reaction}} = (4.552 \times 10^{-5} \cdot T - 0.894)$ for the reaction of $\text{O}^{2-}(\text{solid}) \rightarrow 1/2 \cdot \text{O}_2(\text{gas}) + 2e^-$ obtained from a linear fit of the $\Delta S_{\text{reaction}}$ vs. T plot, e.g. Figure 2 of Ref. [27]

TABLE II. Summary of the calculated DFT defect interaction energies of $V_A''' - V_B'''$, $V_O^{\bullet\bullet} - V_A'''$, $V_O^{\bullet\bullet} - V_B'''$, $V_O^{\bullet\bullet} - (V_A''' - V_B''')$, and $Sr_A' - V_A'''$ in bulk $\text{La}_{1-x}\text{Sr}_x\text{MnO}_{3\pm\delta}$ ($x=0.0$ and 0.2) within a $4a_{\text{cubic}} \times 4a_{\text{cubic}} \times 4a_{\text{cubic}}$ pseudo-cubic supercells. A range of the calculated defect interaction energies is provided in this table based on the sampled configurations.

	$x=0.0$	$x=0.25$
$V_A''' - V_B'''$	+0.2 – +0.3 eV	+0.2 – +0.3 eV
$V_O^{\bullet\bullet} - V_A'''$	-1.1 – -1.3 eV	-0.5 – -0.7 eV
$V_O^{\bullet\bullet} - V_B'''$	-0.8 – -1.0 eV	-0.6 – -0.8 eV
$V_O^{\bullet\bullet} - (V_A''' - V_B''')$	-0.7 – -1.0 eV	-1.0 – -1.2 eV
$Sr_A' - V_A'''$	--	+0.2 eV (Ref. [29])

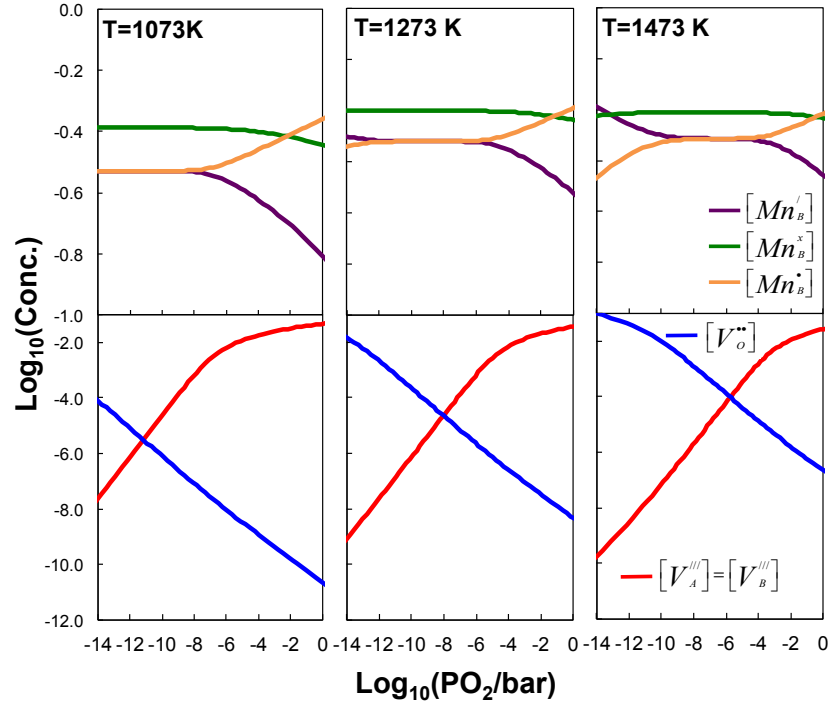
TABLE III. The DFT La_A^x migration barriers in bulk LaMnO_3 for the four diffusion pathways shown in FIG. 3, calculated using three different supercell sizes. For the 80-atom and 160-atom supercell calculations, 1-6 cNEB calculations (specific numbers provided in parentheses) are performed to account for multiple arrangements of the vacancy clusters, and the range of the calculated values are also provided in TABLE III.

La_A^x migration barrier (eV)	80-atom $2\sqrt{2}a_{\text{cubic}} \times 2\sqrt{2}a_{\text{cubic}} \times 2a_{\text{cubic}}$ supercell	160-atom $2\sqrt{2}a_{\text{cubic}} \times 2\sqrt{2}a_{\text{cubic}} \times 4a_{\text{cubic}}$ supercell	320-atom $4a_{\text{cubic}} \times 4a_{\text{cubic}} \times 4a_{\text{cubic}}$ supercell
Path 1 $(V_A''')_A -$ FIG. 2(a)	2.7-3.0 (3 calcs)	2.6-2.9 (3 calcs)	3.0 (1 calc)
Path 2 $(V_A''' - V_B''')_A -$ FIG. 2(b)	1.3-1.5 (3 calcs)	1.5-1.6 (3 calcs)	1.5 (1 calc)
Path 3 $(V_A''' - V_O^{\bullet\bullet})_A -$ FIG. 2(c)	2.9-3.1 (3 calcs)	3.0-3.3 (3 calcs)	--
Path 4 $(V_A''' - V_B''' - V_O^{\bullet\bullet})_A -$ FIG. 2(d)	1.2-1.9 (6 calcs)	--	--

