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Conduction at a Ferroelectric Interface

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Typical logic elements utilizing the field effect rely on the change in carrier concentration due to the field in the channel region of the device. Ferroelectric field effect devices provide a non-volatile version of this effect due to the stable polarization order parameter in the ferroelectric. In this work, we describe an oxide/oxide ferroelectric heterostructure device based on (001)-oriented PbZr_{0.2}Ti_{0.8}O₃ (PZT)-LaNiO₃ where the dominant change in conductivity is a result of a significant mobility change in the interfacial channel region. The effect is confined to a few atomic layers at the interface, and is reversible by switching the ferroelectric polarization. More interestingly, in one polarization state the field effect induces a 1.7 eV shift of the interfacial bands to create a new conducting channel in the interfacial PbO layer of the ferroelectric.

Electronic devices based on the ferroelectric field effect are designed with two functional components, a ferroelectric gate and a conducting channel. The device operates via large changes in carrier density in the conducting channel, which is controlled by the ferroelectric polarization [1]. Here we describe a device where a single atomic layer in the ferroelectric itself serves as the conducting channel. Generally, ferroelectricity and metallicity are incompatible in the bulk because conduction electrons screen the bulk polarization [2], but it has been predicted that metallic states form at ferroelectric surfaces due to the large electric fields present at surfaces where the polarization terminates [3-6]. Here, we describe a device heterostructure where this mechanism operates at a PbZr_{0.2}Ti_{0.8}O₃ (PZT)-LaNiO₃ interface. When the polarization direction points away from the interface, the normally fully occupied PbO bands of the interfacial PZT cross the Fermi level to form a conducting channel. In this approach, the

properties of the channel material, LaNiO₃, are critical for the formation of the metallic state in the ferroelectric. In order to induce a ferroelectric interface that becomes metallic, the material adjacent to the ferroelectric must be sufficiently conductive to provide carriers that screen the polarization, but also sufficiently resistive to avoid shorting out conductivity in the ferroelectric. While LaNiO₃ is fully metallic in the bulk, ultra-thin films of LaNiO₃ can have low conductivity due to structural distortions [7], spin scattering, and scattering from boundaries [8].

Because of the focus on interfacial metallic states, their contribution to the electronic transport will be most pronounced for channels of ultra-thin films with atomically abrupt interfaces. To realize these structures, oxygen-plasma assisted molecular beam epitaxy is used to grow LaNiO₃ films on AlO₂-terminated (001)-oriented LaAlO₃ substrates, which are prepatterned with Hall bar devices. The substrate temperature is 590 °C during deposition at an oxygen partial pressure of ~5.4×10⁻⁶ Torr. Oscillations of the reflection high-energy electron diffraction (RHEED) specular spot intensity are monitored in situ to determine the film thickness. A 150 - 200 nm thick layer of PbZr_{0.2}T0i_{0.8}O₃ (PZT) is grown using off-axis RF magnetron sputtering at 520 °C, in 225 mTorr of Ar : O₂ (1 : 3 ratio). The PZT/LaNiO₃ structures are cooled to room temperature in the process gases, to avoid the formation of vacancies that may adversely affect the ferroelectric switching [9, 10]. TEM sample preparation is performed using a focused-ion beam (FIB) lift-out technique. After FIB milling, low energy (0.9 keV) Ar ion milling with a Nanomill (E. A. Fischione Instruments, Inc.) is used to remove FIB-induced sample damage. A JEOL ARM 200CF microscope equipped with a cold fieldemission electron gun and double spherical-aberration correctors (CEOS GmbH) is used for high-angle annular-dark-field (HAADF) scanning transmission electron microscopy (STEM) imaging. The collection angles are in the range of 68 to 280 mead. The first-principles

