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Strongly-coupled plasmon and phonon polaritons as seen by photon and electron probes

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The ability to control and modify infrared excitations in condensed matter is of both fundamental and application interests. Here we explore a system supporting low-energy excitations, in particular, mid-infrared localized plasmon modes and phonon polaritons that are tuned to be strongly coupled. We study the coupled modes by using far-field infrared spectroscopy, state-of-the-art monochromated electron energy-loss spectroscopy, numerical simulations, and analytical modeling. We demonstrate that the electron probe facilitates a precise characterization of polaritons constituting the coupled system, and enables an active control over the coupling and the resulting sample response both in frequency and space. Although far-field optical spectra can be substantially different from near-field electron energy-loss spectra, we show that a direct comparison is possible via post-processing and right positioning of the electron beam. The resulting spectra allow us to evaluate the key parameters of the coupled system, such as the coupling strength, which we demonstrate to be probe independent. Our work establishes a rigorous description of the spectral features observed in light- and localized electron-based spectroscopies, which can be extended to the analysis of analogous optical systems with applications in heat management, and electromagnetic field concentration or nanofocusing.

I. INTRODUCTION

Polaritons are quasiparticles emerging due to strong coupling between photons and excitations in condensed matter, such as plasmons in metals and semiconductors or optical phonons in ionic crystals [1]. The resulting plasmon polaritons (PPs) and phonon polaritons (PhPs) are known to facilitate the confinement of light at the nanoscale, often deeply below the diffraction limit, which finds applications in nanoscale focusing [2-5], extreme waveguiding [6], design of novel optical elements [7] or enhanced molecular detection [8]. Spatial confinement and energies of the polaritonic excitations can be typically tuned by nanostructuring, e.g. in a form of gratings or the so-called optical nanoantennas [9], but also by coupling between polaritons themselves. Such coupling results in hybridized modes [10-15] and introduces more degrees of freedom to engineer system functionalities and on-demand optical response [16, 17],

Both uncoupled and coupled polaritons in the midinfared (MIR) energy range have been experimentally explored by far-field IR spectroscopy [18–21]. IR spectroscopy provides very high spectral resolution, however, its spatial resolution is restricted by the diffraction limit. Accessing both spectral and spatial information on the coupled polaritonic modes is only possible by utilizing near-field probes. Besides scanning near-field optical microscopy (SNOM) [22], which relies on light localized at sharp tips, we can nowadays employ focused fast electron beams. Only very recently, due to instrumental improvements [23], electron energy-loss spectroscopy (EELS) [24] in a scanning transmission electron microscope (STEM) has become another suitable technique for mapping MIR polaritons with (sub-)nanometric spatial and few-meV spectral resolution [25–32].

Coupled polaritonic systems have been so far analyzed by one of the aforementioned experimental techniques, however, a correlative study that would bring detailed understanding of common aspects and differences between spectral features measured by light- or electronbased spectroscopic techniques in the same sample is, to the best of our knowledge, missing. In this work, we present such correlative study and explore nanostructured systems, where both infrared PhPs and PPs can exist. We probe the electromagnetic coupling between MIR surface PhPs (SPhPs) in a thin silicon dioxide film and low-energy localized surface plasmon (LSP) modes formed by the confinement of PPs in micrometerlong gold antennas. We find that far-field IR spectra of the coupled LSPs-SPhPs can be substantially different from EEL spectra, which we confirm by experiments supported by numerical simulations and analytical modeling. We show that by precisely positioning the electron beam, the coupling between the polaritonic excitations can selectively trigger either SPhPs only or coupled LSPs-SPhPs. We also present a post-processing analysis in the EEL spectra that facilitates identification of the hybrid modes, allowing an easier comparison to far-field optical spectroscopy.

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II. METHODS

II.A. Numerical simulations

Finite-difference time-domain simulations of far-field optical spectra were obtained using the Ansys Lumerical software [33]. A single rectangular antenna placed on a semi-infinite membrane was illuminated by a linearly polarized plane wave impinging at normal incidence with respect to the substrate provided by a total-field scattered-field (TFSF) source. The scattering (absorption) spectra were calculated from the scattered (total) power flux monitors placed outside (inside) the TFSF source. The whole simulation domain with dimensions of 10 μ m \times 10 μ m \times 6 μ m³ was enclosed in a perfectly matched layer.

EEL spectra and field plots were obtained using the finite element method implemented within the Comsol Multiphysics software [34], where we calculate the induced electromagnetic field emerging in the interaction of the nanostructure with a line current representing the focused electron probe. The EEL probability is then evaluated as [35]

$$\Gamma(\mathbf{R}_{\rm b},\omega) = \frac{e}{\pi\hbar\omega} \int_{-\infty}^{\infty} \mathrm{d}z \operatorname{Re}\left\{E_z^{\rm ind}(\mathbf{R}_{\rm b},z,\omega) \,\mathrm{e}^{-\mathrm{i}\omega z/v}\right\},\tag{1}$$

where e is the elementary charge, $\hbar\omega$ energy, and v is the electron velocity. z denotes the optical axis along which the fast electron propagates, $\mathbf{R}_{\rm b} = (x_{\rm b}, y_{\rm b})$ is the impact parameter (*i.e.* position in the transverse plane with respect to the optical axis which the electron trajectory intersects) and where we integrate the z component of the induced electric field along the beam trajectory.

II.B. Experimental methods

Electron beam lithography on SiO₂ TEM membranes (thickness 40 nm) was performed using a scanning electron microscope Mira3 (Tescan) with a laser interferometry stage (Raith). Subsequent gold deposition was done using an electron beam evaporator (Bestec).

