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Multipolar Resonances with Designer Tunability Using VO$_2$ Phase-Change Materials

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Subwavelength nanoparticles can support electromagnetic resonances with distinct features depending on their size, shape and nature. For example, electric and magnetic Mie resonances occur in dielectric particles, while plasmonic resonances appear in metals. Here, we experimentally demonstrate that the multipolar resonances hosted by VO$_2$ nanocrystals can be dynamically tuned and switched thanks to the insulator-to-metal transition of VO$_2$. Using both Mie theory and Maxwell Garnett effective medium theory, we retrieve the complex refractive index of the effective medium composed of a slab of VO$_2$ nanospheres embedded in SiO$_2$ and show that such a resulting metamaterial presents distinct optical tunability compared to unpatterned VO$_2$. We further show that this approach provides a new degree of freedom to design low-loss phase-change metamaterials with record large figure of merit ($\Delta n/\Delta k$) and designer optical tunability.

I. INTRODUCTION

The potential of nanophotonics for tailoring light-matter interaction at the nanoscale has attracted considerable interest in recent years [1–3]. For example, metasurfaces enable an ultimate control of light fields thanks to abrupt phase modifications using engineered nanoscale elements [4, 5]. A wealth of nano-fabrication techniques are readily available to produce nanoscale elements with specific shapes, sizes and nature. Thanks to these technological developments, light scattering by spherical nanoparticles revealed exciting optical phenomena such as strong localized optical resonances, directional scattering or light emission control [6–9]. However, the dimensions of these nano-resonators, and the scale of nanophotonic devices make them difficult to be tuned and reconfigured. So in essence most of nanophotonic devices are static devices. It is therefore currently a great challenge to find efficient means to dynamically tune photonic devices at the nanoscale [10, 11].

Recently, a large number of researches make use of phase-change materials (PCM) to tune photonic devices. Although a large variety of PCMs exist, most of the works exploit the tunable properties of either VO$_2$ or GeSbTe [12–15]. In the standard visible (Vis) and near-infrared (NIR) ranges, these materials typically have large refractive index modulation but also large extinction coefficients. So far, it has proven difficult to circumvent this extinction coefficient, which translates into net optical losses in photonic devices. One interesting approach to modify the intrinsic properties of these materials is to locally arrange or modify them by patterning, doping or straining. These strategies were recently used to demonstrate phase modulation [16], tunable optical absorption [17, 18] or switchable dielectric-plasmonic regimes [19]. A particularly promising method is to reduce the dimensions of VO$_2$ down to the nanoscale. This approach is not only interesting for gaining theoretical insights into the fundamentals of the Insulator-to-Metal Transition (IMT) of VO$_2$ [20] but also to tailor the physical properties of this strongly correlated system. The first works on synthesis and characterization of VO$_2$ nanocrystals (NCs) were reported in 2002 [21, 22], followed by studies on their nonlinear optical properties [23] and their potential for ultra-fast modulation of optical transmission [24]. Recent works report various methods of fabrication of VO$_2$ nanocrystals and their use as thermochromic smart windows [25, 26], differentially-doped multilayer VO$_2$ films [27], electrochemically-induced transformations [28] or dynamical reconfiguration of optical devices [29–31].

Here, we show that an ensemble of VO$_2$ nanospheres support multipolar resonances and can be homogenized as a tunable effective medium metamaterial whose optical properties and tunability are adjustable by design. Specifically, we exploit a Mie theory-based extension of Maxwell-Garnett effective medium approximation to precisely explain the light-matter interactions at play in VO$_2$-NCs and decompose it into multipolar modes. These multipolar resonances are both dynamically tunable through the IMT of VO$_2$ and adjustable via controlling the size of the particles. VO$_2$-NCs is therefore a tunable metamaterial platform whose properties can both be engineered through fabrication (size and density of VO$_2$-NCs) and actively tunable by external excitations (switching from insulator to metal). But more importantly, we show in the following that this metamaterial approach enables designing tunable composite metamaterials presenting a refractive index modulation without induced extinction, or in other words a zero-induced extinction phase-change metamaterial.