calculations are based on density functional theory (DFT) within the periodic supercell planewave pseudopotential approach, as implemented in the Quantum ESPRESSO software package [11]. The LaNiO₃-PZT interface is modeled as a slab containing four $c(2 \times 2)$ unit cells of LaNiO₃ in contact with 3.5 unit cells of PbTiO₃. To simulate the effect of the LaAlO₃ substrate, the in-plane lattice parameter of the slab is strained to the value corresponding to bulk LaAlO₃, computed within the same theoretical framework. Vanderbilt ultrasoft pseudopotentials are employed to describe atoms [12]. We have chosen to use the local-density approximation (LDA) with the Perdew-Zunger parameterization [13] to describe the exchange-correlation potential, since Gou et al. found that LDA was more appropriate to study LaNiO₃ compared to other functionals [14]. We use a 35 Ry plane-wave energy cut-off for the wavefunctions and a 280 Ry cut-off for the electron density. Each slab is separated from its periodic image by ~ 10 Å. The Brillouin zone is sampled by a regular $4 \times 4 \times 1$ mesh of k points. To simulate the accumulation and depletion states, the polarization state of PbTiO₃ is set by fixing the atomic positions of oneunit-thick layer of PbTiO₃ furthest from the interface to corresponding theoretical values of polarized bulk PbTiO₃ strained to LaAlO₃. Following the structural relaxation, we verify that the entire PbTiO₃ is in the desired polar state. To reduce the artificial polarization effects from the surface charges, the terminal PbO layer facing the vacuum is covered by two layers of Pt, which also serve as the electron reservoir (electrode) for the system. To check that there is no spurious effect from the electric field in the vacuum region, we applied the dipole correction technique [15], which we found to have negligible impact on the crystal structure and the electronic structure of the interface (Fig. S5). Structural relaxation of the two slabs modeling the accumulation and depletion states of the interface is performed until all Cartesian components of the forces on all atoms are 30 meV/Å in magnitude. In order to project the electronic band

structure onto the various structural components, we compute maximally localized Wannier functions [16, 17] using the Wannier90 software package [18]. The spatial locality of the Wannier functions then allows us to disentangle the bands of interest (with Ni or Pb character) from the Pt bands crossing the Fermi level, as the latter are not related to or of interest for the electronic structure of the PbTiO₃/LaNiO₃ interface.

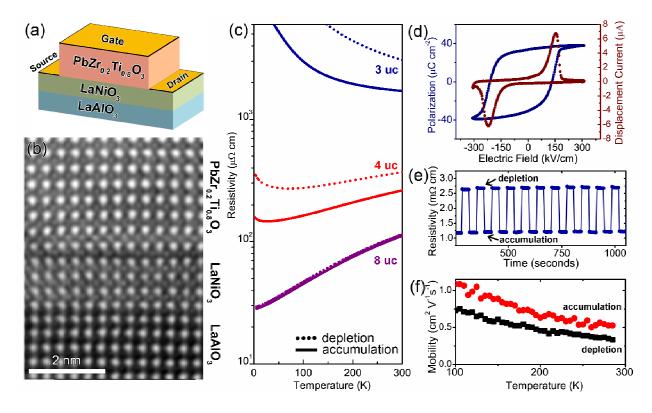


FIG. 1. Resistivity and switching behavior of PbZr_{0.2}Ti_{0.8}O₃/LaNiO₃ devices. (a) Schematic of the PZT/LaNiO₃ devices, shown with gold electrodes. (b) Cross-sectional transmission electron micrograph of a PZT/4 uc LaNiO₃ device. (c) Resistivity versus temperature for PZT/LaNiO₃ devices with LaNiO₃ thicknesses of 3 uc, 4 uc and 8 uc (solid and dotted lines correspond to accumulation and depletion of holes, respectively). (d) The polarization-electric field (P-E) loop obtained from a structure of 150 nm PZT/ 3 uc LaNiO₃. The remnant polarization is \approx 30 μ C/cm². In (e) the room-temperature resistivity of a 3 uc LaNiO₃ device is shown as a function

of time as the system is switched from the low resistance state (accumulation of holes) to the high resistance state (depletion of holes). (f) Polarization-dependent carrier mobility determined from Hall measurements for a PZT/4 uc LaNiO₃ device.

A schematic of the device structure is shown in Fig. 1(a). As seen from the transmission electron micrograph in Fig. 1(b), these device structures display atomically sharp interfaces. The PZT layer exhibits a well defined hysteresis in the polarization versus electric field (P-E) loop [Fig. 1(d)], measured using a positive-up negative-down (PUND) method [19]. Hall measurements indicate that transport in LaNiO₃ is hole-like, in agreement with previously reported measurements [7, 8]. The ferroelectric polarization thus depletes hole carriers from the PZT/LaNiO₃ interface when the polarization direction points towards the nickelate (depletion state), and accumulates hole carriers at the interface when the direction of polarization points away from the nickelate layer (accumulation state). This polarization couples to the electrical properties of the nickelates, as shown in the resistivity versus temperature plots for the PZT/LaNiO₃ devices [Fig. 1(c)], for which the thicknesses of the LaNiO₃ are 3 uc, 4 uc and 8 uc. The resistivity of the 8 uc LaNiO₃ film is bulk-like and metallic down to 2 K for both polarization states of PZT. The resistivity of the 4 uc thick film shows a distinct change in behavior at low temperatures. In the depletion state, the 4 uc thick film has a metal-insulator transition at ≈ 75 K. In contrast, the accumulation state of the 4 uc thick film is metallic down to ≈ 20 K. The 3 uc thick LaNiO₃ film is insulating at all temperatures, exhibiting a factor of two change in room temperature resistivity when switched from accumulation to depletion. Applying a train of 100 ms long voltage pulses at room temperature to switch the polarization of the ferroelectric reveals reversible and non-volatile switching of the LaNiO₃ resistivity [Fig. 1(e)].