Fourier-transform infrared spectroscopy (FTIR) was measured using an IR microscope [Vertex 70v and an IR microscope Hyperion 3000 (Bruker)] with an aperture allowing the signal collection from an area of 50 μ m \times 50 μ m² in a spectral range of 600-6000 cm⁻¹ and resolution of 2 cm⁻¹. Convergence (illumination) and collection semi-angles were between 15° and 30°.

Electron energy-loss spectra were acquired using a Nion monochromated aberration-corrected scanning transmission electron microscope operated at 60 kV accelerating voltage [23, 36]. The measurements were performed with a convergence semiangle of 30 mrad, a collection semiangle of 20 mrad, a beam current of ~ 20 pA, using a Nion Iris spectrometer with a dispersion of 0.4 meV/channel [37], and an energy resolution (defined as the full width at half-maximum of the zero loss peak) between 10 meV and 14 meV.

III. RESULTS AND DISCUSSION

III.A. Response of uncoupled system constituents

To understand the spectral response of the studied nanostructured system, we first theoretically analyze the response of its individual constituents, *i.e.* a SiO_2 film and a long Au antenna, when they are excited by light and by a focused electron probe in Fig. 1. The optical response of SiO_2 in the spectral region of interest is governed by a phononic mode corresponding to the Si-O-Si symmetric stretching vibration around 100 meV and a mode stemming from the Si-O-Si antisymmetric stretch around 130 meV [38]. The latter mode is associated with strong polarization yielding the transverse optical - longitudinal optical (TO-LO) splitting associated with the energy region, known as the Reststrahlen band (RB), where $\operatorname{Re}[\epsilon_{SiO_2}] < 0$ which forbids propagation of light within the bulk. However, in presence of boundaries, such as those imposed in the thin film geometry, a new interface SPhPs emerge inside the RB [40].

Due to the energy-momentum mismatch, infrared photons cannot excite SPhPs in a thin film as it is demonstrated in Fig. 1(a). The most intense spectral feature corresponds to the excitation of the TO phonons which yields a strong absorption (red line) and featureless field profile (not shown). The absorption spectrum is nearly equal to extinction (scattering is negligible) and thus proportional to $\text{Im}[\epsilon_{\text{SiO}_2}]$.

Focused fast electrons, on the other hand, can provide sufficient momentum and naturally excite the SPhPs inside the RB as demonstrated by the green spectrum in Fig. 1(a), consistent with recent experiments [27, 41, 42]. More precisely, fast electrons interacting with a thin film supporting polaritons can excite either a chargesymmetric or charge-antisymmetric SPhP modes [9, 43] [see the inset in (a)]. SPhPs in SiO_2 are rather damped compared especially to those in ionic crystals [22, 25], resulting in the two SPhP modes to be spectrally indistinguishable. However, due to the symmetry of the probing field, the main peak close to 140 meV is dominated by charge-symmetric SPhPs as shown schematically in the inset and further confirmed in the field plots in (c). The field plots demonstrate that the electron beam couples (with different probability) to SPhPs with varying wavelengths and energies within the entire RB. The fast electrons can also excite the bulk LO phonon, which requires high momentum to be activated, corresponding to the polarization along the electron trajectory. The LO phonon excitation appears as a small "shoulder" close to 155 meV.

To enable an efficient coupling between the different types of polaritons, a spatial overlap of their electromag-



FIG. 1. (a) Numerically calculated EEL (green) and optical absorption (red) spectra of an infinitely extended SiO₂ thin film with a thickness of t = 40 nm. The dielectric response of SiO₂ is modeled using complex dielectric response obtained from experimental measurements in Ref. [38]. All the spectra are probe-position invariant. Vertical dashed lines denote energies of the TO and LO phonons in SiO₂. The inset shows charge-symmetric (left) and charge-antisymmetric (right) SPhP modes. (b) Spectral response of a gold (dielectric response taken from Ref. [39]) rectangular plasmonic antenna with the length $L = 3 \mu m$, width w = 400 nm and height h = 25 nm on top of a substrate of the thickness t = 40 nm with a constant dielectric response (characterized by a relative dielectric constant $\epsilon_{sub} = 1.8$). Absorption (red line) cross section is calculated for excitation by a plane wave impinging at normal incidence along the z axis with a linear polarization aligned along the long antenna's axis (x axis). EEL spectra are obtained for an electron beam placed 10 nm outside the antenna's corner (solid green line) and at the antenna's center (dashed green line) as shown in the schematics. The electron beam energy is 60 keV in both (a,b). (c) z-component of the total electric field emerging in the excitation of the SiO_2 film by focused electrons (trajectories shown by green arrows) at two energies around the peak in EEL spectrum in (a). (d) z-component of the electric field confirming the excitation of the dipolar plasmon by the plane wave (red frame, top) and the electron beam placed close to the antenna side (green solid frame, middle). When the electron beam passes close to the antenna center, it can only weakly excite a higher-order plasmon mode (dashed green frame, bottom). All plots are obtained at energy 150 meV approximately corresponding to the peaks in (b) and are extracted at the central plane y = 0 while the electron beam is passing in the plane $y_{\rm b} = d/2 + 10$ nm (10 nm from the antenna shorter edge). We show total/induced field in the electron beam/plane-wave excitation and real/imaginary part of the field in panels (c)/(d).

netic fields as well as an overlap of their energies needs to be simultaneously targeted. As the SPhPs in SiO₂ emerge in the RB between ~ 130 and 155 meV, we shall tune the LSP resonances accordingly by a careful choice of the metal used and dimensions of the plasmonic antenna. We consider gold particles of a rectangular shape and numerically simulate their spectral response as if the antenna were probed by a plane wave polarized along its long axis or by a perfectly focused electron beam placed close to the antenna's corner [see the inset in Fig. 1(b)].