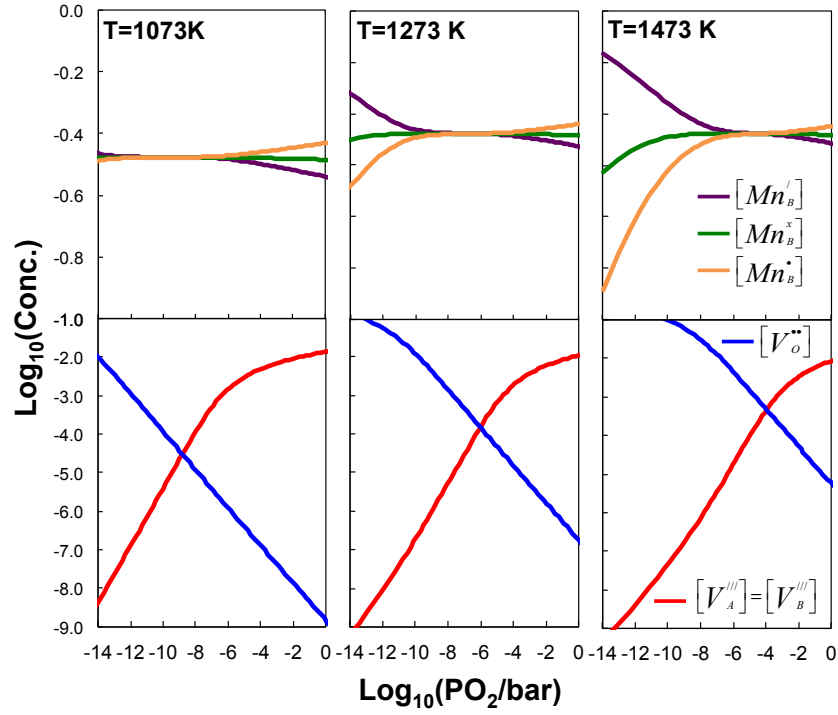
TABLE IV. Summary of the migration barriers of the four B-site diffusion pathways calculated in this work versus those reported in Ref. [20]

Mn migration barrier (eV)		$x=0.0$	$x=0.25$
Path 1 $(V_A''' - V_B''')_B$	Ref. [20]	3.5	~ 5.0
	This work (DFT)	1.5-2.0	1.7-2.3
Path 2 $(\text{curved } V_B''')_B$	Ref. [20]	7.7-10.6	10-11
	This work (DFT)	4.4	4.5
Path 3 $(2NN V_B''')_B$	Ref. [20]	14-15	--
	This work (DFT)	8.4	8.6
Path 4 $(V_O^{\bullet\bullet} - V_B''')_B$	Ref. [20]	--	--
	This work (DFT)	3.9	4.0
Path 5 $(V_A''' - V_B''' \text{ with } V_O^{\bullet\bullet})_B$	This work (DFT)	2.5	2.6
Path 6 $(V_O^{\bullet\bullet} - V_B''' \text{ with } V_A''')_B$	This work (DFT)	2.0	2.3

(a) $\text{LaMnO}_{3\pm\delta}$



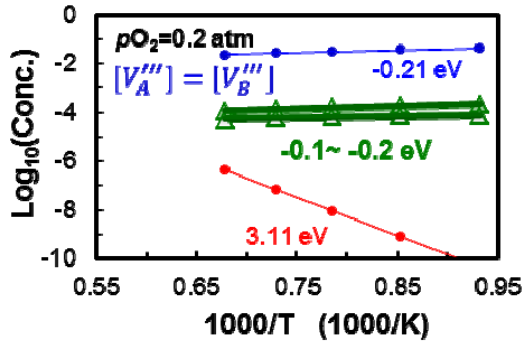
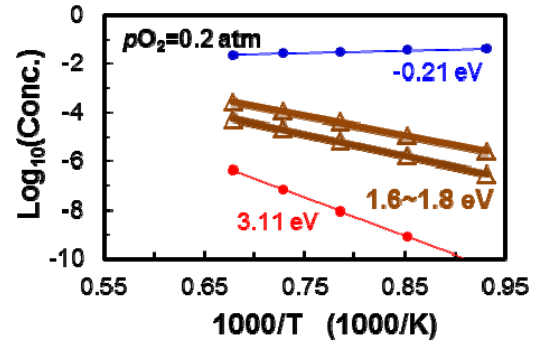
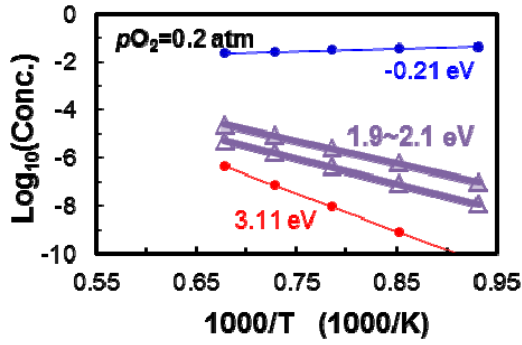
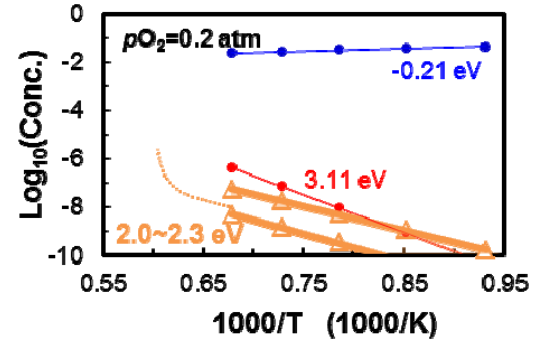
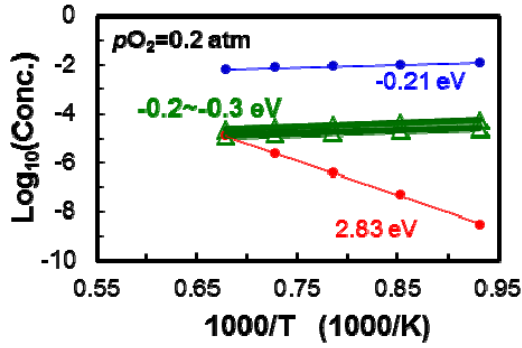
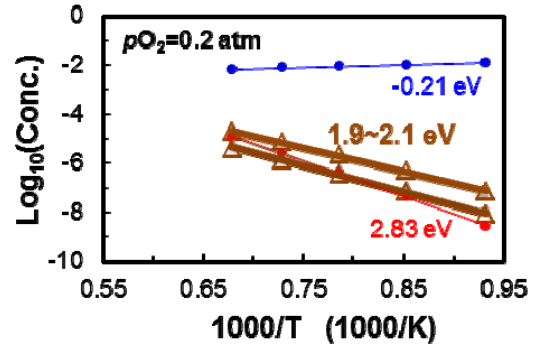
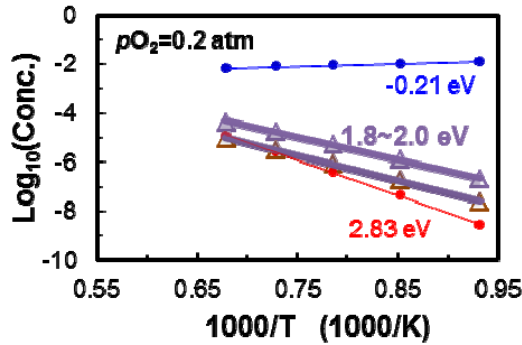
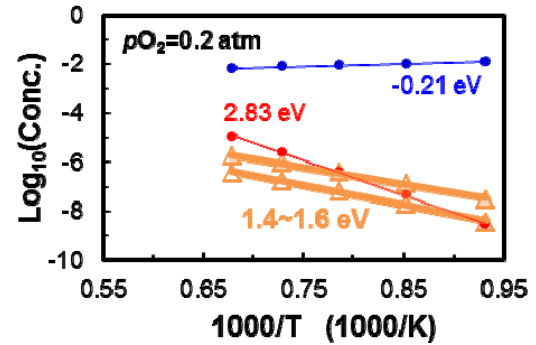
(b) $\text{La}_{0.8}\text{Sr}_{0.2}\text{MnO}_{3\pm\delta}$



