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# On the atomistic mechanisms for the thermal relaxation of Au-hyperdoped Si

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Au-hyperdoped Si produced by ion implantation and pulsed laser melting exhibits sub-band gap absorption in the near infra-red, a property that is interesting for Si-photonics. However, the subband gap absorption has previously been shown to be thermally metastable. In this work, we study the atomistic processes that occur during the thermal relaxation of Au-hyperdoped Si. We show that the first step in thermal relaxation is the release of substitutional Au from lattice sites. This process is characterised by an activation energy of around 1.6 eV, a value similar to that associated with Au diffusion in Si, suggesting that both processes could be rate limited by the exchange of substitutional and interstitial Au atoms. As the system further relaxes, Au is found to locally diffuse and become trapped at nearby lattice defects, notably vacancies and vacancy complexes. In fact, DFT results suggest that the formation of Au dimers is energetically favourable after the Au becomes locally trapped. The dimers could subsequently evolve into trimers, etc., as other diffusing Au atoms become trapped at the dimer. At low Au concentrations, this clustering process does not form visible precipitation after annealing at 750 °C for 3 minutes. In contrast, spherical Au precipitates are found in samples with higher Au concentrations ( $> 0.14$  at.  $\%$ ), where the Au atoms and the associated lattice defect distributions are laterally inhomogeneous.

#### I. INTRODUCTION

Single crystalline Si containing impurities at nonequilibrium concentrations (orders of magnitude higher than the equilibrium solid solubility limit) can be produced by ion implantation followed by pulsed laser melting (PLM) [\[1–](#page-8-0)[3\]](#page-8-1). The ion-implanted Si layer melts during the nanosecond laser pulse and, on cooling, rapidly resolidifies into a single-crystalline structure while kinetically trapping the impurities inside  $[4, 5]$  $[4, 5]$  $[4, 5]$ . The high impurity concentrations in hyperdoped Si lead to unusual optoelectronic properties that are of wide interest. With conventional dopants such as B, P, As, and Sb, the ultraheavily-doped layers give rise to correspondingly high electrical activity  $[6, 7]$  $[6, 7]$  $[6, 7]$ . When impurities such as chalcogens and suitable transition metals are used to hyperdope Si, the discrete sub-band gap levels that they introduce extend into an intermediate band, enabling room temperature sub-band gap photoresponse at near- to mid-IR wavelengths  $[8-10]$  $[8-10]$ , a behaviour which is significant for Si-photonics [\[11,](#page-8-8) [12\]](#page-8-9). Novel behaviours have also been demonstrated in hyperdoped Si nanostructures such as nanocrystals and nanowires [\[13,](#page-8-10) [14\]](#page-8-11).

Given the highly non-equilibrium impurity concentrations achieved, the metastability of hyperdoped Si under subsequent thermal annealing is hardly surprising. During thermal annealing, Si hyperdoped with As, for example, has been shown to form electrically-inactive clusters and As-vacancy complexes (that appear substitutional in the Si lattice) which then evolve into precipitates [\[15,](#page-8-12) [16\]](#page-8-13). A similar behaviour has also been observed with Sb-hyperdoped Si and As-hyperdoped Ge [\[17–](#page-8-14)[19\]](#page-8-15). In Si hyperdoped with chalcogens (S, Se and Te), a de-

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crease in sub-band gap absorption after thermal annealing has been observed, with thermally-activated formation of electrically inactive dopant configurations being identified as a relevant mechanism in the deactivation process [\[20,](#page-8-16) [21\]](#page-8-17). In addition, kinetically-limited processes have also been shown to contribute to the deactivation of the sub-band gap optical absorption [\[22\]](#page-8-18). Such processes are characterised by a lack of long-range impurity diffusion, short range trapping and possible precipitation [\[20,](#page-8-16) [21,](#page-8-17) [23\]](#page-8-19), and have been hypothesised to give rise to chemical states that are optically inactive [\[21\]](#page-8-17).