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II. OPTICAL PROPERTIES OF VO$_2$ THIN-FILMS

VO$_2$ is a strongly correlated material that is dielectric at room temperature and becomes metallic when heated above 68°C. According to band theory and given its crystallography, it should be metallic even at room temperature, but electron-electron correlations freeze the potential free carriers on their respective sites (Mott localisation) [32–34]. Upon the transition, several interrelated physical processes occur: the crystallographic lattice changes from monoclinic to tetragonal (Peierls distortion), hence modifying the band structure and “liberating” free carriers. VO$_2$ therefore undergoes large changes in its electrical properties and its band structure, what translates into large modulation of its optical properties.

We have investigated the optical properties of a thin layer of VO$_2$ across the IMT using spectroscopic ellipsometry combined with a heat cell (more details in the experimental section and supplementary information [35]). Thanks to a physically consistent optical model (more details in the supplementary [35]), we have extracted the dielectric function of VO$_2$ as a function of temperature. In Figure 1, we show the complex optical permittivity of VO$_2$ upon phase-change. As displayed in the figure, we see very large modifications of both the real ($\epsilon_1$) and imaginary parts ($\epsilon_2$) of the permittivity upon the IMT of VO$_2$.

The extraordinary feature of VO$_2$ is the strong modulation of its electric permittivity, which is as large as $\Delta \epsilon \sim 20$ in the near-infrared range. But, as explained previously, this modulation is accompanied by an intrinsic very large increase of the optical absorption, which dominates the optical response in the infrared range [45, 46]. Given this large absorption, VO$_2$ is therefore often used as an on-off switch and little to no works actually make use of its refractive index tunability.

III. VO$_2$ NANOCRYSTALS

When an object is illuminated by an electromagnetic wave, it reradiates parts of the energy while being lost from the original wave. This phenomenon is known as scattering. The quantity and direction of light that is scattered depend on the nature, shape and size of the object [47]. The problem becomes substantially more complex when the size of the object approaches the wavelength of the incident wave. In that situation, we can no longer assume the field to be constant in the object and the so-called “long-wavelength approximation” no longer holds, so retardation effects must be considered. To compute the scattered field, one needs a numerical approach for an arbitrary object. Such a complex problem can however be simplified if the object is a sphere. In 1908, Mie found an exact solution to that problem, by calculating the scattered field as a series solution [48]. The general idea is to expand the electric and magnetic fields in vector spherical harmonics. The field functions are then linear combinations of terms that are products of separable functions of the three spherical coordinates. The electromagnetic interaction of light with spheres can then be modeled following the Lorenz-Mie formalism for scattering and absorption of light by small particles [49]. Within this formalism, the extinction, scattering and absorption efficiencies are given by:

$$Q_{ext} = \frac{2}{x^2} \sum_{n=1}^{\infty} (2n+1) Re(a_n + b_n)$$

$$Q_{sca} = \frac{2}{x^2} \sum_{n=1}^{\infty} (2n+1)(|a_n|^2 + |b_n|^2)$$

$$Q_{abs} = Q_{ext} - Q_{sca}$$

where $a_n$ and $b_n$ are the so-called scattering coefficients [49]. These depend on both the particle optical properties (relative to its surrounding medium) and size. The size parameter $x$ is defined as $x = \frac{2\pi m_{med} R}{\lambda}$ where $m_{med}$ is the refractive index of the surrounding medium, $\lambda$ the wavelength of the incident light in vacuum and $R$ the sphere’s radius. Physically, $a_n$ and $b_n$ are the weighting factors of the different excited electric and magnetic multipolar contributions. For instance, $a_1$ and $b_1$ represent the electric and magnetic dipolar modes, and $a_2$ and
$b_2$ correspond to the electric and magnetic quadrupolar modes, respectively.