(FIG. 1)

(Caption of FIG. 1)

FIG. 1. The predicted point defect concentrations ($[Mn_B^x]$, $[Mn_B^\bullet]$, $[Mn_B']$, $[V_A''']$, $[V_B''']$, and $[V_O^{\bullet\bullet}]$) versus pO_2 at T=1073 K, 1273 K, and 1473 K in the (a) $LaMnO_{3\pm\delta}$ and (b) $La_{0.8}Sr_{0.2}MnO_{3\pm\delta}$ in the Brouwer diagram. The results are based on fittings to the experimental nonstoichiometry data of LSM [23,50].

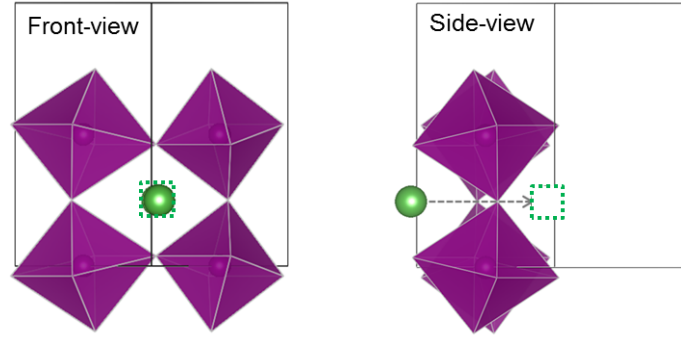
(a) $\text{LaMnO}_{3+\delta}$ (b) $\text{LaMnO}_{3+\delta}$ (c) $\text{LaMnO}_{3+\delta}$ (d) $\text{LaMnO}_{3+\delta}$ (e) $\text{La}_{0.8}\text{Sr}_{0.2}\text{MnO}_{3+\delta}$ (f) $\text{La}_{0.8}\text{Sr}_{0.2}\text{MnO}_{3+\delta}$ (g) $\text{La}_{0.8}\text{Sr}_{0.2}\text{MnO}_{3+\delta}$ (h) $\text{La}_{0.8}\text{Sr}_{0.2}\text{MnO}_{3+\delta}$ 

(FIG. 2)

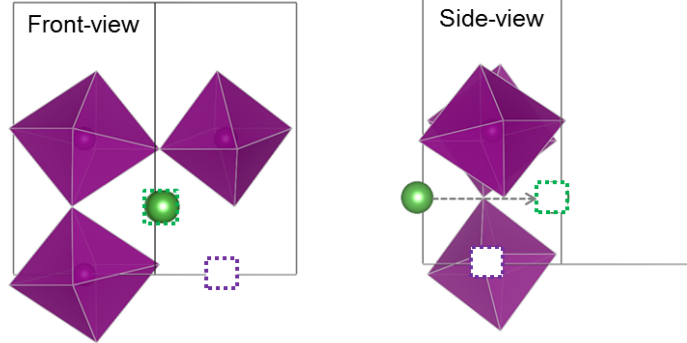
(Caption of FIG. 2)

FIG. 2. The calculated concentration of the defect complexes of (a) $[V_A''' - V_B''']$ (green triangles), (b) $[V_O^{\bullet\bullet} - V_A''']$ (brown triangles), (c) $[V_O^{\bullet\bullet} - V_B''']$ (purple triangles), and (d) $[V_O^{\bullet\bullet} - (V_A''' - V_B''')] = [V_O^{\bullet\bullet} - V_B''']$ (orange triangles) in bulk $\text{LaMnO}_{3+\delta}$ as well as (e) $[V_A''' - V_B''']$, (f) $[V_O^{\bullet\bullet} - V_A''']$, (g) $[V_O^{\bullet\bullet} - V_B''']$, and (h) $[V_O^{\bullet\bullet} - (V_A''' - V_B''')] = [V_O^{\bullet\bullet} - V_B''']$ in bulk $\text{La}_{0.8}\text{Sr}_{0.2}\text{MnO}_{3+\delta}$ at $p\text{O}_2=0.2$ atm versus $1/T$. The effective formation energies extracted from the slopes are labeled in the figures. The shaded area represents the range of the defect interaction energies based on the values of TABLE II. For comparison, concentration of $[V_A'''] = [V_B''']$ (blue circles) and $[V_O^{\bullet\bullet}]$ (red circles) versus $1/T$ and their effective formation energies are also included in each figure. All the y-axes in FIG. 2 are in the unit concentration (Conc.) in the log10 scale.