For antennas with the dimensions $L \times w \times h = 3000 \times$

 $400 \times 25 \text{ nm}^3$ placed on a 40-nm thick dielectric substrate (mimicking a constant dielectric offset imposed by SiO₂ film), we obtain the theoretical lowest-energy dipolar LSP resonance centered around 150 meV as demonstrated in Fig. 1(b). The light excitation leads to relatively strong absorption (red line) associated with a dipolar mode that makes the electric field enhanced close to the antenna's tips. The electron beam is also capable of excitation of the same dipolar mode, which is demonstrated in the numerically calculated EEL probability (solid green line). Alternatively, focusing the electrons close to the antenna center results in a near zero signal (dashed green line) in the energy region of interest, since only higher-order modes at larger energies can be excited in this case [44, 45]. We confirm these observations in Fig. 1(d), where we plot the electric field in the vicinity of the antenna. For the plane-wave excitation (red-framed plot) and for the electron beam placed close to the antenna side (green frame), the field clearly corresponds to the opposite charges accumulated at left and right side of the antenna, and thus the dipolar plasmon. The <u>centered</u> electron beam placed at the antenna center is capable of exciting only a higher-order plasmon and therefore the corresponding plot [dashed green frame in Fig. 1(d)] is dominated by the field produced by the electron beam.

III.B. Coupled system

From the analysis of the system constituents, we can see that in an uncoupled scenario, the setup consisting of a gold antenna on top of a thin SiO_2 film can sustain three dominant polaritonic modes in the energy region of interest: a single LSP mode, and symmetric and anti-symmetric thin-film SPhP modes (in formulas abbreviated as SPhP₁ and SPhP₂, respectively). The electromagnetic interaction between these polaritonic modes can be described by a model of three coupled oscillators captured within the matrix

$$\mathbf{M} = \begin{bmatrix} 1/(\alpha_{\rm LSP} f_{\rm LSP}) & -K_1 & -K_2 \\ -K_1 & 1/(\alpha_{\rm SPhP_1} f_1) & 0 \\ -K_2 & 0 & 1/(\alpha_{\rm SPhP_2} f_2) \end{bmatrix},$$
(2)

where $\alpha_n = 1/[\omega_n^2 - \omega(\omega + i\gamma_n)]$ (here $n = \{LSP, SPhP_1, SPhP_2\}$) determines the spectral response of a mode with a resonant energy $\hbar\omega_n$, damping $\hbar\gamma_n$ and effective strength f_n . In the following, we assume that the phononic modes are non-radiative, while the damping of the LSP involves radiative losses, *i.e.* $\gamma_{LSP} \rightarrow \gamma_{LSP} + \omega^2/(6\pi\epsilon_0c^3)$ [15, 46, 47]. The coupling will introduce three new hybrid modes whose eigenfrequencies and dampings are obtained from $|\mathbf{M}| = 0$. However, the coupling is efficient only if both spectral and spatial overlaps of the modes' electromagnetic fields are achieved, which is described by the coupling parameters K_1 and K_2 . We also assumed that SPhPs do not couple to each other.

Now we consider the same antenna and thin film dimensions as in Fig. 1 and analyze optical absorption and scattering spectra of the coupled system (red and blue lines in Fig. 2(a), respectively), which exhibit several spectral features. The absorption is again dominated by the excitation of the TO phonon mode and with a similar spectral behavior as that of pure SiO_2 [as shown in Fig. 1(a)] which is due to the large extent of the thin film and presence of absorption unrelated to the coupling. The scattering, on the other hand, clearly shows excitations beyond the RB as well as an additional weaker peak within the RB. All three peaks are associated with the new hybrid modes emerging due to the coupling. We also empirically find that the experimental measurement of $(1-T_{\rm rel})$, where $T_{\rm rel}$ is the relative transmission obtained from FTIR (orange line), strongly resembles the theoretically predicted scattering spectra with only a slight discrepancy in positions of the new peaks (see also Fig. 3(b) and Appendix A).

As previously mentioned, an electron beam allows to control the strength of the plasmonic excitation by simply positioning the beam at different relative positions from the antenna's center (or tip), as shown in the inset of Fig. 2(b). The corresponding simulated spectra (shown in the figure as thin lines) then capture either only nearly non-interacting SPhPs and bulk LO phonon excited in the SiO₂ (black), or a mixture of non-interacting SPhPs and coupled LSP-SPhPs (red to violet). The coupling is clearly manifested by a dip around the TO phonon position and emergence of new peaks beyond the RB. The weaker excitation inside the RB is here indistinguishable due to the presence of the uncoupled SPhP and bulk signal.

Notice that the spectrum calculated at the antenna's center is slightly different from that of a plain SiO_2 film shown in Fig. 1(a). This happens because the antenna represents an obstacle for the SPhPs and thus fa vors excitation of SPhPs with slightly different momenta. As faintly observed in the corresponding field plot in Fig. 2(d) at 137 meV, the SPhPs interact with the edges of the antenna.

The experimental EEL spectra plotted in Fig. 2(b) (shown as thick lines) obtained for similar beam positions as in the simulations show less features due to limited energy resolution (between 10 and 14 meV). However, a clear broadening and emergence of "shoulders" of the main peak associated with the polaritonic coupling when the beam approaches the tip of the antenna can still be resolved. Similar behavior of the simulated spectra is obtained when the finite experimental resolution is introduced in the simulations (see Fig. 6 in Appendix).