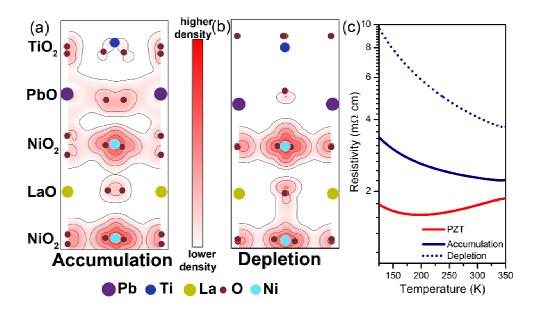


FIG. 2. Electronic structure of PTO/4 uc LaNiO₃ strained to the theoretical in-plane lattice constant of LaAlO₃. A 2D projection of the local density of electronic states derived from first-principles calculations integrated within \pm k_BT eV of the Fermi level (T = 300 K) at the interface of PbTiO₃ and LaNiO₃ for (a) the accumulation state and (b) the depletion state. The red contours indicate a higher density of states, and the white areas indicate a lower density of states. (c) Temperature dependent resistivity measurements for devices with 3 uc-thick LaNiO₃ in the accumulation (solid blue) and depletion states (dashed blue). The resistivity, normalized to 1 uc of interfacial PZT, is also shown (red). A zoomed-out version is shown in Fig. S1.

To elucidate the origin of the polarization-dependent changes in resistivity, we measure the carrier concentration of the channel for both polarization directions on a device with a 4 uc LaNiO₃ channel. Hall measurements show that conduction is dominated by majority hole carriers, with a carrier concentration of $\approx 5 \times 10^{22}$ cm⁻³ at 285 K. This value corresponds to 3 holes/uc, in agreement with band theory and measurements of thin films of LaNiO₃ [20-23].

From the value of the remnant polarization of the PZT ($25 \,\mu\text{C/cm}^2$), we expect the change in carrier concentration for a 4 uc thick LaNiO₃ device to be $\approx 2\%$ if we assume that most charge is screened within one interfacial unit cell of the nickelate. This value of 2% is much smaller than the measured change in conductivity of 30% for a 4 uc thick LaNiO₃ device (Fig. 1(c)), and thus one finds that the change in mobility is about 30%, as shown in Fig. 1(f). A modulation of mobility is unexpected and distinct from the modulation of conductivity for semiconductor devices, which rely on changes in the carrier concentration to modify the conductivity [9, 24-26]. This result is also distinct from those obtained using electrolytically gated NdNiO₃ thin films, where the mobility is unchanged when a large polarization is applied[21]. Hence, we expect that the details of the physical and electronic structure at the interface play a key role, where changing the PZT polarization distorts the interfacial structure, in addition to changing the carrier concentration [27].

To predict changes in the physical and electronic structure, we turn to first-principles calculations and compute the local electron density for the ground state structures of each polarization state [Figs. 2(a) and 2(b)]. In the accumulation state, there is significant density in the PbO layer of the PbTiO₃ closest to the interface, which is notably absent in the depletion state. We understand the presence of states at the Fermi level in the PbO layer by examining the band structures shown in Fig. 3(a) (accumulation) and Fig. 3(b) (depletion). For the accumulation state [Fig. 3(a)], we observe bands with strong Pb character at the Fermi level, in which Pb 6s states hybridize with O 2p states. In the depletion state [Fig. 3(b)], these Pb-related states are absent close to the Fermi level, showing that the bands crossing the Fermi level have no Pb character and arise exclusively from Ni and O. Similarly, the layer-resolved LDOS is plotted in accumulation [Fig. 3(c)] and depletion [Fig. 3(d)], where it is evident that significant