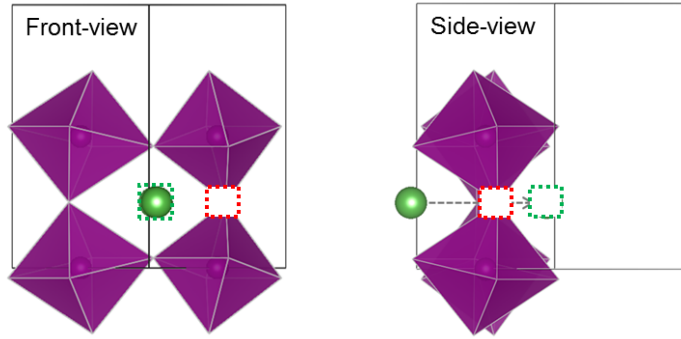
(a) Path 1(V_A''')_A



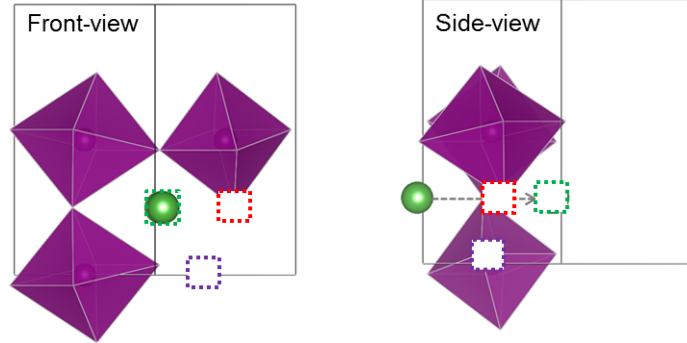
(b) Path 2($V_A''' - V_B'''$)_A



(c) Path 3($V_A''' - V_O^{\bullet\bullet}$)_A



(d) Path 4($V_A''' - V_B''' - V_O^{\bullet\bullet}$)_A

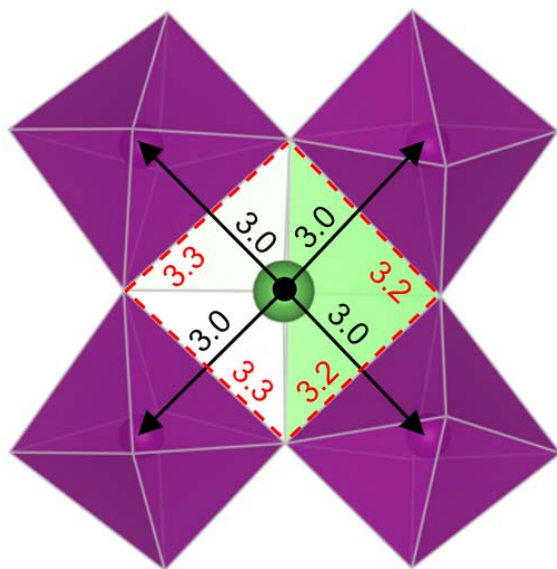


(FIG. 3)

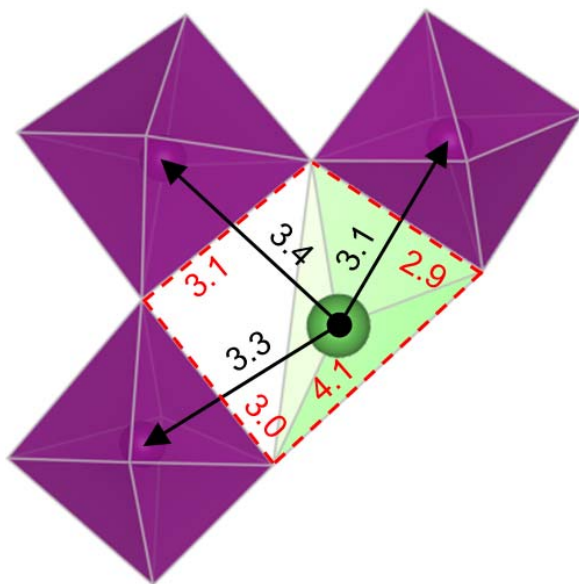
(Caption of FIG. 3)

FIG. 3. The schematic illustrations of the investigated A-site cation migration mechanisms in bulk LSM, created using the Vesta software[65] (same below): (a) the traditional straight-line V_A''' hop, (V_A''') _A, (b) the V_A''' hop in the presence of a nearest V_B''' , $(V_A''' - V_B''')$ _A, (c) the V_A''' hop in the presence of a nearest $V_O^{\bullet\bullet}$, $(V_A''' - V_O^{\bullet\bullet})$ _A, and (d) the V_A''' hop in the presence of both a nearest V_B''' and a nearest $V_O^{\bullet\bullet}$, $(V_A''' - V_B''' - V_O^{\bullet\bullet})$ _A. In FIG. 3.(a)-(d), the left plots are the front view of the respective migration pathways and the right plots are the side view of the migration pathways. Green, red, and purple dashed squares represent the V_A''' , V_B''' , and $V_O^{\bullet\bullet}$ respectively, while the green spheres and the purple octahedra represent La/Sr and Mn-O octahedra in the perovskite lattice.

(a)



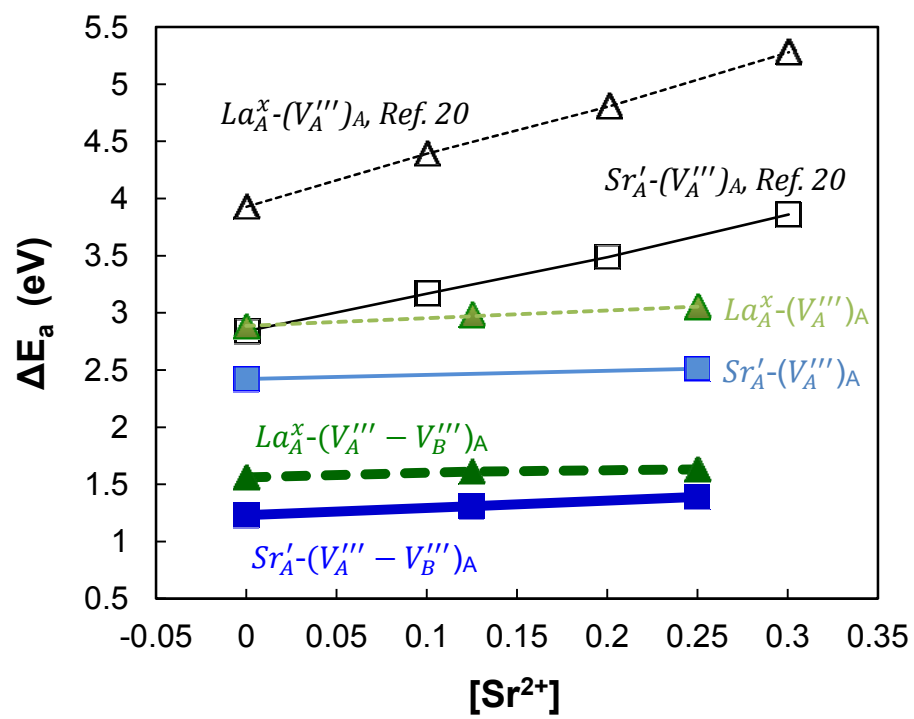
(b)