Figure 2 shows the absorption cross section $Q_{abs}$ of a VO$_2$ sphere of radius 50 nm in its insulating and metallic states embedded in quartz ( $m_{med} = 1.45$ for $\lambda = 1 \mu m$ [50]). With colored lines, dipolar electric $a_1$, dipolar magnetic $b_1$, quadrupolar electric $a_2$ and quadrupolar magnetic $b_2$ contributions to $Q_{abs}$ are represented. It can be seen that, regardless of the state of VO$_2$, below 700 nm the electromagnetic response is dominated by the dipolar electric (DE) and magnetic response (DM), with a small contribution of the quadrupolar electric term (QE). These resonances correspond to Whispering Gallery Modes (WGM, $\text{Re}(\epsilon) > 0$) which resonate at the suitable wavelengths, the magnetic resonance redshifted with respect to the electric one [8]. On the other hand, when VO$_2$ is in its metallic phase ( $\text{Re}(\epsilon) < 0$), a DE-localized surface plasmon resonance (LSPR) appears at a longer wavelength (1015 nm). The higher the temperature and consequently, with increasing metallic character, the more intense this resonance is. This resonance is plasmonic and its physical origin is the negative value of the dielectric constant above 1000 nm in the metallic phase.

![Figure 2](image)

**Figure 2.** Calculated absorption efficiency of VO$_2$ spheres with radius 50 nm in its a) insulating and b) metallic states embedded in quartz. With colored lines are represented the dipolar electric $a_1$ (red), dipolar magnetic $b_1$ (yellow), quadrupolar electric $a_2$ (light blue) and quadrupolar magnetic $b_2$ (dark blue) contributions to $Q_{abs}$.

An ensemble of VO$_2$ nanospheres would therefore enable a dynamic tuning of multipolar resonances together with their coherent effects for directionality purposes [51] and to actively control the presence and intensity of a plasmonic mode in the NIR.

**IV. FABRICATION AND OPTICAL CHARACTERIZATION**

The synthesis of a dense layer of isolated VO$_2$ nanocrystals embedded in about 100 nm depth below the surface begins with a high fluence ion implantation of V$^+$ and O$^+$ with energies of 100 keV and 36 keV, respectively. These energies were chosen to produce overlapping concentration depth profiles of the elements. The formation of the VO$_2$ chemical compound was controlled by the fluence ratio of V to O (i.e. $8 \times 10^{16}$ cm$^{-2}$ to $1.6 \times 10^{17}$ cm$^{-2}$ and $4 \times 10^{16}$ cm$^{-2}$ to $8 \times 10^{16}$ cm$^{-2}$ for a ratio of 1:2). Then, ion implantation nanocrystal growth was initiated by a rapid thermal annealing (RTA) step at 1000°C for 10 min in an inert gas at atmospheric pressure. After these steps, spherical VO$_2$-NCs are formed, embedded below the surface (for more details, see e.g. [30]). As verified by TEM analysis (see Fig. 3a), the produced sample contains an ensemble of VO$_2$ nanospheres that are close to be perfectly spherical [31].

Unpatterned VO$_2$ thin-films were fabricated as follows: 25 nm VO$_2$ was deposited on quartz substrate by magnetron sputtering. A V$_2$O$_5$ target was sputtered at a power of 100 W radio frequency. During deposition, the substrate was maintained at 750°C; the pressure of chamber was kept as 5 mtorr with flowing of 49.5 sccm Ar and 0.5 sccm 10% Ar-balanced oxygen gases.

Following the depositions, the analysis of the complex dielectric functions of all the samples of VO$_2$ (both NCs and thin-films) were carried out using a variable-angle spectroscopic ellipsometer (UVISEL Horiba Jobin-Yvon). The incident broadband light source (Xenon) was polarized at 45°. After reflection off the sample under study, the light is directed to a spectrometer, dispersed by appropriate gratings and measured with UV/Vis and NIR detectors. In the case of phase-modulated ellipsometry, like the one we use, we do not measure the ellipsometric angles $\Psi$ and $\Delta$ directly. Instead, we measure $I_s$ and $I_c$ which, under our measurements conditions, are defined as: $I_s = \text{sin}(2\Psi)\text{sin}(\Delta)$ and $I_c = \text{sin}(2\Psi)\text{cos}(\Delta)$. The acquired ellipsometric parameters $I_s$ and $I_c$ of the samples have been collected for varying angles 55° - 70° over a spectral range of 260 - 2100 nm. The complex dielectric functions of samples and their thicknesses can be derived by fitting realistic optical models to these experimental data (more details in the supplementary information [35]). To analyze temperature-dependent optical properties, the acquisitions were carried out in a range of temperatures from 30°C to 80°C using a digitally controlled heat cell (Linkam THMSEL350V).