LDOS are present in the interfacial layer of PbTiO₃ at the interface in accumulation, but not in depletion. The origin of PbO character in bands that cross the Fermi level is two-fold. First, the electric field due to the ferroelectric field effect shifts the PbO bands upwards to cross the Fermi level in the accumulation state by about 1.7 V, as predicted to occur at vacuum-PbTiO₃ surfaces for the same polarization direction¹⁸. The magnitude of the shift is also consistent with the magnitude of the ferroelectric polarization. Second, the change in apical oxygen bond length in the top-most nickelate layer facilitates hybridization between Ni and Pb. As the apical oxygen moves further away from the NiO₂ layer in the depletion state, hybridization between Pb states with those of Ni and O is suppressed. Density functional theory predicts the appearance of an additional channel for conduction in the PbO layer of the ferroelectric. We estimate an upper bound for the resistivity of this layer by taking the difference in conductance in accumulation and depletion [Fig. 2(c)]. Strikingly, even though the film as a whole has insulating character, the additional conductivity of the channel has a metallic temperature dependence. The role of NiO₆ and TiO₆ octahedral rotations may also be tested by calculating the layer-resolved LDOS using a 1×1 supercell, which suppresses all octahedral tilts and rotations, as shown in Fig. S2. This indicates that the appearance of a conductive PbO state at the interface in the accumulation state is not directly related to octahedral rotations.

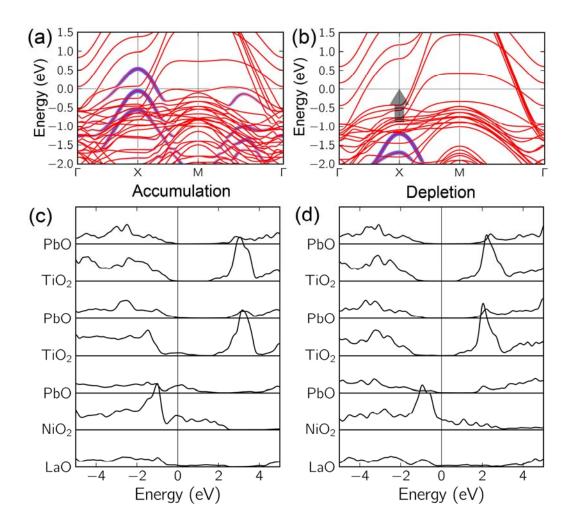


FIG. 3. Band structure of PTO/ LaNiO₃ strained to the theoretical in-plane lattice constant of LaAlO₃. Band structure for (a) accumulation and (b) depletion, where the zero of energy is the Fermi level in each case and a (1 × 1) interfacial unit cell is employed. Red-colored bands correspond to dominant LaNiO₃ character, while blue-colored bands indicate strong contributions from the interfacial PbO layer. The top of the PbO-dominated bands shift from about -1.2 eV in depletion to approximately 0.5 eV in accumulation. (c) The layer-resolved LDOS at the interface for accumulation, and (d) depletion. The PbTiO₃ is insulating in depletion, and is insulating in accumulation away from the interface, which has LDOS at the Fermi level.

While these theoretical calculations are theoretically self-consistent, they also explain the experimentally measured changes in conductivity. To test the robustness of the calculations, we calculated a structure in which the LaNiO₃ is 3 uc thick (Fig. S4), performed an LDA+U calculation where U = 3 eV on the Ni d site (Fig. S3), and applied a dipole correction to ensure zero electric field in the vacuum region (Fig. S5) [28]. All of these calculations are in agreement with the results presented in Fig. 3, reinforcing the robustness of the DFT results. These results show that the ferroelectric polarization induces a robust metallic state in the ferroelectric at the interface. This state forms by electrostatically shifting the valence bands of PZT upward to cross the Fermi level of the LaNiO₃ channel. In addition, the ferroelectric polarization strongly modifies the bond lengths involving Ni, O, and Pb across the interface, which in turn hybridizes the Ni, O, and Pb states to facilitate charge redistribution into the PZT layer. What results is a change in carrier mobility, as carriers redistribute into the higher mobility channel in PZT. The mobility of the PbO layer may be higher than that of LaNiO₃ due to a smaller effective mass [29] or due to reduced scattering. In particular, PbTiO₃ is likely less susceptible to hole carrier scattering with spins, which is expected to contribute to the resistivity of LaNiO₃ due to the d⁷ electron configuration of the Ni sites_[8]. Such metallic states in ferroelectrics have been recently predicted using first principles density functional theory [6, 30, 31]. These works focus on conduction at surfaces, rather than at interfaces [6]. Such surface states on ferroelectrics can be challenging to realize experimentally due to surface reconstructions and screening by adsorbates. While interface structure can influence the polarization [32, 33], the ferroelectric does not undergo such a reconstruction at an interface [34, 35].

The mechanism for interfacial conductivity in a ferroelectric is general and raises possibilities for engineering buried interfaces. For instance, the layer of PbO at the interface can be replaced with a single atomic layer of another material with enhanced conductive, ferroelectric, or magnetic properties. Moreover, the use of a ferroelectric interface enables dynamic reversible control via switching of the polarization. This effect may be useful in realizing novel ferroelectric field effect devices that function in a mechanistically different way than existing technology.

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