(FIG. 4)

(Caption of FIG. 4)

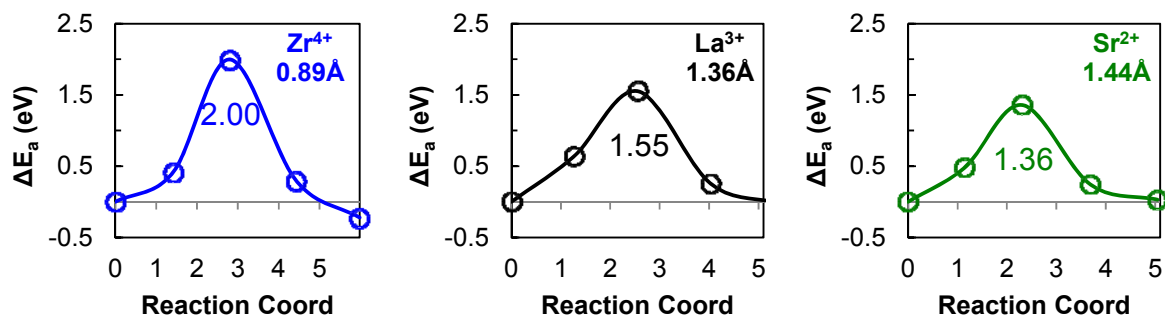
FIG. 4. The saddle point configurations of the investigated A-site cation migration mechanisms in bulk LSM: (a) the traditional straight-line V_A''' hop, $(V_A''')_A$, and (b) the V_A''' hop at presence of a nearest V_B''' , $(V_A''' - V_B''')_A$. Green spheres and the purple octahedra represent La/Sr and Mn-O octahedra in the perovskite lattice. The $La_{mig}-Mn_B^x$ distance are labeled with black solid arrows and corresponding numbers in black font (unit: Å), whereas the nearest octahedral O-O interstices are labeled with red dashed lines and numbers in red font (unit: Å).



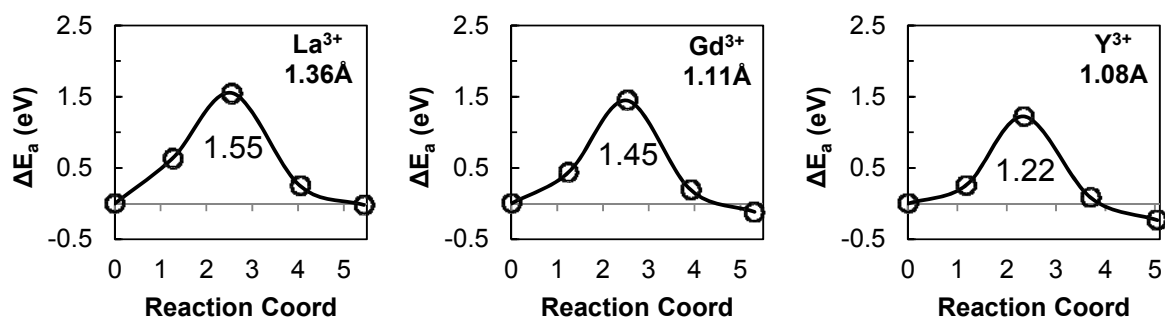
(FIG. 5)

FIG. 5. A-site cation migration energies as a function of Sr doping concentration in $\text{La}_{1-x}\text{Sr}_x\text{MnO}_3$ for the migration pathways of $(V_A''')_A$ and $(V_A''' - V_B''')_A$. The black empty symbols are taken from the empirical potentials simulations in Ref. [20], whereas the solid symbols are the migration barriers calculated using DFT in this work. Triangle and square data points represent the simulated La and Sr migration energies via a direct hop to the first nearest neighbor A-site vacancy. It can be seen in FIG. 5 that the DFT migration energies obtained in this work (solid symbols) are consistently lower than those reported in Ref. [20] based on the empirical potentials, and both exhibit different slopes versus Sr concentration.

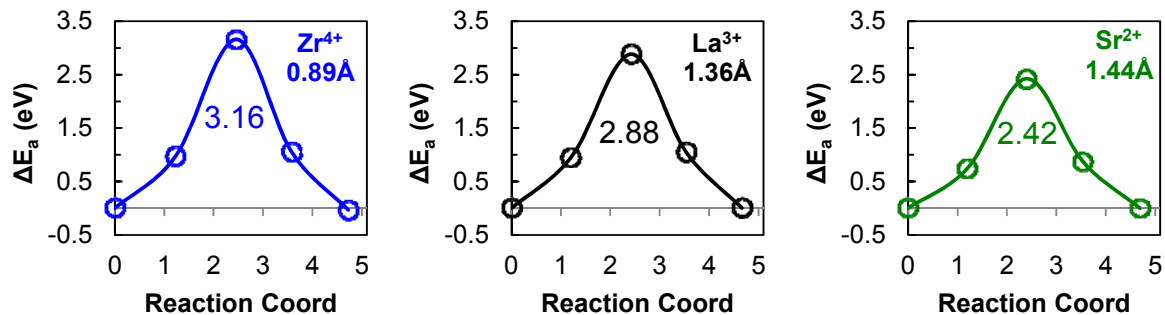
(a) Zr^{4+} hop of $(\text{Zr}^{4+} - \text{O}^{2-})_A$ (ionic charge)



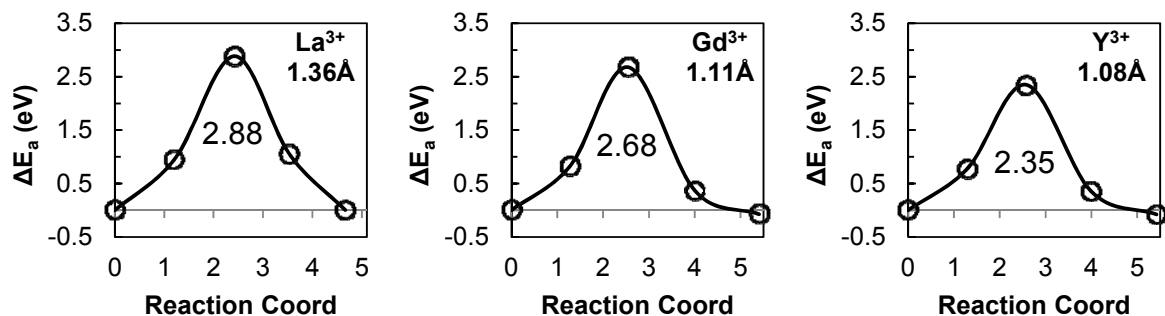
(b) La^{3+} hop of $(\text{La}^{3+} - \text{O}^{2-})_A$ (ionic radii)



