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Properties of donor qubits in ZnO formed by indium-ion implantation

Xingyi Wang,^{1,*} Christian Zimmermann,^{2,*} Michael Titze,³ Vasileios Niaouris,² Ethan R. Hansen,² Samuel H. D'Ambrosia,² Lasse Vines,⁴ Edward S. Bielejec,³ and Kai-Mei C. Fu^{2,1}

¹*Department of Electrical Engineering, University of Washington, Seattle, Washington 98195, USA*

²*Department of Physics, University of Washington, Seattle, Washington 98195, USA*

³*Sandia National Laboratories, Albuquerque, New Mexico 87123, United States*

⁴*Department of Physics/Centre for Materials Science and Nanotechnology,*

University of Oslo, Blindern, Oslo N-0316, Norway

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Shallow neutral donors (D^0) in ZnO have emerged as a promising candidate for solid-state spin qubits. Here, we report on the formation of D^0 in ZnO via implantation of In and subsequent annealing. The implanted In donors exhibit optical and spin properties on par with *in situ* doped donors. The inhomogeneous linewidth of the donor-bound exciton transition is less than 10 GHz, comparable to the optical linewidth of *in situ* In. Longitudinal spin relaxation times (T_1) exceed reported values for *in situ* Ga donors, indicating that residual In implantation damage does not degrade T_1 . Two laser Raman spectroscopy on the donor spin reveals the hyperfine interaction of the donor electron with the spin-9/2 In nuclei. This work is an important step toward the deterministic formation of In donor qubits in ZnO with optical access to a long-lived nuclear spin memory.

I. INTRODUCTION

Neutral shallow donors (D^0) in semiconductors have shown potential as solid-state spin qubits for use in quantum technologies, such as quantum computing and quantum communication [1–4]. In direct band-gap semiconductors, the bound electron spin states of shallow donors forming the qubit states can be optically accessed via the donor-bound exciton (D^0X) with high radiative efficiency [5, 6]. The direct band-gap semiconductor ZnO is an emerging platform for D^0 qubits, with D typically consisting of Al, Ga, or In substituting on a Zn site, denoted as Al_{Zn} , Ga_{Zn} , or In_{Zn} , respectively. For these donor qubits, narrow optical D^0X linewidths, efficient radiative transitions, optical state initialization, long longitudinal spin relaxation times ($T_1 > 400$ ms) and moderate coherence times ($T_2 \approx 50$ ms) have been demonstrated [7–9].

One feature of qubits based on impurities is that impurities can be incorporated by ion implantation and subsequent annealing [10–13]. Using ion implantation, donor density and depth can be controlled. Thus, one can either introduce high densities of donors for quantum memory and transduction applications [14, 15] or low densities of individually addressable donor qubits for quantum computing and networks [1, 2, 16]. Using focused ion beam technology, one can also control the lateral positioning of the donor impurities [17, 18], enabling the deterministic placement of single donor qubits after fabrication of photonic devices [19]. Moreover, for single site defects, such as substitutional donors, near-deterministic incorporation is possible [13].

Here, we report on the optical and spin properties of In_{Zn}^0 in ZnO formed at a depth of 200 nm through ion implantation and subsequent annealing. We focus on In_{Zn}^0 because

of the following favorable features: large binding energy (≈ 63.2 meV [20]), strong hyperfine interaction with the In nucleus [21, 22] for access to a nuclear spin quantum memory [23], and the availability of ZnO substrates with low residual In doping. Ion implantation at relatively large fluences has previously been employed to yield impurity-related shallow donors in ZnO [24–28]. Here we focus on low implantation fluences and the resulting donor properties relevant to quantum information applications. We demonstrate that implanted In_{Zn}^0 exhibit D^0X inhomogeneous optical transition linewidths less than 10 GHz, comparable to the narrowest linewidths observed for in-grown In_{Zn}^0 . The narrow linewidths owing to low strain and small spectral diffusion from charge traps indicate low implantation damage, which is consistent with the reported resilience of ZnO to radiation damage [29, 30]. Favorable spin properties are also demonstrated, with measured longitudinal T_1 times in the hundreds of ms, approximately four times longer than the T_1 times observed for in-grown Ga_{Zn}^0 donors [7]. Further, two laser Raman spectroscopy on implantation-doped In_{Zn}^0 demonstrates that we can begin to resolve the large hyperfine interaction between the bound electron and the In nucleus, pointing to the potential for an optical interface to a long-lived nuclear spin memory.

II. SAMPLE PREPARATION

A hydrothermally-grown ZnO single crystal substrate (Tokyo Denpa, 5 mm \times 5 mm \times 0.3 mm) with a surface orientation of (0001) is utilized as the implantation substrate [31]. In the remainder of the article, the [0001] direction of the crystal is referred to as the \vec{c} axis. Ion implantation is performed using the Sandia Ion Beam Laboratory 6 MV Tandem accelerator. In is extracted as a negative ion utilizing a pressed cathode filled with In wire. The landing energy of In^+ ions is 800 keV, leading to an implant depth of approximately 200 nm determined by simulating

* The authors contribute equally to this project.

Corresponding author: xingyiw@uw.edu

the implantation process using the Stopping and Range of Ions in Matter software [32] (Fig. 1). The ions are focused with a magnetic quadrupole lens, giving a beam spot of $780 \times 870 \mu\text{m}^2$. The spot size is measured using a luminescent phosphor and imaged using a home-made camera setup. The imaging setup utilizes a 10 mm hole in the center of its final imaging mirror, allowing concentric imaging of the beam. The focused ion beam allows us to vary the ion implantation fluence within a single sample. The nominal implantation fluence ranges from 10^8 to 10^{15} ions/ cm^2 . Post-implantation annealing at 700 Celsius in oxygen for an hour is used to recover implantation damages.

Secondary ion mass spectrometry (SIMS) is performed to characterize the In implantation profile and to determine the background concentrations of Al and Ga, prominent donors present in the substrate [20, 33, 34]. A Cameca IMS 7f secondary ion mass spectrometer equipped with a 15 keV O_2 primary ion beam source is used to record the concentration vs. depth profiles of In, Al and Ga. Absolute concentration values of In are obtained by measuring ion implanted reference samples, ensuring less than 10 % error in accuracy. For depth calibration, the sputtered crater depths are determined by a Dektak 8 stylus profilometer and a constant erosion rate is assumed.

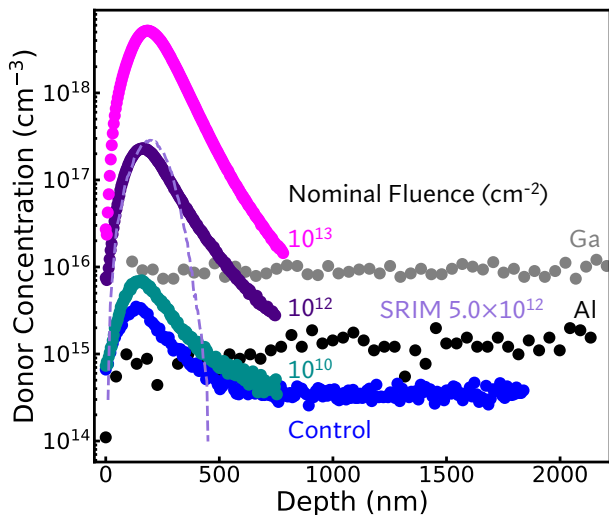


FIG. 1. SIMS data collected from the central $62 \mu\text{m}$ of a crater size of $200 \mu\text{m}$: The measured (nominal) In implantation fluences are 1.1×10^{14} (10^{13}) cm^{-2} , 5.0×10^{12} (10^{12}) cm^{-2} , 1.7×10^{11} (10^{10}) cm^{-2} , 1.3×10^{11} (Control) cm^{-2} . The peak of In concentration from SRIM simulated In implantation profile matches well with that of the measured implantation profile.