In general, the far-field optical spectra of the coupled system are very different to EELS due to the absence of the spectral features corresponding to the nearly uncoupled SPhPs that are not directly excitable by plane waves, but launchable by fast electrons. Interestingly, we can achieve resemblance between the light and EEL spectral signals by post-processing of EEL spectra. As only bulk LO phonon and nearly uncoupled SPhPs are excited by the beam at the center of the antenna, we take the black spectrum in Fig. 2(b) as a reference and subtract it from the spectra obtained with the beam positioned at different distances from the antenna tip. Although the directly launched SPhPs for varying beam positions acquire slightly different momenta because of varying distance between the beam and antenna edges at which the polaritons scatter, such subtraction makes the EEL spectra to be better comparable with optical scattering spectra. See for instance the selected spectra in Fig. 2(c).



FIG. 2. Comparison of electron and light spectra for an approximately optimally-coupled antenna-substrate system (individual system components have the same geometry and dimensions as in Fig. 1). (a) Experimentally measured FTIR spectrum corresponding to (1-T), where T is the total transmission (orange line) for light polarized along the long antenna axis. Numerically calculated absorption (red) and scattering (blue) cross-section spectra for an entire system are shown for comparison. (b) Experimental vs. calculated electron spectra (thick vs. thin lines) obtained for the 60 keV beam, which is placed just next to the antenna and scanned along the antenna's long axis. Colors approximately correspond to the electron positions as marked schematically in the inset. (c) Selected EEL spectra from (b) after subtraction of the (reference) spectrum recorded at the center of the antenna, which is dominated by uncoupled SPhPs and LO phonon excitation in SiO₂ [black lines in (b)]. For clarity, subsequent spectra in (b,c) are vertically shifted by a constant offset. The vertical dashed lines denote energies of TO and LO phonon modes in SiO₂. (d) z-component of the electric field for plane-wave and electron excitation (red and blue frames, respectively) at different energies as denoted above. The electron beam is placed at the side of the antenna or close to its center (solid vs. dashed frames; electron trajectories represented by green lines). All plots are extracted at the central plane y = 0 while the electron beam is passing in the plane $y_b = w/2 + 10$ nm (10 nm from the antenna shorter edge). We show total/induced field in the electron beam/plane-wave excitation.

The resulting peak intensities, relative strength and contrast however change with the beam position, which controls the plasmon mode excitation efficiency. We emphasize that the subtraction allows clear distinction of the coupling-related spectral signatures also for the measured data, which before the subtraction in (b) showed only one broad spectral feature.

Electric field profiles shown in Fig. 2(d) for the planewave (red frames) and electron-beam (green frames) excitation are dominated by the presence of the dipolar plasmonic field, except for the cases when the electron beam is passing close the antenna center (dashed green frames). Hence, they strongly resemble the field plots in Fig. 1(d) with slight, yet important differences due to the presence of SiO_2 film. 1) depletion vs. enhancement of the field inside the SiO_2 film beneath the antenna (energies outside the RB; 122 vs. 165 meV), and 2) emergence of uncoupled SPhPs freely propagating from the antenna at 137 meV within the RB. Unfortunately, due to the strong damping of the SPhPs, we can only observe one field oscillation [similarly as in Fig. 1(c)] near the antenna boundaries and close to the electron beam. We also note that the directly-launched SPhPs strongly contribute to EEL spectra [black line in Fig. 2(b)] as they couple to the

electron beam, while for plane-wave excitation, we only observe a small contribution from the SPhPs launched secondarily by the antenna (faint features close to the antenna sides appearing in the plot at 137 meV).

IV. CONTROLLING THE COUPLING

The coupling can be adjusted by tuning the LSP energies as shown in many preceding studies [8, 14, 28, 45]. Fig. 3 shows the dependence of the coupled system response on the parameter controlling the energy of the LSP, which is simply given by the length of the antenna's long axis L. Changing the antenna's dimension enables to analyze the length-dependent coupling strengths $g_i = K_i \sqrt{f_i f_{\text{LSP}}} / \sqrt{\omega_{\text{SPhP}_i} \omega_{\text{LSP}}}$, where $i = \{1, 2\}$ [48], which can be obtained from fitting the optical scattering cross section and reference-subtracted EEL spectra to analytical models. We find that the overall system spectral response is approximately governed by an effec-



FIG. 3. Coupled system response as a function of the plasmonic antenna length. (a,b) Optical scattering and (c,d) referencesubtracted EEL spectra (see Fig. 2 for details). Simulated pseudo-dispersions in (a,c) are obtained via the transformation $k_{\text{LSP}} = \pi/L$, where L is the antenna length and k_{LSP} is the effective wavevector of the dipolar LSP. Gray dashed lines trace energies of the uncoupled LSPs and PhPs whereas the colored symbols denote energies of the new hybrid modes characterized by eigenvalues obtained from fitting of spectra and solution of $|\mathbf{M}| = 0$. Examples of numerically calculated, fitted and experimental spectra (thin, dashed and thick curves, respectively) for three selected lengths (2.4/3.0/3.6 µm) are shown in (b,d) [denoted by vertical colored dashed lines in (a,c)]. All EEL spectra were obtained for a 60 keV electron beam placed close to the corner of the antenna [violet line in Fig. 2(c)]. Experimental measurements of EELS and FTIR were performed on the same sample.

tive polarizability

then be modeled by [46, 47]

$$\sigma_{\rm sca} \approx \frac{k^4}{6\pi\epsilon_0^2} \left|\alpha\right|^2,\tag{4}$$

$$\alpha \propto [\mathbf{M}^{-1}]_{11} = \frac{\alpha_{\mathrm{LSP}J}}{1 - \sum_{i=1,2} g_i^2 \omega_{\mathrm{SPhP}_i} \omega_{\mathrm{LSP}} \alpha_{\mathrm{SPhP}_i} \alpha_{\mathrm{LSP}}},$$
(3)

where
$$f$$
 is an effective response strength, and which in-
dicates that the LSP primarily couples and decouples to
the propagating IR photons as well as to the evanescent
electromagnetic field supplied by the electron beam. The
 $[\mathbf{M}^{-1}]_{11}$ term also suggests that the SPhPs are launched
secondarily by the antenna.