In the following, we present our ellipsometric measurements and analysis via these functions $I_s$ and $I_c$, that are directly related to the usual ellipsometry angles $\Psi$ and $\Delta$. Figures 3b-c show the evolution of the $I_s$ and $I_c$ parameters of ellipsometry measurements as a function of temperature, the effect of the IMT of VO$_2$-NCs is clearly observable on the raw ellipsometry measurements, with the appearance of a large peak in $I_s$ whose intensity progressively increases around 1100 nm. This phenomenon is reversible, with a broad hysteresis behavior (more details in the supplementary information [35]), and is a clear signature of the presence of stoichiometric VO$_2$ in the sample.
V. RETRIEVAL OF THE EFFECTIVE PARAMETERS OF THE METAMATERIAL.

We now want to retrieve the effective permittivity of the active layer containing VO$_2$-NCs. From previous TEM analysis [31], we know that the VO$_2$-NCs medium is a single-plane of NCs that are spaced by a few tens of nanometers. In order to model the optical response of the slab composed of VO$_2$-NCs embedded in quartz, we have calculated its effective refractive index $n_{eff}$ using a Mie theory-based extension of Maxwell Garnett effective medium approximation (EMA), as proposed by Doyle [52]. Using this approach, we can calculate an effective electric permittivity ($\epsilon_{eff}$) and magnetic permeability ($\mu_{eff}$) that are directly governed by the Mie dipolar electric $a_1$ and magnetic $b_1$ dipolar coefficients respectively. In this way, we take into account size effects that are ignored by the electrostatic approximation which is the base of conventional Maxwell Garnett EMA. The dipolar coefficients are enough to model the response of the VO$_2$ particles since the quadrupolar terms are negligible as seen in Figure 1. Therefore, $\epsilon_{eff}$ and $\mu_{eff}$ can be written as

$$\epsilon_{eff} = \frac{x^3 + 3ia_1}{x^3 - \frac{3}{2}ia_1}$$  \hspace{1cm} (4)$$

$$\mu_{eff} = \frac{x^3 + 3ib_1}{x^3 - \frac{3}{2}ib_1}$$ \hspace{1cm} (5)
Figure 4. a) Effective dielectric function ($\epsilon_{\text{eff}}$), b) magnetic permeability ($\mu_{\text{eff}}$), and c) real and d) imaginary parts of the effective refractive index ($m_{\text{eff}} = n_{\text{eff}} + ik_{\text{eff}}$) of a slab of quartz with VO$_2$ spheres with radius $R = 35$ nm and a filling fraction $f = 0.18$ in their insulating (low temperature) and metallic (high temperature) states.

where $x$ is the size parameter of the VO$_2$ spheres and $f$ the volume filling fraction of the VO$_2$ spheres in the slab (the complete derivation for eqs. (4) and (5) can be found in the supplementary [35]). From the values of $\epsilon_{\text{eff}}$ and $\mu_{\text{eff}}$ the effective complex refractive index of the slab can be calculated as

$$m_{\text{eff}} = n_{\text{eff}} + ik_{\text{eff}} = \sqrt{\epsilon_{\text{eff}} \mu_{\text{eff}}}$$(6)