As shown in Fig. 1, the measured peak implantation depth is consistent with simulation. However the measured implantation fluence ranges from 5 to over 10 times the nominal fluence. Moreover a fluence of 10^{11}cm^{-2} is measured in a nominally unimplanted control region. The discrepancy in the nominal and measured implantation fluences is attributed to overspray from the very high fluence implantation areas. Despite the higher-than-intended fluences, as we show below, the optical and spin properties of implanted In donors appear promising for quantum information appli-

cations. Throughout this work we refer to the implantation regions in terms of the nominal implantation fluence. Finally, a background concentration of $9.2 \times 10^{15} \text{cm}^{-3}$ and $1.2 \times 10^{15} \text{cm}^{-3}$ is measured for Ga and Al respectively.

III. RESULTS AND DISCUSSION

The properties of the implanted In donors are characterized via low-temperature photoluminescence (PL) and PL excitation (PLE) spectroscopy, spin relaxation and two laser coherent population trapping measurements.

A. Photoluminescence Spectroscopy

The optical signature of donor incorporation in a semiconductor is the corresponding D^0X luminescence transition. Fig. 2 (a) shows a comparison of the normalized PL spectra from an as-grown ZnO single crystal and on a single crystal after In implantation and subsequent annealing. Prior to In implantation, a weak signal attributed to the $\text{In}_{\text{Zn}}^0\text{X}$ [20] line can be observed. The corresponding feature is about three orders of magnitude weaker than the PL features attributed to $\text{Ga}_{\text{Zn}}^0\text{X}$ and $\text{Al}_{\text{Zn}}^0\text{X}$ [20], indicating that In_{Zn}^0 is present in concentrations on the order of 10^{13}cm^{-3} . After In implantation, a dramatic increase in the $\text{In}_{\text{Zn}}^0\text{X}$ line relative to the $\text{Ga}_{\text{Zn}}^0\text{X}$ and $\text{Al}_{\text{Zn}}^0\text{X}$ lines is observed. The $\text{In}_{\text{Zn}}^0\text{X}$ linewidth is spectrometer resolution limited up to a fluence of 10^{11}cm^{-2} . The complete fluence-dependent spectra are included in the Supplemental Material.

In addition to the prominent $\text{In}_{\text{Zn}}^0\text{X}$ feature, a few additional new features can be observed after implantation and annealing. A sharp line at 3.3673eV is labelled I^+ (see Fig. 2 (a)). This feature is close to a PL feature attributed to excitons bound to ionized In_{Zn} [35]. Magneto-PL measurements on this sample confirm that the I^+ is related to an exciton bound to either an ionized donor or acceptor (Supplemental Material) and we attribute the I^+ line to $\text{In}_{\text{Zn}}^+\text{X}$. Additionally, a low-energy shoulder on the $\text{Al}_{\text{Zn}}^0\text{X}$ line can be observed, indicating additional donor formation of unknown origin (Supplemental Material). Finally the prominent Y_0 exciton line, which is thought to arise from excitons bound to structural defects [20], can be seen in the sample both before and after In implantation.

Curiously, the absolute PL intensity for $\text{In}_{\text{Zn}}^0\text{X}$ remains approximately constant with implantation fluence (Fig. 3(a)), whereas the PL intensity of the $\text{Al}_{\text{Zn}}^0\text{X}$, $\text{Ga}_{\text{Zn}}^0\text{X}$, and Y_0 decrease with increasing In implantation fluence. These observed changes in the integrated PL intensity indicate that the entire volume of material probed with near-band gap excitation ($\lambda_{\text{exc}} = 360 \text{nm}$) is affected by the In implantation. This does not necessarily mean the probing depth is only the 200nm depth of implanted In ions, because intrinsic defects created during implantation could diffuse deeper into the material during annealing [36–38].

While the absolute $\text{In}_{\text{Zn}}^0\text{X}$ remains constant, the ratio of the integrated PL intensity of $\text{In}_{\text{Zn}}^0\text{X}$ and $\text{Ga}_{\text{Zn}}^0\text{X}$, denoted as R_{InGa} , increases with fluence, as shown in Fig. 3(b). R_{InGa}

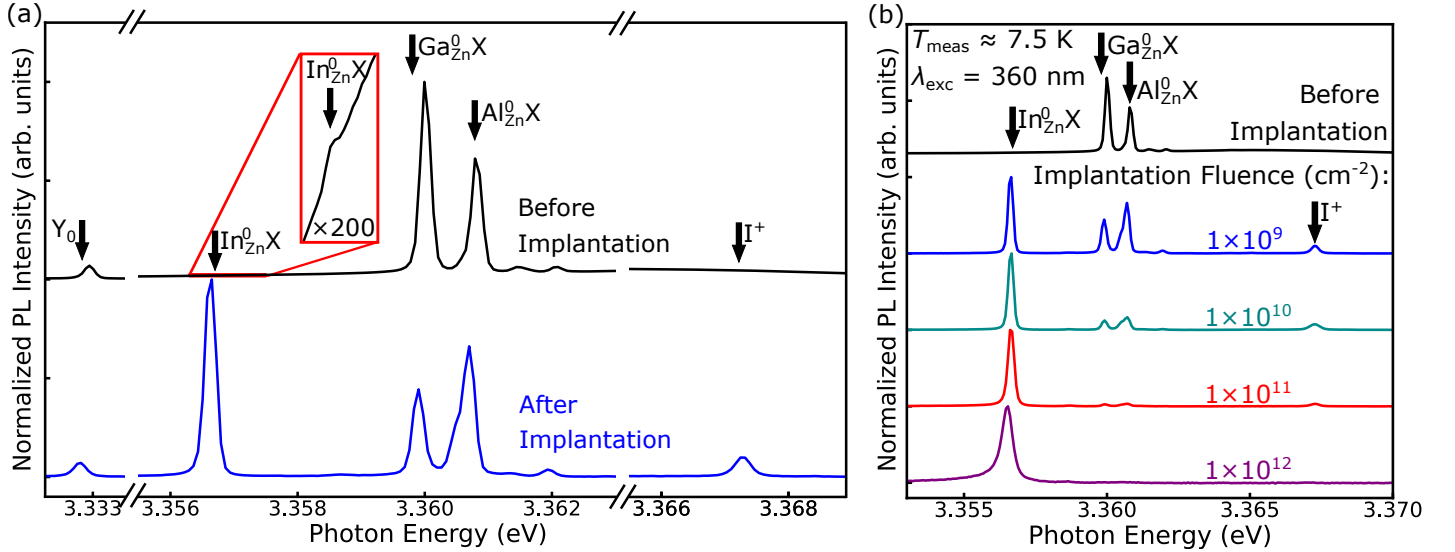


FIG. 2. (a) Comparison of normalized PL spectra of an as-grown ZnO single crystal, and for a single crystal after In implantation and subsequent annealing. (b) PL spectra normalized to the highest intensity peak for different implantation fluences. $T = 7.5$ K, $\lambda_{\text{exc}} = 360$ nm, $I_{\text{exc}} = 800$ nW/ μm^2 .

could not be tracked for fluences higher than 10^{12} cm^{-2} because the $\text{Ga}_{\text{Zn}}^0\text{X}$ line cannot be resolved at these high fluences. The constant $\text{In}_{\text{Zn}}^0\text{X}$ PL intensity coupled with the increase in R_{InGa} with fluence suggests an implantation-induced decrease in the bound exciton excitation efficiency and/or decrease in radiative efficiency for all donors in the excitation volume. Resonant photoluminescence excitation spectroscopy, described further below, supports the hypothesis that it is the off-resonant excitation efficiency and not the radiative efficiency that is primarily affected with implantation fluence.