With energy levels deeper in the band gap of Si than chalcogens, transition metals have also gained considerable interest as candidates for hyperdoping Si. For instance, a near-IR photodetector fabricated from Au-hyperdoped Si has already been demonstrated [\[9\]](#page-8-20). Clearly, further device development necessitates an understanding of the subsequent thermal stability of the hyperdoped material, especially since the formation of contacts and other device structures, such as anti-reflective coatings, require elevated temperature processing following PLM. Although the annealing behaviour of Si hyperdoped with conventional dopants and chalcogens is relatively well-studied, similar studies on Si hyperdoped with transition metals remain limited to Ti [\[24\]](#page-8-21) and Au [\[25\]](#page-8-22). Studies on Ti hyperdoped Si have only focused on the changes in electrical properties after annealing and no structural characterisation has been attempted. However, it is worth noting that the formation of Ti-silicide has been hypothesized to be responsible for the changes in electrical behaviour [\[24\]](#page-8-21). In Au hyperdoped Si, we have previously reported an annealing-induced decrease in sub-band gap absorption that can be correlated with a reduction in Au substitutionality, as Au was found to move off lattice sites during annealing [\[25\]](#page-8-22). Nevertheless, the details of this process were not investigated and the study focussed only on samples with a high Au concentration ( $> 1$  at.  $\%$ ). Furthermore, the atomistic behaviour of the supersaturated Au atoms during thermal annealing was not specifically examined. To this end, the current paper aims to provide the first systematic study of the behaviour of Au during the thermal relaxation of hyperdoped Si. Because Au is a well-studied impurity in Si at least at equilibrium concentrations, there is a wellestablished framework for understanding its behaviour in hyperdoped Si. In particular, we show that the first step in this multi-step process is controlled by the same activation energy for all Au concentrations studied, and is also similar to that previously found for the diffusion of Au in Si.

In this work, Au-hyperdoped Si produced by ion implantation and PLM is subjected to isochronal rapid thermal annealing (RTA). We have chosen to use RTA to carry-out this study because the fast ramping rates associated with RTA compared with furnace annealing will result in less Au diffusion during ramping. This is not only more industrially relevant (it is desirable to retain the high Au concentrations during post-PLM processes)

but will also allow us to study the thermal behaviour more accurately. The change in Au distribution and atom location at different temperatures is monitored by Rutherford backscattering spectrometry combined with channelling (RBS/C) and the structural changes are examined by cross-sectional transmission electron microscopy (XTEM) for selected samples. We examine the role of Au diffusion and trapping in the thermal relaxation process and explore the possibility of Au dimerization during the thermal relaxation by comparing experimental results with first-principles calculations by density functional theory (DFT) published previously in Ref. [\[26\]](#page-8-23), to which the reader is referred for a more comprehensive analysis of the DFT data. In addition, we explore whether the relaxation behaviour depends on the Au-concentration. This is especially relevant as two distinct Au concentration regimes were previously identified for Au in hyperdoped Si formed by rapid solidification: a homogeneous regime at low Au concentrations where the Au distribution is laterally uniform, and an inhomogeneous regime at high Au concentrations (>∼ 0.2 at. %) where Au-rich filaments are observed [\[25\]](#page-8-22).

## II. EXPERIMENTAL METHODS

Samples were prepared by implanting various doses of Au<sup>+</sup> into (100) oriented n-type Si wafers (double-side polished, phosphorus-doped, resistivity 1-10  $\Omega$ -cm) at energies ranging from 50 keV to 300 keV at liquid nitrogen temperature in vacuum. Two samples (implanted at 200 keV and 300 keV) are analysed in detail in this paper, as the Au concentrations achieved in these samples are representative of the homogeneous and inhomogeneous cases, respectively. The implanted samples were subsequently melted by a single laser pulse from a Nd:YAG laser. The sample that received a 200 keV implant with a Au dose of  $1 \times 10^{15}$  cm<sup>-2</sup> has a peak sub-surface Au concentration of 0.14 at.% (as measured by  $RBS/C$ ); this sample is described as the low-concentration sample in our analysis below. The sample that received a 300 keV implant with a Au dose of  $6 \times 10^{15}$  cm<sup>-2</sup> has a peak subsurface Au concentration of 1.4 at.% and is described as the high-concentration sample. Detailed description of the ion implantation and PLM conditions can be found in Ref. [\[25\]](#page-8-22).

Rapid thermal annealing (RTA) was performed in a flowing Ar ambient using a JetFirst RTA furnace. The temperature profiles were recorded by a thermocouple attached to the back of a virgin Si wafer onto which the samples were placed. The nominal annealing temperature was varied between 350◦C and 850◦C, and the annealing duration was kept constant at 3 minutes. RBS and channelling measurements were performed using 2  $MeV$  He<sup>+</sup> with the RBS system at ANU. A glancing angle detector situated 78◦ from the sample surface normal was used for optimum depth resolution[\[27\]](#page-8-24). TEM was performed using a JEOL 2100F microscope on cross-sectional samples prepared using conventional ionpolishing.