The scattering cross section spectra in Fig. 3(a,b) can

where ϵ_0 is the permittivity of vacuum and $k = \omega/c$ is the free-space wave vector of the light with photon energy $\hbar\omega$ moving at the speed of light c. To model the reference-subtracted EEL probability in Fig. 3(c,d), we use [15]

$$\text{EELS} - \text{reference} \approx \mathcal{F}_1(\omega) \text{Im} \{\alpha\} + \mathcal{F}_2(\omega) \text{Im} \{\alpha_{\text{SPhP}_1}\},$$
(5)

where $\mathcal{F}_{1/2}(\omega) = A_{1/2}\omega^{j_{1/2}}$ with A_x and j_x being unknown real fitting parameters representing scaling factors and powers. These spectral functions incorporate an overlap of the plasmonic field with the field of the electron beam. The second term in Eq. (5) captures a residual spectral contribution of the non-interacting SPhPs, which remains even after the reference subtraction. A residual spectral contribution remains because a slightly larger portion of SPhPs (or SPhPs with different momenta) can be excited when the beam is placed close to the antenna's corner. This residue can be clearly seen within the RB in Fig. 3(c) when compared to Fig. 3(a).

Fitting the simulated scattering and the referencesubtracted EEL spectra with models in Eqs. (4) and (5), respectively, allows to obtain the parameters characterizing the uncoupled system constituents, *i.e.* excitations' energies and dampings. The theoretically obtained LSP and SPhP energies are interpolated by the gray dashed lines in Fig. 3(a,c). We can observe the plasmon energy linearly increasing with the inverse antenna length, which is typical for MIR plasmonic antennas on transparent substrates [49]. Notice, however, that energies of both SPhPs remain nearly constant as expected. The equation $|\mathbf{M}| = 0$ together with the parameters obtained from the model fitting provides the energies of the new hybrid modes, shown as colored symbols. These energies should be close to the actual peak positions, but typically do not coincide perfectly. However, we observe a close correspondence of the coupled system energies obtained for both types of probes.

The simulated spectra are compared with the experimental results for three fabricated antenna lengths in Fig. 3(b,d). The $(1 - T_{rel})$ FTIR spectra exhibit a decent agreement with the calculated scattering with only slight discrepancies in the observed peak energies and relative strengths. However, it is important to keep in mind that the correspondence of the $(1 - T_{\rm rel})$ with the scattering cross section is established only empirically; an exact illumination and light collection geometry can play a role (see Appendix A for further discussion). Maybe more importantly, the optical spectra were recorded for an antenna array and thus involve many antennas with various imperfections and divergences with respect to nominal dimensions. On the other hand, each reference-subtracted experimental EEL spectrum in Fig. 3(d) was recorded for an individual antenna within the array and thus does not involve any size averaging, which represents a great advantage of using focused electron probes. However, some of the fine details are hidden due to the current instrumental resolution (see Fig. 6 in Appendix).

V. QUANTIFICATION OF THE COUPLING

The fitting enables to extract the values of the coupling strengths g_n which are key for the classification of the coupling in the system. We theoretically predict and experimentally confirm that a rectangular Au gold nanoantenna on a SiO₂ substrate can be in a strong coupling regime, supported by the fulfillment of the criterion [50] $2g_n > \gamma_{\text{LSP}} + \gamma_{\text{SPhP}_n}$ for coupling of the LSP with both SPhPs as documented in Fig. 4, where we find optimal coupling conditions for $L \sim 3.4 \,\mu\text{m}$. The fits of the optical spectra and reference-subtracted EELS (the latter not shown) provide similar coupling strengths with differences within uncertainties due to fitting errors, which demonstrates that the coupling is determined by the system itself, and is not probe dependent. Moving the electron beam towards the antenna center substantially lowers the overall efficiency of the LSP excitation, and thus the contrast of the spectral features. However, the coupling strengths stay nearly the same except for the beam positioned at the center of the antenna, where we observe a dramatic change of the coupling strengths towards zero as the dipolar LSP cannot be excited anymore.



FIG. 4. Coupling parameters compared to their damping extracted from the fitted optical spectra in Fig. 3 (fitting reference-subtracted EEL spectra provides values with a difference within ~ 1 meV). The criterion $2g_i > \gamma_{\text{LSP}} + \gamma_{\text{SPhP}_i}$ establishes the strong coupling.

VI. CONCLUSIONS

In conclusion, here we have performed a comparative experimental study of spectra of the coupled antennasubstrate system obtained with far-field light and nearfield electron spectroscopy. The study reveals fundamental differences when probing a complex polaritonic system with light and focused electron probes. We show that a precise positioning of the electron beam offers the possibility to probe coupled or uncoupled excitations at will, thus offering complementary information to that obtained from far-field optical spectroscopy.

We also present a post-processing analysis in the EEL spectra, that consists of subtracting a reference from spectra acquired for different beam positions with respect to the nanostructure system to reveal the strength of coupling between phonon and plasmon polariton excitations. The post-processing facilitates comparison of EEL with far-field optical spectra, from which we find that both

techniques can yield nearly identical coupled-system parameters. Such comparison confirms that the coupling is eventually determined by the optical properties and geometry of the system constituents, and should be independent of probing technique. The workflow presented here can be generalized for the study of excitations arising when geometry, topology and different materials are used to generate new hybrid optical systems.