B. Photoluminescence Excitation Spectroscopy

In photoluminescence excitation (PLE) spectroscopy, a narrow band laser is scanned over the dominant transition, corresponding to relaxation from $\text{In}_{\text{Zn}}^0\text{X}$ to the 1s donor state of In_{Zn}^0 , while two-electron satellites (TES, corresponding to relaxation to donor 2s/2p states, see inset of Fig. 4(b)) and phonon replica transitions are detected [9]. Resonant excitation spectra of the two-electron satellites and phonon replica are shown in the Supplemental Material. Fig. 4(a) shows the PLE spectra for an as-grown ZnO single crystal and for three different In implantation fluences. The ability to perform resonant excitation of the $\text{In}_{\text{Zn}}^0\text{X}$ transition (see Fig. 2 (b)) shows that an appreciable population of In_{Zn} exists in the desired neutral charge state.

Fig. 4(b) displays the full width at half maximum (FWHM) extracted from PLE and PL spectra for all implantation fluences. For implantation fluences lower than 10^{10} cm^{-2} , the linewidth of implanted $\text{In}_{\text{Zn}}^0\text{X}$ is comparable to that of in-grown $\text{In}_{\text{Zn}}^0\text{X}$. For larger fluences, the linewidth of implanted $\text{In}_{\text{Zn}}^0\text{X}$ ensembles increases with increasing fluence, indicating that residual lattice damage contributes sig-

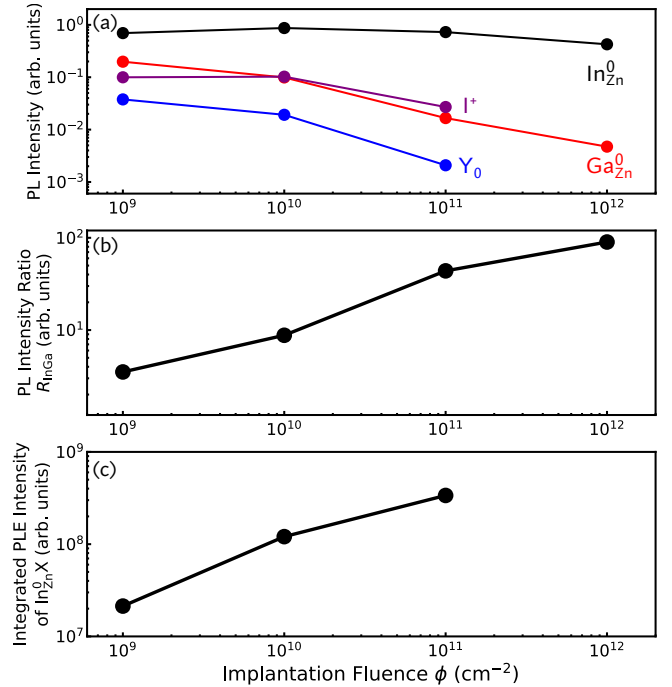


FIG. 3. (a) PL intensity on In implantation fluence for transitions labelled in Fig. 2(a). (b) Dependence of the ratio of the integrated PL intensity for $\text{In}_{\text{Zn}}^0\text{X}$ to $\text{Ga}_{\text{Zn}}^0\text{X}$, denoted R_{InGa} , on In implantation fluence. (c) Integrated PLE intensity of $\text{In}_{\text{Zn}}^0\text{X}$. $T = 7.5$ K, $\lambda_{\text{exc}} = 360$ nm (for PL), $I_{\text{exc}} = 800$ nW/ μm^2 .

nificantly to the inhomogeneous broadening. In contrast to PL measurements with 360 nm excitation, under resonant excitation we observe an increase in the $\text{In}_{\text{Zn}}^0\text{X}$ PLE-intensity with implantation fluence Fig. 3 (c). This result indicates that the constant PL intensity with fluence ob-

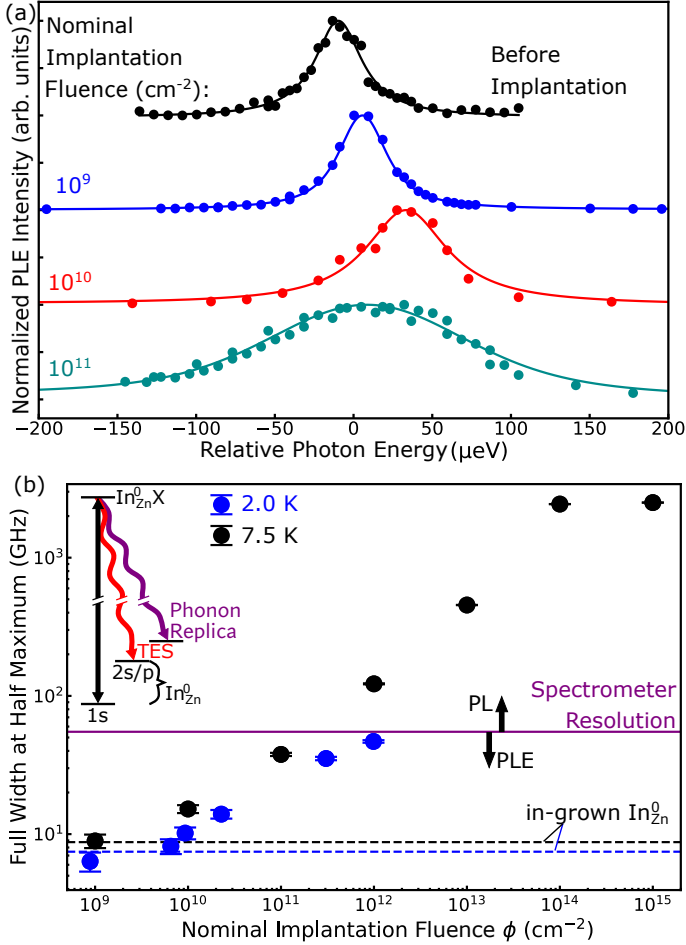


FIG. 4. (a) PLE spectra of $\text{In}_{\text{Zn}}^0\text{X}$ for in-grown and implanted In_{Zn}^0 . FWHM of each spectrum is determined by fitting to a Voigt profile. (b) Dependence of $\text{In}_{\text{Zn}}^0\text{X}$ FWHM on In implantation fluence. The implanted fluence is estimated from R_{InGa} for the data at 2.0 K (blue dots). Dashed lines indicate FWHM of in-grown $\text{In}_{\text{Zn}}^0\text{X}$ at 2.0 K and 7.5 K performed on a ZnO single crystal with a similar concentration of In_{Zn}^0 as the pre-implanted sample.

served in Fig. 3(a) is at least in part due to reduced excitation efficiency of D^0X . We also observe a linear relationship between PLE intensity with the PL ratio R_{InGa} at low excitation fluence (Supplemental Material). We thus utilize R_{InGa} as a proxy for fluence in the tails of the implantation regions for finer fluence sampling (blue data in Fig. 4(b)).