In the following, we fit the experimental ellipsometry measurements with a multi-layer model composed of four layers as sketched in Figure 3a: (i) a thin SiO$_2$ layer, (ii) the VO$_2$-NCs + SiO$_2$ effective layer, (iii) an intermediate layer containing vanadium inclusions and impurities and (iv) a semi-infinite SiO$_2$ substrate. This four-layer model is justified by transmission electron microscopy (TEM) observations of the sample’s cross sections. Indeed, from previous TEM analysis on similar samples, we know that the implantation process of V$^+$ and O$^+$ ions produces a layer of almost perfectly spherical VO$_2$ nanocrystals (layer #2), but also another layer below containing very small (<10nm) metallic Vanadium inclusions (layer #3), as found by elemental composition measurements [53]. We use a reference dispersion file for SiO$_2$ (Palik [54]). The respective thicknesses of SiO$_2$ top layer, VO$_2$-NC layer and V inclusion layer are set as free fit parameters. None of the material’s dispersion are fit, rather we modify the size and density of VO$_2$-NCs in our Mie-Maxwell Garnett model to adjust the fits to the measurements. Thin partially absorbing films are known to present correlations between thickness and dispersion, what make the ellipsometry analysis difficult. Interestingly, this situation gets manageable when measuring thin-films of PCMs: their optical dispersion is modulated across the change of phase, while their thickness remains the same (this is especially true for VO$_2$, for which there is no change of thickness upon the insulator to metal transition). This phenomenon was previously used to find unique solutions for the ellipsometry fit of thin-films of VO$_2$ [46]. We followed the same method for our VO$_2$-NC layer: to break the correlations between thickness and complex refractive index, we simultaneously fit the ellipsometry measurements of VO$_2$-NCs in both their insulating and metallic state and we force the final fitted thickness to converge towards the same value in both states of VO$_2$. In other words, the final fit will yield the same thicknesses for the different layers whatever the phase of VO$_2$-NCs. The only difference between the two models for VO$_2$ insulating and metallic lies in the dispersion of VO$_2$-NCs.

In Figure 3d-e, we show the optimized fits together with the experimental data. We obtain an overall good correspondence between model and measurements for a VO$_2$-NCs size of $R = 35$nm and a filling-factor $f = 0.18$. 
Based on our different fits to the experimental measurements, we can give an estimated uncertainty for the extracted values for the sizes and filling-factor of VO\textsubscript{2}-NCs to about 5\%. If we round up this number, the extracted values with their associated uncertainties are $R = 35$ nm $\pm 2$ nm and $f = 0.18 \pm 0.01$.

The fits are nearly perfect in the UV/Vis range but a slight discrepancy appears in the NIR. The observed discrepancy in 3d-e between the model and the experimental results is due to different effects which cannot be included without losing simplicity in the proposed model. The two most important are the electromagnetic interaction between the particles and a potentially non-negligible degree of polydispersity in the size distribution of the VO\textsubscript{2}-NCs. The electromagnetic interaction between nanoparticles has a long standing history and a nice work on this effect can be found in Rechberger et al. [55]. We have applied the results of this research to our case and the details can be found in the supplementary information [35]. Here, we have considered the experimental conditions used in the ellipsometry measurements with an exciting beam linearly polarized at 45\° with respect to the incidence plane. In the metallic phase, the pure plasmonic resonance is affected by blue and red shifts due to the interparticle electromagnetic interaction with a clear net red shift of this resonance. This would explain the apparent discrepancy observed between the measured spectral position of the plasmonic peak around 1000 nm and that predicted with our model where multiple interactions are not included. Concerning the insulating phase, its resonance is clearly less influenced by electromagnetic interaction between the particles. It is important to point out that this resonance is composed mainly of two dipolar ones (see Figure 1) of electric and magnetic character, respectively. As it is shown in the supplementary information [35], due to the particle interaction, there is a competition between the blue shift undergone by the magnetic contribution and the red shift for the electric one [56]. The net result is a slight blue shift of the whole resonance when the interparticle gap is small. This is the small discrepancy we observe in Figure 3 when the experiment and the model result are compared for the resonance at 380 nm.

Concerning polydispersity, some detailed calculations have been included in the supplementary information [35] but the main conclusion is that, assuming an asymmetric size distribution, the net effect would be a general red-shift and broadening of the resonance peak, especially for those resonances of low energy (long wavelengths) and associated to the metallic phase which are more sensitive to changes in the morphology and optical properties of the VO\textsubscript{2} nanoscaters.