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APPENDIX

Appendix A: Correspondence between experimental FTIR and numerically calculated spectra

It is well known that experimentally measured optical spectra strongly depend on exact illumination and collection geometry [51]. In our case, the illumination and collection angles are between 15° and 30° , we however do not know an exact instrument point spread function, which prevents us from perfectly mimicking the experimental setup in the simulations.

Moreover, the collected signal comes from an array of antennas where fabrication imperfections cause averaging over signal from slightly different antenna sizes (estimated size deviation of ~ 10 nm) and maybe more importantly, the antenna edges and surfaces are not perfectly smooth. Our approach thus relies on evaluation of all relevant optical quantities in a standard brightfield illumination geometry, which we then compare with experimentally measured spectra and establish the best correspondence. Fig. 5(a) shows the calculated reflection, absorption and transmission (or more precisely 1-T) spectra, whose spectral shapes strongly resemble scattering, absorption and extinction cross-sections, respectively. The experimentally measured spectra on antenna-SiO₂ layer system are, however, normalized with respect to spectra measured on plain SiO₂ membranes. This "relative" experimental transmission spectrum [orange in Fig. 5(b) and also in Fig. 2(a)] then exhibits a slightly better correspondence with the calculated scattering cross-section [blue line in Fig. 5(b)] compared to calculated relative transmission (green line). Such empirical observation leads us to considering calculated scattering cross-sections for the comparison with relative transmission obtained from FTIR measurements.



FIG. 5. (a) Comparison of theoretically calculated absorption (A, red line), reflection (R, blue line) and 1- transmission (1-T, orange line) spectra for the plane-wave excitation and the geometry considered in Fig. 2. (b) Comparison of "relative" transmission spectra $(1 - T_{\text{rel}})$ obtained by dividing the total transmission spectra by a reference on a plain SiO₂ layer. We show calculated and experimentally measured FTIR spectra (green vs. orange lines) together with calculated scattering cross section (dark blue line).

Appendix B: Finite spectral resolution in EELS

Figure 6 shows a comparison of the theoretical EEL spectra when is convoluted with a Gaussian function of 14 meV FWHM to mimic the energy resolution of the involved STEM-EELS setup.



FIG. 6. Comparison of theoretically calculated EEL spectra after convolution with a Gaussian function of 14 meV FWHM (thin lines) with experimentally measured spectra (thick lines) for the varying beam position as shown in the inset and three antenna's lengths.

Appendix C: Details on fitting

We have used least-square method and fixed parameters within restricted ranges as specified below.

Parameter	Lower bound	Upper bound
$\omega_{\rm SPhP_1} \ ({\rm meV})$	131.9	135.6
$\gamma_{\rm SPhP_1} (\rm meV)$	1	10
$\omega_{\rm SPhP_2} \ ({\rm meV})$	148	154.6
$\gamma_{\rm SPhP_2} \ ({\rm meV})$	2	20
$\omega_{\rm LSP} ({\rm meV})$	80	200
$\gamma_{\rm LSP} \ ({\rm meV})$	1	50
f	1	10
$g_1 \;(\mathrm{meV})$	1	50
$g_2 \text{ (meV)}$	1	50
j_1	-2	3
j_2	-1	1.5

REFERENCES

- J. D. Caldwell, L. Lindsay, V. Giannini, I. Vurgaftman, T. L. Reinecke, S. A. Maier, and O. J. Glembocki, "Lowloss, infrared and terahertz nanophotonics using surface phonon polaritons," Nanophotonics 4, 44–68 (2015).
- [2] M. I. Stockman, "Nanofocusing of optical energy in tapered plasmonic waveguides," Phys. Rev. Lett. 93, 137404 (2004).
- [3] A. J. Huber, B. Deutsch, L. Novotny, and R. Hillenbrand, "Focusing of surface phonon polaritons," Appl. Phys. Lett. 92, 203104 (2008).
- [4] E. Moreno, S. G. Rodrigo, S. I. Bozhevolnyi, L. Martín-Moreno, and F. J. García-Vidal, "Guiding and focusing of electromagnetic fields with wedge plasmon polaritons," Phys. Rev. Lett. **100**, 023901 (2008).
- [5] P. Li, M. Lewin, A. V. Kretinin, J. D. Caldwell, K. S. Novoselov, T. Taniguchi, K. Watanabe, F. Gaussmann, and T. Taubner, "Hyperbolic phonon-polaritons in boron nitride for near-field optical imaging and focusing," Nat. Commun. 6, 1–9 (2015).
- [6] S. Dai, Z. Fei, Q. Ma, A. S. Rodin, M. Wagner, A. S. McLeod, M. K. Liu, W. Gannett, W. Regan, K. Watanabe, T. Taniguchi, M. Thiemens, G. Dominguez, A. H. C. Neto, A. Zettl, F. Keilmann, P. Jarillo-Herrero, M. M. Fogler, and D. N. Basov, "Tunable phonon polaritons in atomically thin van der waals crystals of boron nitride," Science **343**, 1125–1129 (2014).
- [7] G. Spektor, A. David, B. Gjonaj, G. Bartal, and M. Orenstein, "Metafocusing by a metaspiral plasmonic lens," Nano Lett. 15, 5739–5743 (2015).
- [8] M. Autore, P. Li, I. Dolado, F. J. Alfaro-Mozaz, R. Esteban, A. Atxabal, F. Casanova, L. E. Hueso, P. Alonso-González, J. Aizpurua, A. Y. Nikitin, S. Vélez, and R. Hillenbrand, "Boron nitride nanoresonators for phonon-enhanced molecular vibrational spectroscopy at the strong coupling limit," Light Sci. Appl. 7, 17172 (2018).
- [9] U. Hohenester, Nano and Quantum Optics (Springer, 2020).
- [10] E. Prodan, C. Radloff, N. J. Halas, and P. Nordlander, "Hybridization model for the plasmon response of complex nanostructures," Science **302**, 419–422 (2003).
- [11] P. Nordlander, C. Oubre, E. Prodan, K. Li, and M. I. Stockman, "Plasmon hybridizaton in nanoparticle dimers," Nano Lett. 4, 899–903 (2004).
- [12] C. Cherqui, Y. Wu, G. Li, S. C. Quillin, J. A. Busche, N. Thakkar, C. A. West, N. P. Montoni, . D. Rack, J. P. Camden, and D. J. Masiello, "Stem/eels imaging of magnetic hybridization in symmetric and symmetry-broken plasmon oligomer dimers and all-magnetic fano interference," Nano Lett. 16, 6668–6676 (2016).
- [13] S. C. Quillin, C. Cherqui, N. P. Montoni, G. Li, J. P. Camden, and D. J. Masiello, "Imaging plasmon hybridization in metal nanoparticle aggregates with electron energy-loss spectroscopy," J. Phys. Chem. C 120, 20852–20859 (2016).
- [14] A. B. Yankovich, B. Munkhbat, D. G. Baranov, J. Cuadra, E. Olsén, H. Lourenço-Martins, L. H. G. Tizei, M. Kociak, E. Olsson, and T. Shegai, "Visualizing spatial variations of plasmon–exciton polaritons at the nanoscale using electron microscopy," Nano Lett. 19, 8171–8181 (2019).