C. Longitudinal Spin Relaxation

For in-grown Ga_{Zn}^0 , we have previously shown that the dominant mechanism for spin relaxation for the donor bound spin-1/2 electron is due to spin-orbit coupling and the piezo-phonon interaction [7]. Here, we perform similar longitudinal spin relaxation measurements for implanted In_{Zn}^0 . Fig. 13 shows the dependence of T_1 on B in the Faraday geometry at 1.9 K for in-grown Ga_{Zn}^0 and implanted In_{Zn}^0 .

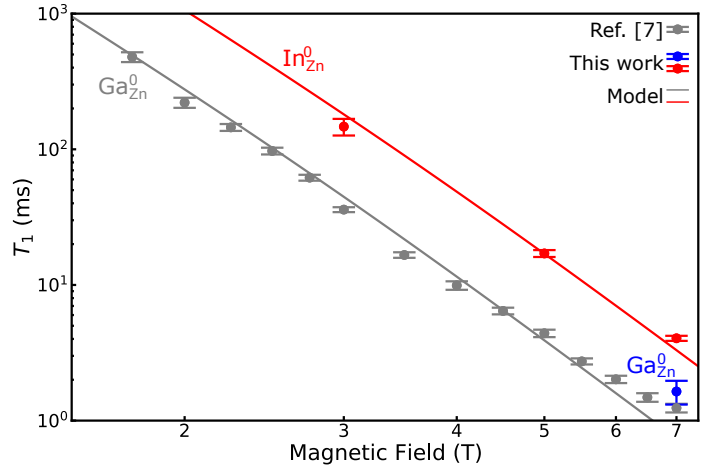


FIG. 5. Dependence of T_1 on the applied magnetic field. Red: Implanted In, fluence 10^9 cm^{-2} . Blue: In-grown Ga. Grey: In-grown Ga from a similar ZnO crystal, published in Ref. [7]. Population is optically initialized into the $|\uparrow\rangle$ state. Relaxation to the thermal equilibrium is probed optically (Supplemental Material). Faraday geometry ($\vec{B} \parallel \vec{c}$), $T = 1.5 \text{ K}$ (for [7]), 1.9 K (this work).

The dependence of T_1 on B can be described by

$$T_1 = (\Gamma_{\downarrow\uparrow} + \Gamma_{\uparrow\downarrow})^{-1} = \frac{1}{\Gamma_{\downarrow\uparrow}} \frac{\exp(\gamma) - 1}{\exp(\gamma) + 1},$$

with $\Gamma_{\downarrow\uparrow} = aB^5$, the relaxation rate from $|\uparrow\rangle$ to $|\downarrow\rangle$, and $\gamma = g_e \mu_B B / k_B T$ [7]. Here, g_e is the electron g -factor, μ_B is the Bohr magneton and T is the temperature. The relaxation rate pre-factor a was found to be $0.08 \text{ s}^{-1} \text{ T}^{-5}$ derived from the effective-mass theory [7]. For In_{Zn}^0 , the same dependence on B is observed, however with an $\sim \times 4$ smaller pre-factor a . This result indicates the longitudinal spin relaxation mechanism is identical for both types of donors, with no degradation observed for In due to residual implantation damage. The difference in pre-factor is expected from the dependence of both the spin-orbit interaction and piezo-phonon coupling on the effective mass wavefunction. A small dependence of T_1 on implantation fluence is also observed (Supplemental Material), which is consistent with the dependence of T_1 on donor density observed in Ga [7].

D. Two-Laser Spectroscopy and Coherent Population Trapping (CPT)

Two-laser spectroscopy can be further utilized to probe the spin properties of In_{Zn}^0 . Fig. 6(a) shows the results of resonant one- and two-laser spectroscopy performed at 7 T (Voigt geometry, $\vec{B} \perp \vec{c}$) and 2 K for an nominal implantation fluence of 10^9 cm^{-2} . The PL dependence on B and a discussion of the g -factors can be found in the Supplemental Material. When one laser (denoted as scanning S) is scanned across the $\text{In}_{\text{Zn}}^0\text{X}$ -related transitions, four transitions can be resolved, corresponding to transitions between the two D^0 electron spin states and two D^0X hole spin states (Fig. 6(a)).