Other effects can also present minor contributions to the discrepancies observed in Figure 3d-e. Indeed, we approximate VO\textsubscript{2}-NCs as composed of purely stoichiometric VO\textsubscript{2} and we neglected the presence of suboxides such as V\textsubscript{2}O\textsubscript{5} at the NCs surface. Furthermore, we directly used the dispersion as extracted from VO\textsubscript{2} thin films measurements to compute the different Mie coefficients. By doing so, we made the hypothesis that the complex permittivity of VO\textsubscript{2} inside the NCs has the exact same dispersion as VO\textsubscript{2} thin films, what could be subject to discussions [20].

Even though we have made all these approximations and neglected potential interactions in the fits, we find a remarkably good qualitative agreement between measurements and calculations. Furthermore, this good agreement holds for all angles of incidence used in this study (55\°-70\°). We emphasize that this simple model is able to reproduce well the prominent features of the optical response for both states of VO\textsubscript{2} by simply changing the dispersion of VO\textsubscript{2} from insulating to metallic. Indeed, the calculations nicely reproduce the first peak in the visible, which is a combination of electric and magnetic dipole resonances and the second peak in the NIR which is a plasmonic resonance. This latter is only present when the VO\textsubscript{2} is metallic, e.g. when the real part of the permittivity is negative and is therefore a dynamically tunable resonance.

These calculations enable us to retrieve the effective permittivity of the active VO\textsubscript{2}-NCs layer and homogenize it as an effective metamaterial medium. Figure 4a-d shows the calculated $\epsilon_\text{eff}$, $\mu_\text{eff}$ and $m_\text{eff}$ for a slab with VO\textsubscript{2} spheres with radius $R = 35$ nm and a filling fraction $f = 0.18$ in their insulating (low temperature) and metallic (high temperature) states. These retrieved $\epsilon_\text{eff}$ and $\mu_\text{eff}$ values are effective angle-independent metamaterial parameters, describing the global optical properties of the hybrid medium.

We see clear differences in the optical dispersion as compared to un-patterned VO\textsubscript{2} layer. In particular, there are ranges of wavelength for which the IMT of VO\textsubscript{2} produces a large modulation of $n_\text{eff}$ with a simultaneously low $k_\text{eff}$ that is much lower than in bulk VO\textsubscript{2}. This is especially true in the NIR, for which $k_\text{eff}$ remains lower than 0.1.

**VI. DISCUSSION**

We have shown that the main spectral characteristics of VO\textsubscript{2}-NC based metamaterials can be calculated using a combination of Mie theory and Maxwell Garnett effective medium. From there, we can now predict the expected optical properties of VO\textsubscript{2}-NCs of arbitrary sizes. In the following, we show how this framework can be used to design tunable metamaterials with tailored properties in desired wavelength ranges. Figure 5a-d shows the calculated evolution of the $n_\text{eff}$ and $k_\text{eff}$ values of VO\textsubscript{2}-NCs in both their insulating and metallic states for different diameters of NCs.

In the insulating state, the absorption peaks are controlled by the Mie resonances while in the metallic state they are dominated by the plasmonic resonance. We can directly see that, by adjusting the size of NCs, we control the spectral position of the absorption peaks in both the insulating and metallic states (see figure 5b) and (d). The size of the VO\textsubscript{2}-NCs therefore enables tailoring the
Figure 5. Variation of effective optical parameters for different sizes of nanocrystals in both states of VO$_2$ a) and b) $n_{eff}$ and $k_{eff}$ for insulating VO$_2$ with a filling fraction $f = 0.18$. c) and d) $n_{eff}$ and $k_{eff}$ for metallic VO$_2$. e) and f) represent the amplitude of modulation of the effective refractive index of the metamaterial as a function of NCs size. e) $\Delta n_{eff}$ and f) $\Delta k_{eff}$.

spectral distribution of the multipolar resonances hosted by this metamaterial.

To have a more general picture of the different regimes of tunability we can obtain with this system, Figure 5e-f displays the amplitude of refractive index modulation produced by the IMT of VO$_2$ as a function of NCs size. To do so, we plot $\Delta n_{eff}$ and $\Delta k_{eff}$, which are defined as $\Delta n_{eff} = n_{eff,\text{insulating}} - n_{eff,\text{metallic}}$ and $\Delta k_{eff} = k_{eff,\text{insulating}} - k_{eff,\text{metallic}}$ and which represent the amplitude of modulation of the effective refractive index and extinction coefficient, respectively. With this figure, we can pinpoint specific regions of the size versus wavelength map in which the switching of VO$_2$ either translates into a tunable refractive index or a tunable extinction coefficient.