(c) direct Zr^{4+} hop (ionic charge)



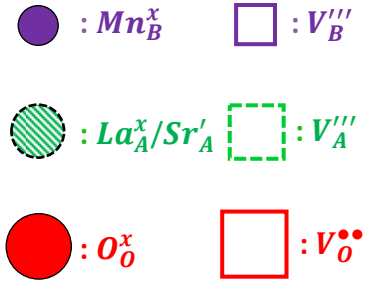
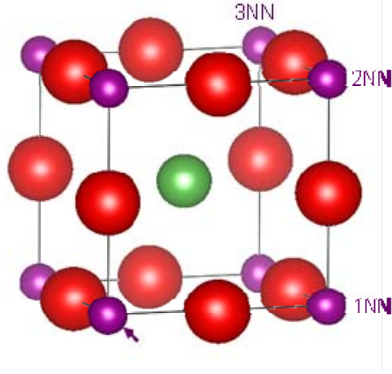
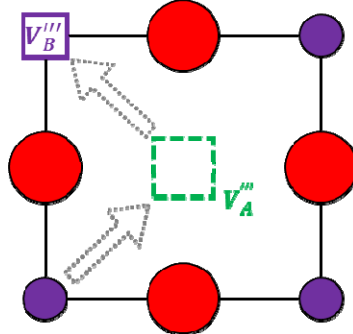
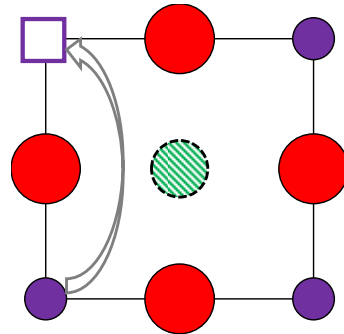
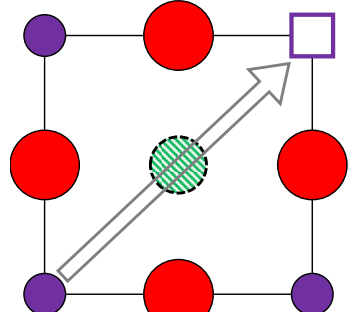
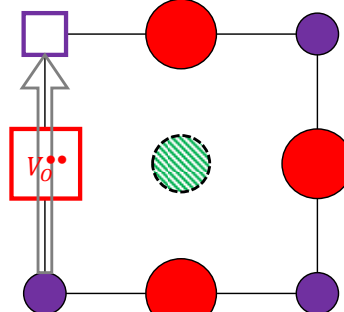
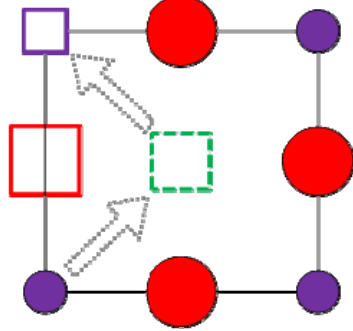
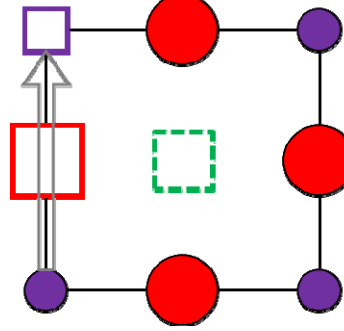
(d) direct La^{3+} hop (ionic radii)



(FIG. 6)

FIG. 6. The variations of the A-site cation migration barriers for the $(V_A''' - V_B''')_A$ pathway (FIG. 3(b)) versus (a) ionic charge and (b) ionic radii at a specific cation oxidation state of 3+, and for the $(V_A''')_A$ pathway (FIG. 3(a)) versus (c) ionic charge and (d) ionic radii at a formal charge state. The Shannon ionic radius of each cation as provided in Ref. [64] is indicated in the top right corner of each figure. The colors of blue, black, and green of the lines and fonts in the figures are used to represent the cation formal charge states of 4+, 3+, and 2+, respectively.

(a)

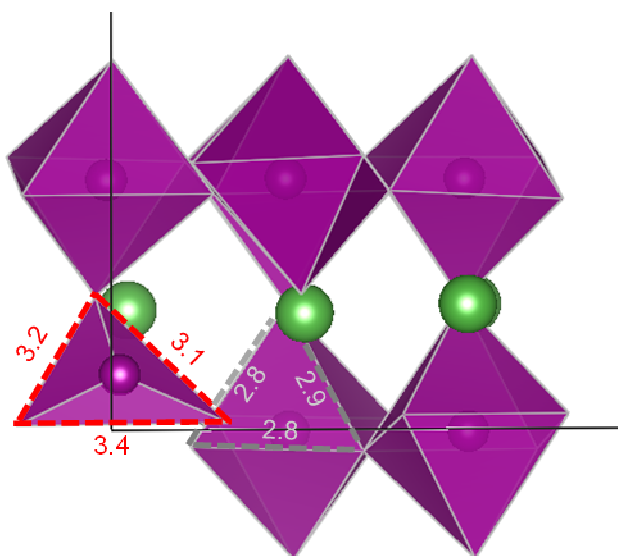
(b) Path 1 ($V_A''' - V_B'''$)_B(c) Path 2 (*curved* V_B''')_B(d) Path 3 (*diag* V_B''')_B(e) Path 4 ($V_O^{\bullet\bullet} - V_B'''$)_B(f) Path 5 ($V_A''' - V_B'''$ with $V_O^{\bullet\bullet}$)_B(g) Path 6 ($V_O^{\bullet\bullet} - V_B'''$ with V_A''')_B

(FIG. 7)