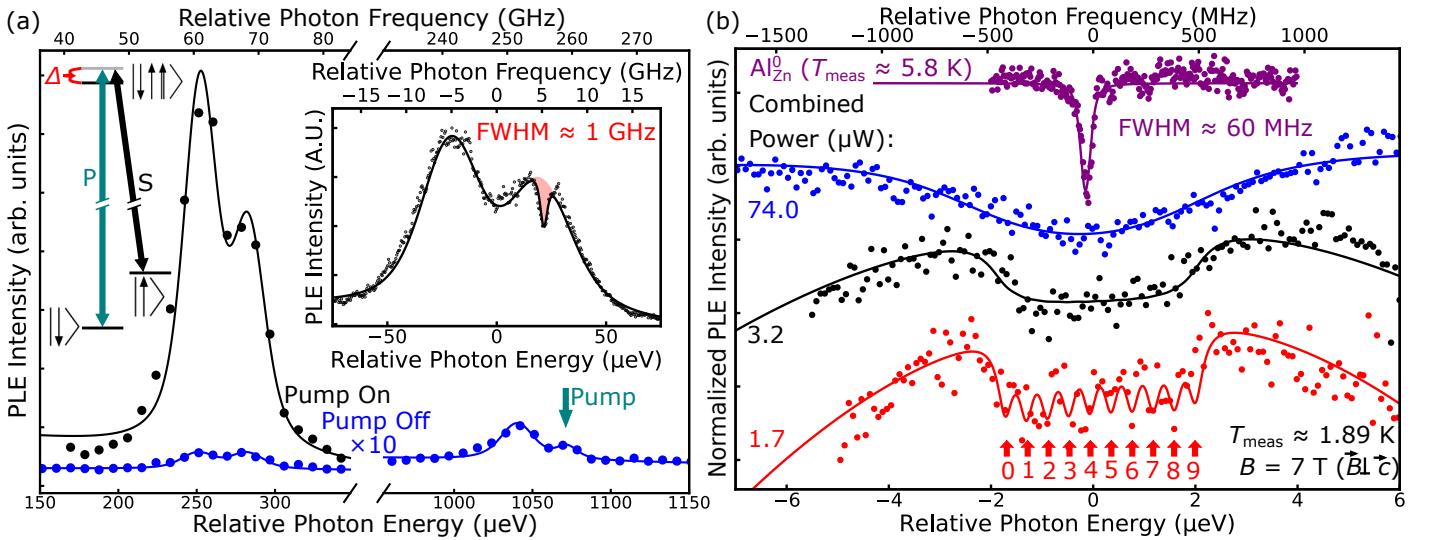


FIG. 6. (a) Resonant one- and two-laser spectroscopy on implanted (10^9 cm^{-2}) In_{Zn}^0 . For the one-laser measurement (blue), a tunable laser is scanned across all four transitions. For the two-laser measurement (see inset on the left for energy diagram where the dashed gray level denotes the detuning of both lasers from state $|\downarrow\uparrow\rangle$), the pump laser (P) is vertically polarized and resonant with the $|\downarrow\rangle$ to $|\downarrow\uparrow\rangle$ transition, while the scanning laser (S) is horizontally polarized and tuned across the two transitions involving the $|\uparrow\rangle$ state. A high-resolution scan of the two-laser experiment is depicted in the right inset in which a CPT dip is observed. (b) High-resolution PLE spectra showing CPT for different combined powers of the two lasers. For a constant wavelength of the pump laser, this leads to ten different resonance conditions depending on nuclear spin m_I . The data are fitted to the sum of ten equally-spaced Lorentzian profiles (splitting equal to $A \approx 100$ MHz). The full electron-nuclei energy diagram can be found in the Supplemental Material. The measurements are performed at 7 T (Voigt geometry $\vec{B} \perp \vec{c}$) and 2 K.

The overall PL intensity, however, is much lower than what is observed for measurements without magnetic field. When a second laser (denoted as pump P) is resonant on the $|\downarrow\rangle$ to $|\downarrow\uparrow\rangle$ transition, an enhancement in signal is seen when the scanning laser scans across the transitions connected to $|\uparrow\rangle$. Without the pump laser (one laser measurement), population is transferred from one spin state of the ground state to the other, where it is trapped and cannot be re-excited. When the second laser is placed resonantly on the opposite spin state, population is transferred back to the spin state that the scanning laser can excite.

The two-laser experiment performed here is often referred to as reverse spectral hole burning [39]. The observed anti-hole can be used to determine the homogeneous linewidth of an optical transition in the presence of inhomogeneous broadening; the pump laser only repopulates the sub-ensemble resonant with the narrow band pump [39]. A double Voigt fit to the anti-hole linewidth reveals a linewidth of 8 GHz at 2 K, surprisingly similar to the PLE linewidth at 0 T (see Fig. 4 (a)). For the reported lifetime of 1350 ps for In_{Zn}^0 [20], the corresponding lifetime-limited linewidth is 120 MHz. Additionally, In_{Zn}^0 exhibits a strong hyperfine interaction of the bound electron with the spin-9/2 In nucleus, which splits the electron spin into ten levels which are spaced by 50 MHz [21, 22]. The expected linewidth of the reverse-spectral hole is 550 MHz due to the combined lifetime-limited linewidth and the hyperfine interaction. Thus, the 8 GHz anti-hole indicates additional broadening mechanisms that are the subject of future investigations.

In addition to the anti-hole peak, a narrow 1 GHz dip can

be observed on two-photon resonance (Fig. 6(a) inset). The presence of the dip is the signature of coherent population trapping and the establishment of a ground state spin coherence [9, 40–43]. Fig. 6(b) displays higher resolution spectra for the CPT dip seen in Fig. 6(a) for different excitation powers for the scanning and pump lasers. Also included is a CPT spectrum for in-grown Al_{Zn}^0 for reference. It is immediately evident that the CPT dip of In_{Zn}^0 is much broader than the 60 MHz Al_{Zn}^0 dip. Moreover, for lower combined powers of the scanning and pump lasers, the overall shape of the In CPT dip resembles an inverted top-hat, rather than the Lorentzian or Gaussian lineshape expected for a single homogeneously or inhomogeneously broadened transition. We attribute these unique features to the hyperfine interaction of the In donor electron with the spin-9/2 In nucleus. At high fields, in which the electron spin number is a good quantum number, two-photon Raman transitions correspond to dips occurring between states of the same nuclear spin. Thus, 10 dips separated by twice the hyperfine interaction are expected (see energy diagram in Supplemental Material). For Al_{Zn}^0 one expects 6 dips separated by 1.5 MHz [44]. The In data shown in Fig. 6 (b) is fit assuming ten Lorentzian dips spaced by 100 MHz. In the lowest power In CPT spectrum, the best fit corresponds to a dip linewidth of 85 MHz, however reasonable fits can be obtained for linewidths ranging from 50 to 170 MHz. Measurements of laser frequency drift and repeatability indicate the lack of resolved dips may be instrumentation limited at this time. However the flat CPT bottom confirms the expected 100 MHz hyperfine interaction and a potential path toward optical nuclear spin readout.

IV. CONCLUSION AND OUTLOOK

In summary, we have demonstrated that ion implantation and annealing can be used to form In_{Zn}^0 ensembles with promising optical and spin properties for quantum information applications. The implanted In_{Zn}^0 exhibit optical linewidths less than 10 GHz for the $\text{In}_{\text{Zn}}^0\text{X}$ transition, comparable with in-grown In_{Zn}^0 . T_1 exceeds previously reported values for in-grown Ga_{Zn}^0 [7], indicating that residual implantation damage has negligible influence on longitudinal spin relaxation. Notably, the dominant longitudinal spin relaxation mechanism for In_{Zn}^0 is the same process as what has been reported for Ga_{Zn}^0 [7], but with a distinctively lower overall relaxation rate. Using two-laser resonant excitation, we demonstrate that a coherent superposition of the ground states of In_{Zn}^0 can be created via CPT. Power-dependent CPT measurements indicate that, for low laser powers, the CPT lineshape for In_{Zn}^0 is determined by the hyperfine interaction between the donor bound electron and the spin-9/2 In nucleus. Thus, it may be possible in the future to access the nuclear spin degrees of freedom of implanted In_{Zn}^0 optically. These results demonstrate that ZnO is a promising host material platform for low-damage creation of donor qubits via ion implantation and subsequent annealing, and thus the deterministic fabrication of donor spin qubits with optical access.

V. ACKNOWLEDGEMENTS

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Appendix A: Sample Layout

A grid pattern defining nine implantation areas is fabricated on the surface of the sample with a UV laser cutter (Protolaser U3) prior to implantation. Fig. 7 shows the layout. Tab. I lists the nominal implantation fluences used for each region marked in Fig. 7.

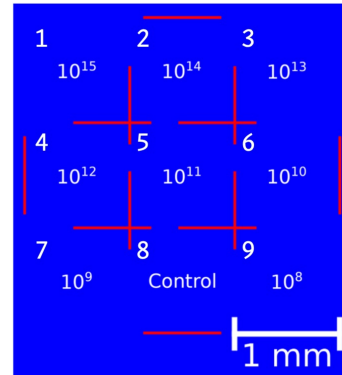


FIG. 7. Layout of the grid.

Region	Nominal fluence (cm^{-2})	Measured fluence (cm^{-2})
1	10^{15}	/
2	10^{14}	/
3	10^{13}	1.1×10^{14}
4	10^{12}	5.0×10^{12}
5	10^{11}	/
6	10^{10}	1.7×10^{10}
7	10^9	/
8	0	1.3×10^{11}
9	10^8	/

TABLE I. Summary of nominal implantation fluences and measured implantation fluences from SIMS for the different regions marked in Fig. 7. “/” denotes not measured.