- [15] K. C. Smith, A. Olafsson, X. Hu, S. C. Quillin, J. C. Idrobo, R. Collette, P. D. Rack, J. P. Camden, and D. J. Masiello, "Direct observation of infrared plasmonic fano antiresonances by a nanoscale electron probe," Phys. Rev. Lett. **123**, 177401 (2019).
- [16] V. Křápek, A. Konečná, M. Horák, F. Ligmajer, M. Stöger-Pollach, M. Hrtoň, J. Babocký, and T. Šikola, "Independent engineering of individual plasmon modes in plasmonic dimers with conductive and capacitive coupling," Nanophotonics 9, 623–632 (2020).
- [17] G. Lu, C. R. Gubbin, J. R. Nolen, T. Folland, M. J. Tadjer, S. De Liberato, and J. D. Caldwell, "Engineering the spectral and spatial dispersion of thermal emission via polariton-phonon strong coupling," Nano Lett. 21, 1831–1838 (2021).
- [18] T. Šikola, R. D. Kekatpure, E. S. Barnard, J. S. White, P. Van Dorpe, L. Břínek, O. Tomanec, J. Zlámal, D. Y. Lei, Y. Sonnefraud, S. A. Maier, J. Humlíček, and M. L. Brongersma, "Mid-IR plasmonic antennas on silicon-rich oxinitride absorbing substrates: Nonlinear scaling of resonance wavelengths with antenna length," Appl. Phys. Lett. **95**, 253109 (2009).
- [19] C. Huck, J. Vogt, T. Neuman, T. Nagao, R. Hillenbrand, J. Aizpurua, A. Pucci, and F. Neubrech, "Strong coupling between phonon-polaritons and plasmonic nanorods," Opt. Express 24, 25528–25539 (2016).
- [20] P. Pons-Valencia, F. J. Alfaro-Mozaz, M. M. Wiecha, V. Biolek, I. Dolado, S. Vélez, P. Li, P. Alonso-González, F. Casanova, L. E. Hueso, L. Martín-Moreno, R. Hillenbrand, and A. Y. Nikitin, "Launching of hyperbolic phonon-polaritons in h-BN slabs by resonant metal plasmonic antennas," Nat. Commun. 10, 1–8 (2019).
- [21] L. Břínek, M. Kvapil, T. Šamořil, M. Hrtoň, R. Kalousek, V. Křápek, J. Spousta, P. Dub, P. Varga, and T. Šikola, "Plasmon resonances of mid-IR antennas on absorbing substrate: Optimization of localized plasmon-enhanced absorption upon strong coupling effect," ACS Photonics 5, 4378–4385 (2018).
- [22] R. Hillenbrand, T. Taubner, and F. Keilmann, "Phononenhanced light-matter interaction at the nanometer scale," Nature 418, 159–162 (2002).
- [23] O. L. Krivanek, T. C. Lovejoy, N. Dellby, T. Aoki, R. W. Carpenter, P. Rez, E. Soignard, J. Zhu, P. E. Batson, M. J. Lagos, R. F. Egerton, and P. A. Crozier, "Vibrational spectroscopy in the electron microscope," Nature 514, 209–214 (2014).
- [24] R. F. Egerton, Electron Energy-loss Spectroscopy in the Electron Microscope (Plenum Press, New York, 1996).
- [25] M. J. Lagos, A. Trügler, U. Hohenester, and P. E. Batson, "Mapping vibrational surface and bulk modes in a single nanocube," Nature 543, 529–532 (2017).
- [26] A. A. Govyadinov, A. Konečná, A. Chuvilin, S. Vélez, I. Dolado, A. Y. Nikitin, S. Lopatin, F. Casanova, L. E. Hueso, J. Aizpurua, and R. Hillenbrand, "Probing lowenergy hyperbolic polaritons in van der waals crystals with an electron microscope," Nat. Commun. 8, 1–10 (2017).
- [27] A. Konečná, K. Venkatraman, K. March, P. A. Crozier, R. Hillenbrand, P. Rez, and J. Aizpurua, "Vibrational electron energy loss spectroscopy in truncated dielectric slabs," Phys. Rev. B 98, 205409 (2018).
- [28] L. H. G. Tizei, V. Mkhitaryan, H. Lourenço-Martins, L. Scarabelli, K. Watanabe, T. Taniguchi, M. Tencé, J. D. Blazit, X. Li, A. Gloter, A. Zobelli, F. P. Schmidt,

L. M. Liz-Marzán, F. J. García de Abajo, O. Stéphan, and M. Kociak, "Tailored nanoscale plasmon-enhanced vibrational electron spectroscopy," Nano Lett. **20**, 2973– 2979 (2020).