Interestingly, by plotting the $\Delta n_{eff}$ and $\Delta k_{eff}$ values calculated for a few selected VO$_2$-NCs sizes (as displayed in Figure 6), we immediately see that around the maxi-
maximum $\Delta n_{eff}$ reached for each NCs size, we simultaneously have $\Delta k_{eff}=0$. Furthermore, the wavelength at which this effect is obtained is directly governed by the size of VO$_2$-NCs. In other words, this phase-change metamaterial platform enables tailoring a dynamical tuning of refractive index without modifying the optical absorption. As displayed in Figure 6, this ‘zero-induced-extinction’ refractive index tuning occur in a designer wavelength range via selecting an appropriate size of NCs.

By plotting the figure of merit (FOM) $\Delta n_{eff}/\Delta k_{eff}$ for different sizes of NCs and comparing the obtained FOM to the corresponding one for VO$_2$ thin films, we immediately see that not only the FOM is enhanced by more than two orders of magnitude but we can design the system to select the wavelength at which the FOM is boosted via the size of VO$_2$-NCs. This designer high FOM is much larger than in any other existing ‘unpatterned’ PCMs [57], and highlights the usefulness of our metamaterial approach. We also note that the opposite effect can be exploited, namely, close to the maximum $\Delta k_{eff}$, we can simultaneously have negligible $\Delta n_{eff}$. So this platform can be used to actively control the absorption without modifying the refractive index of the medium (e.g. for $R=95\text{nm}$ at $\lambda=1500\text{nm}$ we get $\Delta k_{eff}=-0.2$ and $\Delta n_{eff}=0$).

We envision another exciting opportunity for this metamaterial as an active platform to control scattering properties and directional beaming of light. Indeed, when multipolar resonances are spectrally overlapping in nanoparticles, the scattered fields can interfere and produce directional scattering. In particular, spectrally overlapping DE and DM resonances yield the so-called Kerker conditions that either suppress the forward or the backward scattering of light [8, 58]. Figure 7 displays the multipolar decomposition of light fields within VO$_2$-NCs as a function of size and VO$_2$ phase, either insulating or metallic. We see that each size of NCs produces overlapping DE and DM resonances which coherently interfere at specific wavelengths. Then, when the VO$_2$ is switched from its insulating phase to the metallic one, we can suppress the DM contribution associated to the $b_1$ coefficient and strongly enhance the DE contribution associated to the $a_1$ coefficient.

In other words, at specific wavelengths we switch from a dielectric DM resonances to a plasmonic DE resonance. This implies that this hybrid metamaterial enables an active and dynamical control of the Kerker conditions [58]. From that perspective, we foresee a dynamic modulation of the directionality of light scattering as well as actively tunable perfect reflection or absorption. We also note the presence of tunable quadrupolar modes ($a_2$ and $b_2$ coefficients, figure 7) that may be used for complex tunable interference phenomena between different multipoles, hence opening a wealth of different possibilities of spatially distributing the scattered light for directionality control purposes (see [51, 59] for more details). This tunable multipoles could also find an interest in the recently proposed framework of spontaneous emission engineer-

![Figure 6. Spectral variation of the amplitude of modulation of the effective refractive index ($\Delta n_{eff}$ and $\Delta k_{eff}$) of the metamaterial for selected NCs size. Bottom graph: Figure of Merit (FOM=$\Delta n_{eff}/\Delta k_{eff}$) of the VO$_2$-NCs platform for different sizes of nanocrystals and compared to the FOM for a VO$_2$ thin-film.](image)