Appendix B: Photoluminescence Spectra with implantation fluence

Fig. 8 shows normalized PL spectra for an as-grown ZnO single crystal and for different In implantation regions after annealing. Each spectrum corresponds to a region in Fig. 7. The significant broadening of the $\text{In}_{\text{Zn}}^0\text{X}$ line at higher fluences is evident, and only the $\text{In}_{\text{Zn}}^0\text{X}$ transition can be observed for implantation fluences exceeding 10^{11} cm^{-2} .

Appendix C: New donor lines after implantation

Fig. 9 shows PL intensity per excitation power for the 10^9 cm^{-2} implantation fluence. At powers above $9 \mu\text{W}$, a low energy shoulder on the Al peak ($\sim 3.3606 \text{ eV}$) grows with increasing laser power. This shoulder is not observed in non-implanted samples. The origin of this new excitonic feature

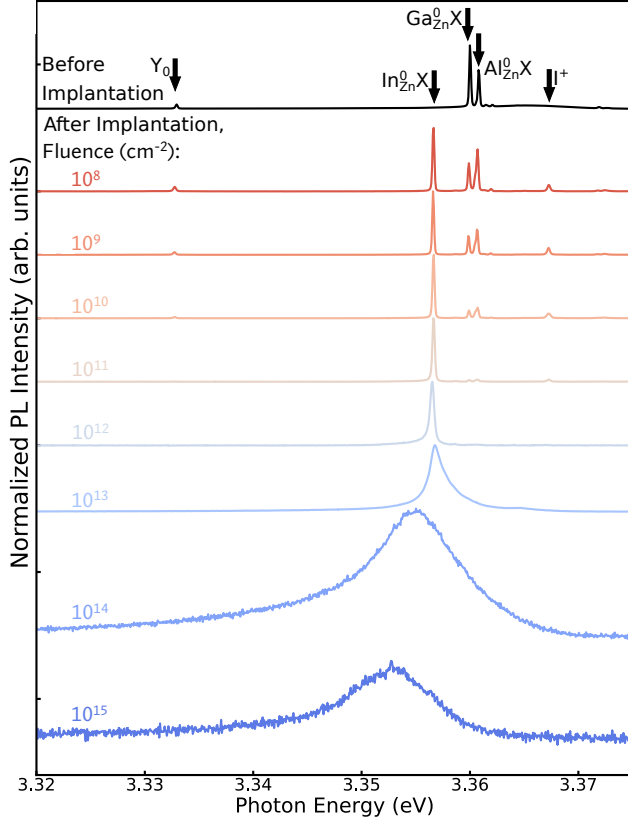


FIG. 8. PL spectra for an as-grown ZnO single crystal and for the crystal after In implantation of different fluences. The maximum intensity of each background-subtracted spectrum is normalized unity. $T = 7.5$ K, $\lambda_{\text{exc}} = 360$ nm, $I_{\text{exc}} = 800$ nW.

is not known, however it has a similar energy to the I_7 line related to carbon impurities that has been observed in prior work [45]. If this peak is carbon related, it is unclear how carbon has been introduced during the In implantation and annealing process.

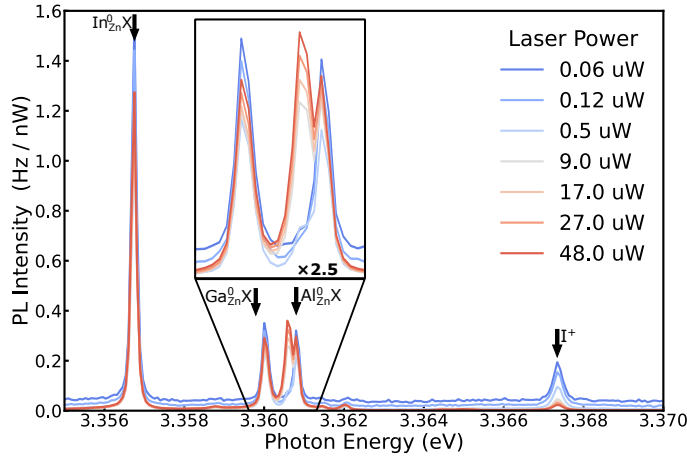


FIG. 9. PL spectra per laser power for 10^9 cm $^{-2}$ implantation for different laser powers. $T = 10.5$ K, $\lambda_{\text{exc}} = 360$ nm.

Magneto-PL spectra at varying external magnetic fields in the Voigt geometry ($\vec{B} \perp \vec{c}$) from $B = 0$ T to $B = 7$ T in Fig. 10 show the Zeeman splittings of transitions $\text{In}_{\text{Zn}}^0\text{X}$, $\text{Ga}_{\text{Zn}}^0\text{X}$ and $\text{Al}_{\text{Zn}}^0\text{X}$. In addition, the appearance of a transition at nonzero field near 3.3664 eV suggests a forbidden transition at zero field is allowed at nonzero field. Both this new transition at 3.3664 eV and the I^+ line at 3.3673 eV do not split at nonzero magnetic field. These observations are consistent with transitions that originate from excitons bound to ionized In donors $\text{In}_{\text{Zn}}^+\text{X}$. [46].

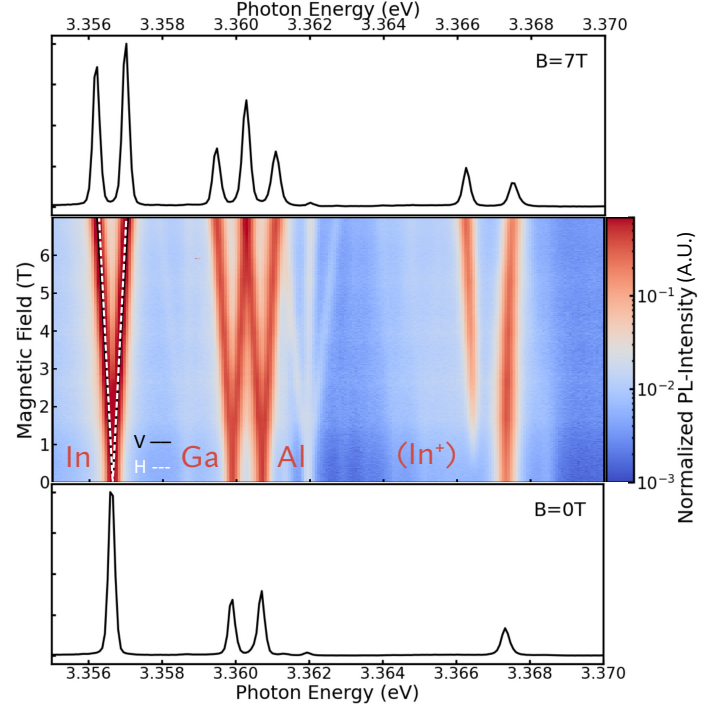


FIG. 10. Bottom panel: Above-band PL spectrum of the In-implanted ZnO crystal $B = 0$ T. Middle panel: Heatmap of the above-band PL at $B = 0$ to 7 T. The dashed white lines and solid black lines denote the expected transitions based on the g-factors of the electron and the hole determined in Sec. VII. Top panel: Above-band PL at $B = 7$ T.