- [29] H. Yang, E. L. Garfunkel, and P. E. Batson, "Probing free carrier plasmons in doped semiconductors using spatially resolved electron energy loss spectroscopy," Phys. Rev. B 102, 205427 (2020).
- [30] N. Li, X. Guo, X. Yang, R. Qi, T. Qiao, Y. Li, R. Shi, Y. Li, K. Liu, Z. Xu, L. Liu, F. J. García de Abajo, Q. Dai, E.-G. Wang, and P. Gao, "Direct observation of highly confined phonon polaritons in suspended monolayer hexagonal boron nitride," Nat. Mater. 20, 43–48 (2020).
- [31] A. Konečná, J. Li, J. H. Edgar, F. J. García de Abajo, and J. A. Hachtel, "Revealing nanoscale confinement effects on hyperbolic phonon polaritons with an electron beam," Small 17, 2103404 (2021).
- [32] M. J. Lagos, P. E. Batson, Z. Lyu, and U. Hohenester, "Imaging strongly coupled plasmon-phonon modes in mid-infrared double antennas," ACS Photonics 8, 1293– 1300 (2021).
- [33] "Ansys Lumerical inc." www.lumerical.com.
- [34] "Comsol Multiphysics," www.comsol.com.
- [35] F. J. García de Abajo, "Optical excitations in electron microscopy," Rev. Mod. Phys. 82, 209–275 (2010).
- [36] J. A Hachtel, A. R. Lupini, and J. C. Idrobo, "Exploring the capabilities of monochromated electron energy loss spectroscopy in the infrared regime," Sci. Rep. 8, 5637 (2018).
- [37] T. Lovejoy, G. Corbin, N. Dellby, M. Hoffman, and O. L. Krivanek, "Advances in ultra-high energy resolution stem-eels." Microsc. Microanal. 24, 446–447 (2018).
- [38] J. Kischkat, S. Peters, B. Gruska, M. Semtsiv, M. Chashnikova, M. Klinkmüller, O. Fedosenko, S. Machulik, A. Aleksandrova, G. Monastyrskyi, Y. Flores, and W. T. Masselink, "Mid-infrared optical properties of thin films of aluminum oxide, titanium dioxide, silicon dioxide, aluminum nitride, and silicon nitride," Appl. Opt. 51, 6789– 6798 (2012).
- [39] E. D. Palik, Handbook of Optical Constants of Solids (Academic Press, San Diego, 1985).
- [40] R. Fuchs and K. L. Kliewer, "Optical modes of vibration in an ionic crystal slab," Phys. Rev. 140, A2076–A2088

(1965).

- [41] K. Venkatraman, P. Rez, K. March, and P. A Crozier, "The influence of surfaces and interfaces on high spatial resolution vibrational EELS from SiO2," Microscopy 67, i14–i23 (2018).
- [42] Y.-H. Li, M. Wu, R.-S. Qi, N. Li, Y.-W. Sun, C.-L. Shi, X.-T. Zhu, J.-D. Guo, D.-P. Yu, and P. Gao, "Probing lattice vibrations at SiO2/Si surface and interface with nanometer resolution," Chin. Phys. Lett. 36, 026801 (2019).
- [43] A. A. Lucas and E. Kartheuser, "Energy-loss spectrum of fast electrons in a dielectric slab. i. nonretarded losses and cherenkov bulk loss," Phys. Rev. B 1, 3588–3598 (1970).
- [44] D. Rossouw, M. Couillard, J. Vickery, E. Kumacheva, and G. A. Botton, "Multipolar plasmonic resonances in silver nanowire antennas imaged with a subnanometer electron probe," Nano Lett. **11**, 1499–1504 (2011).
- [45] A. Konečná, T. Neuman, J. Aizpurua, and R. Hillenbrand, "Surface-enhanced molecular electron energy loss spectroscopy," ACS Nano 12, 4775–4786 (2018).
- [46] S. Albaladejo, R. Gómez-Medina, L. S. Froufe-Pérez, H. Marinchio, R. Carminati, J. F. Torrado, G. Armelles, A. García-Martín, and J. J. Sáenz, "Radiative corrections to the polarizability tensor of an electrically small anisotropic dielectric particle," Opt. Express 18, 3556– 3567 (2010).
- [47] E. Castanié, R. Vincent, R. Pierrat, and R. Carminati, "Absorption by an optical dipole antenna in a structured environment," Int. J. Opt. **2012**, 452047 (2012).
- [48] L. Novotny, "Strong coupling, energy splitting, and level crossings: A classical perspective," Am. J. Phys. 78, 1199–1202 (2010).
- [49] Y. Wu, Z. Hu, X.-T. Kong, J. C. Idrobo, A. G. Nixon, P. D. Rack, D. J. Masiello, and J. P. Camden, "Infrared plasmonics: STEM-EELS characterization of Fabry-Pérot resonance damping in gold nanowires," Phys. Rev. B 101, 085409 (2020).
- [50] P. Törmä and W. L. Barnes, "Strong coupling between surface plasmon polaritons and emitters: a review," Rep. Prog. Phys. 78, 013901 (2014).
- [51] M. W. Knight, J. Fan, F. Capasso, and N. J. Halas, "Influence of excitation and collection geometry on the dark field spectra of individual plasmonic nanostructures," Opt. Express 18, 2579–2587 (2010).