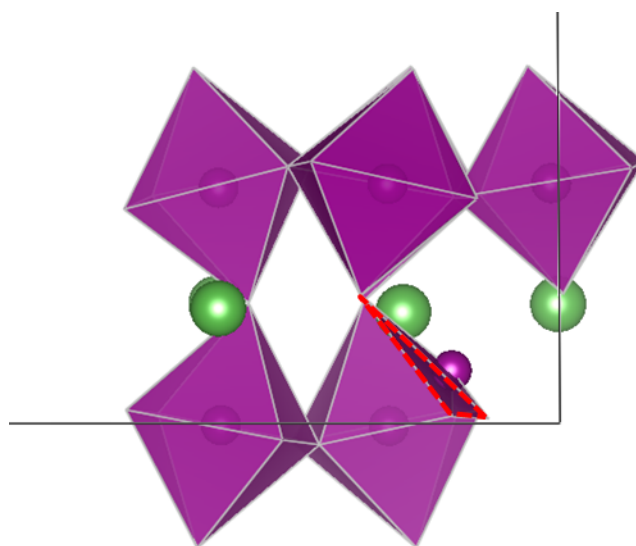
(Caption of FIG. 7)

FIG. 7. (a) A schematic (La,Sr)MnO₃ perovskite crystal created using the Vesta software[65]. The red, purple, and green spheres represent the oxygen, B-site, and the A-site cations whereas the empty squares in the corresponding colors are used to represent vacancies. These symbols are used in FIGs 7(b), (c), (d), (e), (f), and (g) to describe the six Mn migration pathways considered in this work, which are labeled as Path 1 ($V_A''' - V_B'''$)_B, Path 2 (*curved* V_B''')_B, Path 3 (*diag* V_B''')_B, Path 4 ($V_O^{\bullet\bullet} - V_B'''$), Path 5 ($V_A''' - V_B'''$ with $V_O^{\bullet\bullet}$)_B, and Path 6 Path 6 ($V_O^{\bullet\bullet} - V_B'''$ with V_A''')_B, respectively. The purple arrow indicates the Mn_B^x in the initial state before migration, whereas three types of symmetry distinct B-site are labeled as 1NN, 2NN, and 3NN in FIG. 7(a). It is noted that the green solid spheres and the green empty squares are drawn with dashed lines in FIGs 7(b)-(g), to indicate that the AO layer is located above or beneath the BO₂ plane in a top view projection along the $\langle 100 \rangle_{\text{perovskite}}$ direction. Dotted arrows are used in FIGs 7(b) and (f) to indicate an interlayer Mn migration between the AO and BO₂ planes.

(a) Front view



(b) Side view

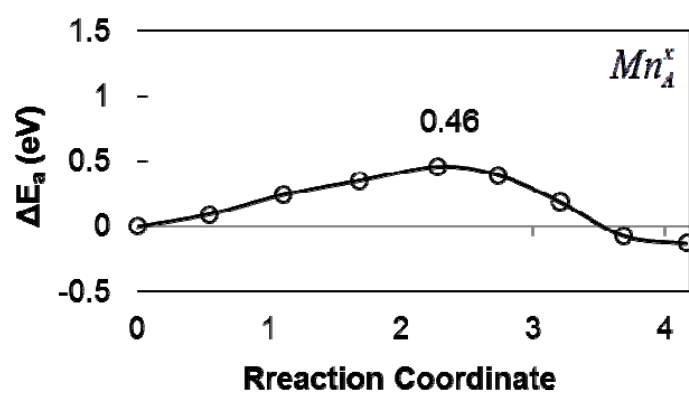


(FIG. 8)

(Caption of FIG. 8)

FIG. 8. (a) Front view and (b) side view of the saddle point image for the Mn migration pathway of $(V_A''' - V_B''')$ shown in FIG. 7(a). The red dashed lines highlight the O-O interstices of the trigonal planar Mn-O, with the red font numbers indicating the O-O distances. A typical O-O interstice and their O-O distances of the Mn-O octahedra are also provided in panel (a) indicated with grey dashed lines and grey font.

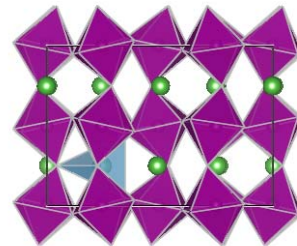
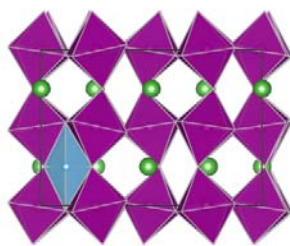
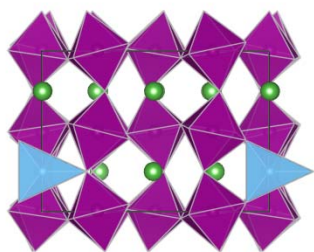
(a)