Appendix D: Relationship between indium-galium PL ratio and PLE intensity

We observe a linear relationship between the $\text{In}_{\text{Zn}}^0\text{X}$ PLE intensity A and the PL intensity ratio R_{InGa} for low implantation fluences ($R_{\text{InGa}} < 30$). As shown in Fig. 11, by fitting a linear curve on 2 K and 7.5 K data, we estimate that $A = (0.23 \pm 0.01)R_{\text{InGa}}$ for $R_{\text{InGa}} < 30$. $R_{\text{InGa}} < 30$ corresponds to nominal implantation fluences lower than 5×10^{10} cm $^{-2}$.

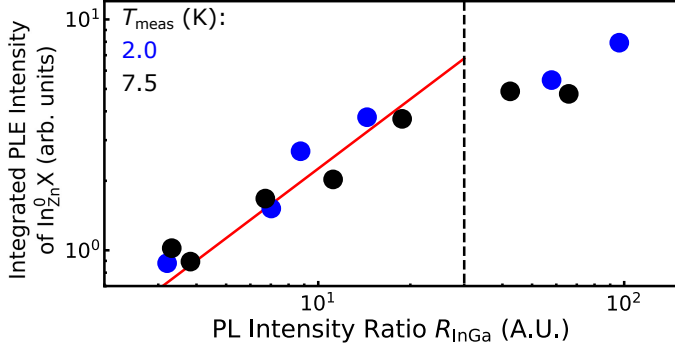


FIG. 11. PLE intensity of $\text{In}_{\text{Zn}}^0\text{X}$ as a function of the PL intensity ratio between the $\text{In}_{\text{Zn}}^0\text{X}$ and $\text{Ga}_{\text{Zn}}^0\text{X}$ lines at 2 K (blue dots) and 7.5 K (black dots). The red line depicts a linearly fitted curve.

Appendix E: Photoluminescence Excitation Spectroscopy

Fig. 12(a) shows PLE spectra for implanted $\text{In}_{\text{Zn}}^0\text{X}$. The PLE intensity is plotted by integrating the total signal of two-electron satellites (TES) and phonon-replicas. Fig. 12 (b) displays the corresponding spectra for the laser on- and off-resonance with the $\text{In}_{\text{Zn}}^0\text{X}$ optical transition. The two-electron satellite transitions can only be observed for neutral donors, and would not be observed for $\text{In}_{\text{Zn}}^+\text{X}$.

Appendix F: Longitudinal spin relaxation time

The longitudinal spin relaxation time T_1 of *in situ*-doped Ga_{Zn}^0 donor ensembles has been thoroughly investigated in [5, 7]. The T_1 is determined by measuring the population recovery of spin state $|\downarrow\rangle$ after optically pumping the population into the spin state $|\uparrow\rangle$ using resonant excitation for different delay times τ after the optical pumping pulse (see Fig. 13(a)). The measurement scheme and energy level diagram are shown as insets in Fig. 13(a).

In prior work [7], we demonstrated an excitation energy dependence that was attributed to varying effective donor density at a given resonant (or near-resonant) excitation energy. In this work, we are able to directly investigate the donor density dependence of T_1 by probing locations of different implanted In fluences. In Fig. 13(b) we show that for a given In fluence of 10^9 cm^{-2} , T_1 varies with excitation energy, same as what has been observed from Ga donors in previous studies. A shorter T_1 is observed when probed on resonance with the ensemble implanted In donors, indicating that a higher density of probed sub-ensemble shortens the measured T_1 . Figure 13(c) depicts the dependence of T_1 on the PL intensity ratio between In_{Zn}^0 and Ga_{Zn}^0 , i.e. a proxy for implantation fluence. At higher implantation fluences, T_1 becomes shorter, which agrees qualitatively with our explanation about effective donor density dependence of T_1 .

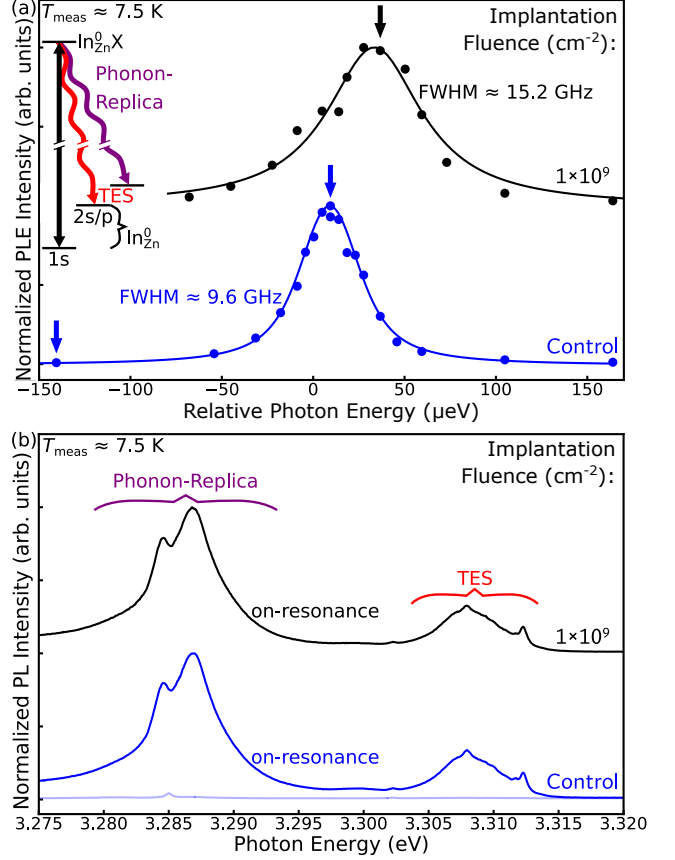


FIG. 12. (a) PLE spectra integrating the TES and phonon replica signals (inset) for 10^9 cm^{-2} implantation and the control region. FWHMs of PLEs are obtained by fitted Voigt profiles. (b) Spectra of TES and phonon replica on- and off-resonance from $\text{In}_{\text{Zn}}^0\text{X}$ taken at excitation wavelengths marked by arrows in (a). The maximum intensity of each background-subtracted spectrum is normalized to unity. $T = 7.5 \text{ K}$.

Appendix G: g-factors of neutral donor-bound excitons

The D^0X Zeeman energy is determined by the un-paired hole spin. At nonzero external magnetic field perpendicular to the crystal axis (Voigt geometry $\vec{B} \perp \vec{c}$), the energy level configuration of the four possible donor bound exciton transitions and each of their polarization are labeled in the inset of Fig. 14. The splitting of the hole is small compared to that of the electron. At the experimental applied fields, the separation between pairs of transitions V_\downarrow and H_\downarrow , V_\uparrow and H_\uparrow cannot be resolved. As shown in Fig. 14, by collecting V and H polarizations, a shift in the excitonic emission can be observed. This shift represents a lower bound of the g-factor of the hole, $g_h^\perp = 0.12$. The g-factor of the electron is 1.95, which are in good agreement with Ref. [46].