**VII. CONCLUSION**

We have demonstrated that VO$_2$-NCs integrated in SiO$_2$ as spherical nano-inclusions enable exploiting the VO$_2$ IMT to tune and switch multipolar modes in the visible and near-infrared ranges. In particular, we showed the presence of a plasmonic mode in the NIR whose gradual appearance and intensity are directly controlled by the VO$_2$ state. The presence of two simultaneous dipole resonances in two different spectral regions, Vis and NIR, could open the possibility of new “multiplexing” based techniques for SERS applications. Contrary to bulk and thin-films VO$_2$, such a metamaterial approach provides means to tailor the complex refractive index and tunability of phase-change materials. Indeed, we have shown that, by adjusting the VO$_2$-NCs size, this system can be exploited as a designer phase-change metamaterial with adjustable refractive index modulation and absorption modulation. Especially, we can design the system to have a large refractive index tunability without inducing modulation of the extinction coefficient at specific wavelengths. This zero-induced-extinction refractive in-

**FIGURE 6**

- **Spectral variation of the amplitude of modulation of the effective refractive index ($\Delta n_{eff}$ and $\Delta k_{eff}$) of the metamaterial for selected NCs size.**
- **Bottom graph:** Figure of Merit (FOM=$\Delta n_{eff}/\Delta k_{eff}$) of the VO$_2$-NCs platform for different sizes of nanocrystals and compared to the FOM for a VO$_2$ thin-film.
Figure 7. Calculated absorption cross-section efficiency $Q_{abs}$ of NCs of different sizes in their insulator and metallic states embedded in quartz. With colored lines are represented the dipolar electric $a_1$ (red), dipolar magnetic $b_1$ (yellow), quadrupolar electric $a_2$ (light blue) and quadrupolar magnetic $b_2$ (dark blue) contributions to $Q_{abs}$.

dex tuning opens up new regimes of very large FOM that are unattainable with conventional unpatterned PCMs layers. Furthermore, such VO$_2$-NCs can be optically switched at femtoseconds timescale (~150 fs) [24] and present very large hysteresis (see [30] and the supplementary information [35]). We can therefore envision this platform to be used for ultra-fast all-optical integrated systems with memory effects. Note however that the speed of modulation will ultimately be limited by the fall times for VO$_2$ devices, which typically depends on device dimensions, thermal dissipation, ambient temperature, and actuation mechanism [61, 62]. Reaching the sub-nanosecond regime will require optimizing the optical and thermal environment of nanostructures for heat management.

Compared to other methods of nanopatterning PCMs, we emphasize that the resulting metamaterial presents several benefits from a practical point of view, and most notably the nanostructures are embedded in a dielectric host that protects them from the environment and consequent processes that can affect its optical response (protection from oxidization [63], chemical reaction [64], mechanical scratches,...). This makes such a platform extremely easy to handle and to integrate in various environments, contrary to thin-films of phase-change materials that are very sensitive.

The samples presented here were fabricated by ion implantation, a technique that is widely used in the microelectronics industry and could therefore be exploited for large-scale fabrication of samples. Furthermore, the size, density and depth of NCs in the host could be controlled through adjustment of implantation parameters and annealing process. This implantation process can be carried out in many different CMOS-compatible platforms such as thermal SiO$_2$ on silicon substrate and results in a flat surface that does not require any complex post-process step such as CMP to planarize the device. A next logical step could be to integrate nanophotonic devices on top of this metamaterial for a wealth of tunable functionalities such as an active control of spontaneous light emission [9, 60, 65] or dynamically tunable Huygen’s metasurfaces [66].

From a broader scientific perspective, the results presented here help define a new system with which to study tunable interactions between nanoparticles and tunable interferences between multipolar resonances leading to interesting scattering directional properties. Our research shows that there are real materials (other than Si as a typical example of HRI material (see refs [7, 8]) with phase change properties that support the basic study made in [51]. With VO$_2$ nanocrystals, the analyzed directionality properties in [51] are “tunable” by taking advantage of its phase change properties. This is a “practical tunability” where we can keep both NP size and exciting wavelength fixed. In the basic research of [51], the tunability is obtained by changing the wavelength or the size of the particle (size parameter tunability) to see a change in the directionality which many times is impractical. As a result, our research serves as a testbed for dynamical modulation of light scattering, tunable Kerker effects and active control of light directionality.

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