(b) Initial state

(c) Saddle point image

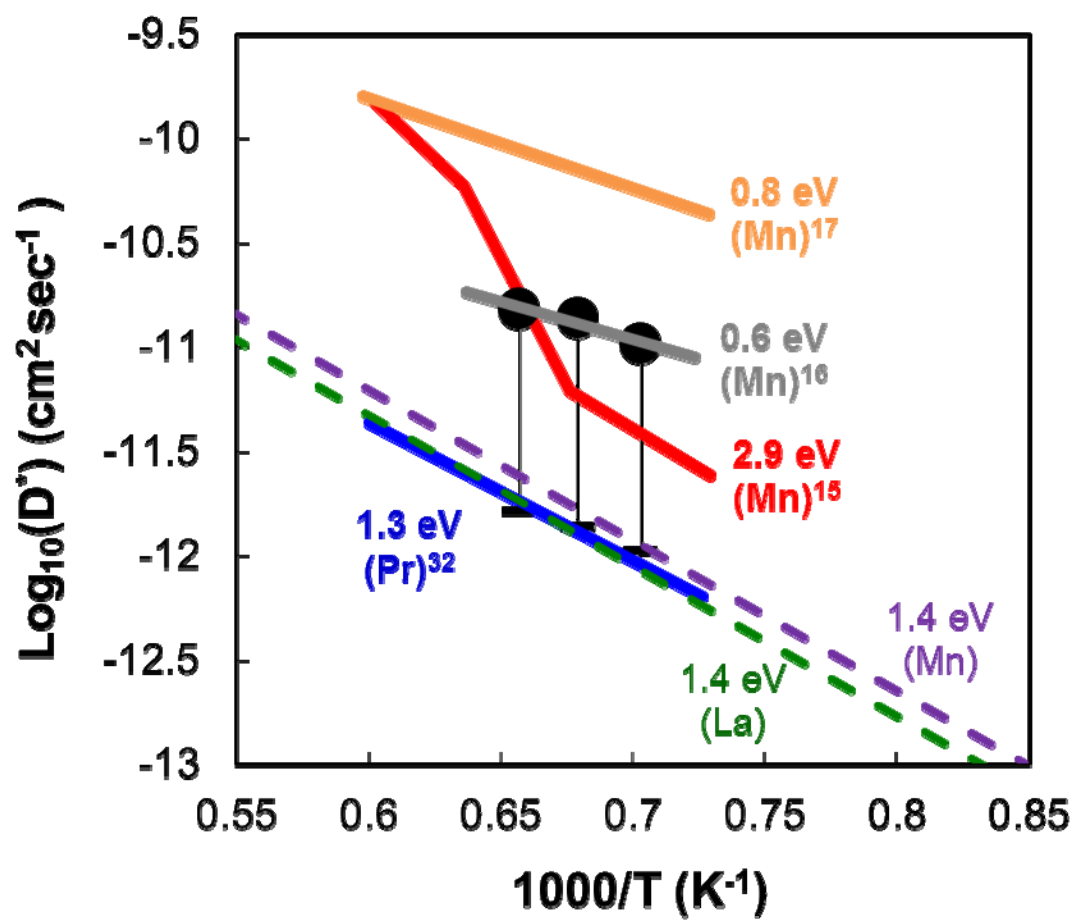
(d) Final state



(FIG. 9)

(Caption of FIG. 9)

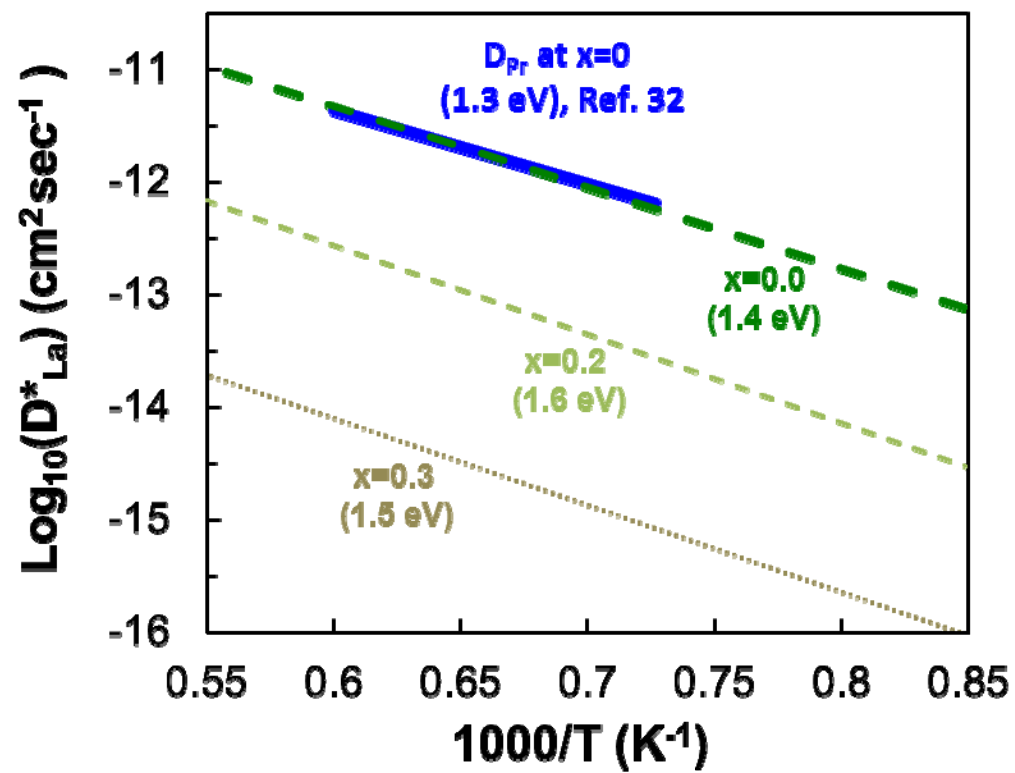
FIG. 9. (a) The potential energy profile of the Mn_A^x migration to the first nearest neighbor V_A''' , (b) the initial state configuration, (c) the saddle point image, and (d) the final state configuration. The Mn-O polyhedral of the migrating Mn cation is presented in the cyan color. The O-O distances of the square-planar Mn-O in the saddle point image are ~ 3.0 Å.



(FIG. 10)

(Caption of FIG. 10)

FIG. 10. Logarithm of the modeled cation tracer diffusion coefficients versus $1000/T$ for D_{La}^* (green dashed and dotted lines) and D_{Mn}^* (purple dashed and dotted lines) in bulk $\text{LaMnO}_{3\pm\delta}$. The data of the experimental Mn tracer/self-diffusion coefficients taken from Ref. [16] (black filled circles with error bars and the grey solid line), Ref. [15] (the red solid line), and Ref. [17], as well as the Pr impurity diffusion coefficients reported in Ref. [32] (the blue solid line) are included for comparison. We note that despite the same fitting parameters are used to calculate D_{Mn}^* , the slightly higher magnitude of the calculated D_{Mn}^* versus D_{La}^* reflects on their different hopping paths and distances (the active pathway of $Mn_B^x(V_A''' - V_B''')_B$ takes place via the second and third nearest neighbor B-sites versus the first nearest neighbor A-sites of the $La_A^x(V_A''' - V_B''')_A$ pathway, as shown FIG. 7(a) and 7(b) versus FIG. 3(b).



(FIG. 11)

FIG. 11. Logarithm of the model predicted D_{La}^* versus $1000/T$ for La (green lines) in bulk LSM at $x=0.0$ (thick green dashed lines), $x=0.2$ (thin light green dashed line), and $x=0.3$ (olive dotted line). The blue thick line corresponds to the experimental $\text{LaMnO}_{3\pm\delta}$ Pr impurity diffusion coefficient results adapted from Ref. [32]. The activation energies extracted from the slopes are also indicated in the figure.

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