Appendix H: Coherent Population Trapping

Fig. 15 shows a schematic illustration of the two-photon transitions in the $\text{In}_{\text{Zn}}^0/\text{In}_{\text{Zn}}^0\text{X}$ system due to the hyperfine

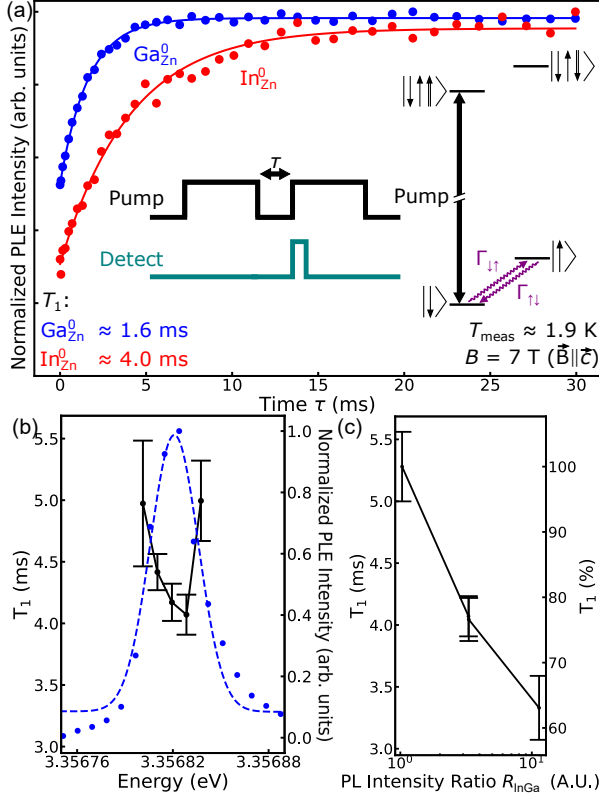


FIG. 13. (a) Population recovery of state $|\downarrow\rangle$ from relaxation of the optically pumped state $|\uparrow\rangle$ as a function of delay time τ between each pump pulse for implanted In (10^9 cm^{-2}) and in-grown Ga. The insets show the pump and detect sequence and the energy level diagram. T_1 equals the decay constant of the fitted exponential profiles. (b) Longitudinal spin relaxation time T_1 of In_{Zn}^0 as a function of excitation photon energy (black points, left y-axis) and PLE spectrum (blue points, right y-axis) for a fluence of 10^9 cm^{-2} . Pump pulse on resonant with $|\downarrow\rangle \Leftrightarrow |\downarrow\uparrow\rangle$. (c) T_1 as a function of the PL intensity ratio between In_{Zn}^0 and Ga_{Zn}^0 denoted R_{InGa} . Different ratios correspond to different implantation fluences (see main text and Tab. I). Error bars are one standard deviation of the exponential fit of T_1 curves in (a). Faraday geometry ($\vec{B} \parallel \vec{c}$), $B = 7 \text{ T}$ and $T = 1.9 \text{ K}$.

interaction between In nuclei (all stable In isotopes have $I = 9/2$) and the valence electron of In_{Zn}^0 [21, 22]. It is assumed that the two-photon resonance necessary for CPT can only occur between ground state levels with the same nuclear spin quantum number (m_1), i.e., nuclear spin flips are forbidden. For a constant wavelength of the pump laser, this leads to different resonance conditions depending on m_1 , i.e., different resonant wavelength for the scanning laser. We expect ten resonances equally spaced by A . CPT can occur at different detunings from the single level representing $|\downarrow\uparrow\rangle$. The hyperfine splitting of the excited state is expected to be much smaller than that of the ground state due to the spin-singlet nature of the electrons and the p-orbital nature of the hole.

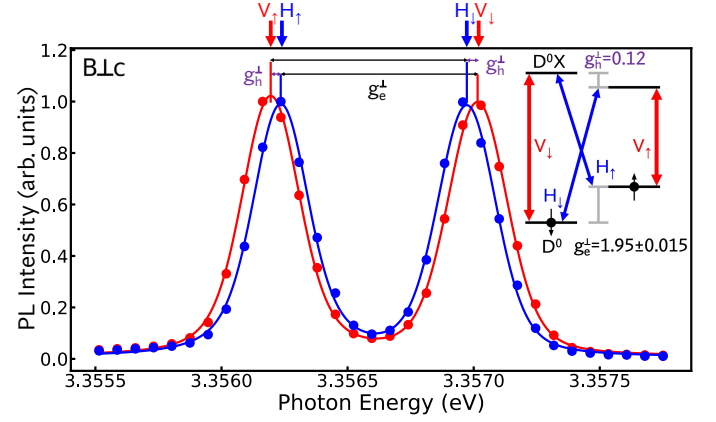


FIG. 14. Magneto-PLs taken with different polarization optics show the energy separation used to find the g-factors of the electron and the hole using $\Delta E = g\mu_B B$. Inset: Energy level diagram at $\vec{B} \perp \vec{c}$, $B > 0$. The measured lower bound of the hole g-factor is 0.12 and the corresponding electron g-factor is 1.95.

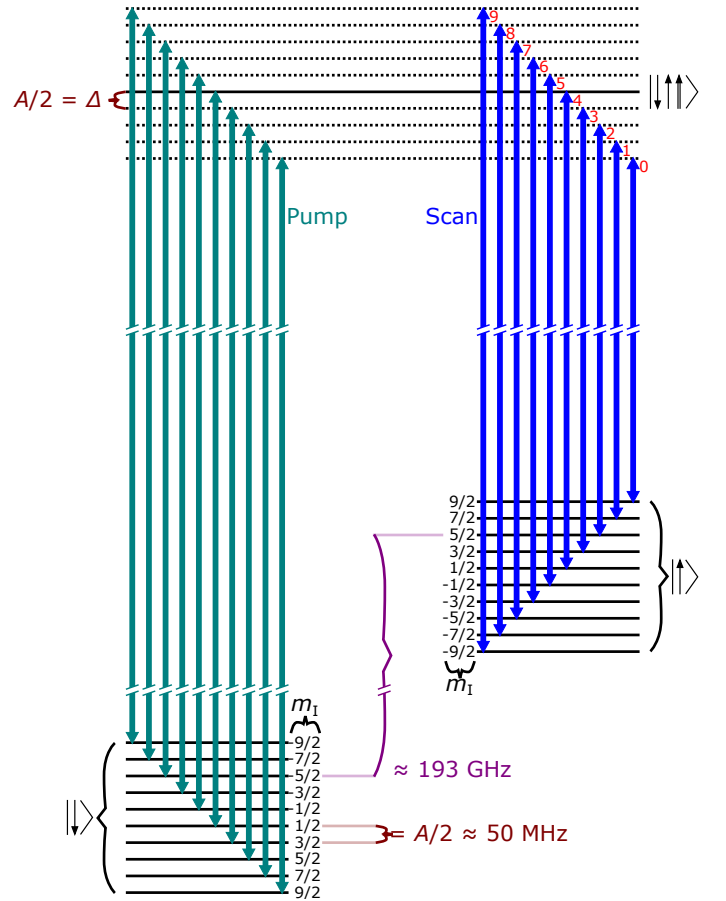


FIG. 15. Ten expected two-photon resonances of CPT due to the hyperfine interaction between the valence electron of In_{Zn}^0 and In nuclei of the same m_1 .

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