#### III. RESULTS AND DISCUSSION

#### A. Change in Au profile

Figure [1](#page-3-0) (a) and (b) show the Au distribution (obtained from RBS) as a function of annealing temperature for low- and high-concentration samples, respectively. For annealing temperatures up to 750◦C, the Au distribution in the low-concentration sample remains unchanged. While the Au distribution of the high-concentration sample also shows no obvious change for annealing temperatures at or below  $550^{\circ}$ C (shown in Fig. [1](#page-3-0) (b) inset), the sharp concentration peak at ∼120 nm below the surface begins to flatten and shift toward the surface at temperatures above 550◦C, indicating outward Au migration in the top 120 nm of the sample. At the highest annealing temperature studied (850◦C), the peak Au concentration drops to ∼0.9 at. % and the profile is flattened in the top ∼65-120 nm. XTEM of both samples is shown above the respective RBS spectrum. Consistent with previous reports on samples fabricated under similar conditions [\[25\]](#page-8-22), no visible defects are observed in the low concentration sample while filamentary features are observed in the high concentration case. Note that the surface Au content decreased marginally with annealing temperature in both cases, presumably because some Au have evaporated during the annealing process, a behaviour which has been observed before [\[28\]](#page-8-25).

The Au concentration in the hyperdoped layer exceeds the equilibrium solubility by orders of magnitude, even in the low-concentration case. Therefore, at the annealing temperatures studied here, the supersaturated Au is expected to relax toward equilibrium by thermally diffusing down the concentration gradient at or below the equilibrium solubility limit into the Au-free Si bulk, and to precipitate at favourable sites [\[29\]](#page-8-26), as will be discussed in more detail later. This would cause a change in the Au profile, which is in fact only observed for the highconcentration sample, as shown in Fig. [1](#page-3-0) (b). Thus, the lack of change in the Au profiles for the low-concentration sample [Fig.  $1(a)$  $1(a)$ ] is rather surprising. As such, we next investigated the change in the lattice position of the Au atoms by RBS/C.

#### B. Change in Au lattice position

The change in Au substitutionality can be deduced from RBS/C spectra as a function of annealing temperature. Here, the Au substitutionality is calculated by comparing the Au backscatter yield from a direction that is aligned with a crystallographic axis ('channelled') and a random direction ('random') [\[30\]](#page-8-27). Figure [2](#page-4-0) (a) and (b) compare the backscattering spectra (one taken from 3



<span id="page-3-0"></span>FIG. 1. (a) Change in the Au concentration profile for (a) the low concentration sample and (b) the high concentration sample after various isochronal anneals, as measured by RBS, plotted against the XTEM of the corresponding as-PLM samples (before annealing) with the same depth scale; inset shows that the Au concentration profiles virtually overlapped for annealing temperatures below 550◦C. The scale bars drawn on the XTEM images are 50 nm.

a random direction and one taken from the channeled direction) of both the low concentration and the high concentration sample obtained before and after a 750◦C anneal for 3 minutes.

Both samples exhibit a drastic decrease in Au substitutionality after annealing. However, examination of these samples by XTEM, as shown in Fig. [2](#page-4-0) (c) and (d), reveals that the loss of Au substitutionality leads to observable Au-precipitation in the high-concentration sample but not in the low-concentration sample. In fact, the XTEM of the low-concentration sample after annealing [Fig. [2](#page-4-0) (c)] appears to be identical to that taken before annealing [Fig.  $1$  (a)], with no signs of Au-clustering or precipitation to the resolution of XTEM. As we shall demonstrate later, the apparent difference in the precipitation behaviour between the two samples is related to the trapping of Au atoms to local sinks.

# C. The thermal relaxation process

The mechanism by which the Au substitutionality decreases is further investigated by monitoring of the rate of substitutionality loss as a function of annealing temperature. Before RTA and excluding the segregated Au on the surface, the average substitutional Au fractions  $(X_{PLM})$  within the hyperdoped layer are 87% and 50% for the low- and high-concentration samples, respectively. This result is consistent with substitutionality values obtained previously for similar Au concentrations [\[25\]](#page-8-22), although the measured substitutional fraction for the high concentration sample may be lower than the actual value due to lattice disorder (strain) around the inhomogeneous Au filaments. In both samples, this Au substitutionality remains roughly unchanged for annealing temperatures lower than 400◦C. At higher temperatures, the Au sub-



<span id="page-4-0"></span>FIG. 2. (a) The random  $(R)$  and channelled  $(C)$  RBS/C spectra for the low concentration sample, before and after RTA at  $750^{\circ}$ C for 3 minutes. The inset is a magnified view of the Au region of the spectra from channel 200 to 320; (b) The random  $(R)$  and channelled  $(C)$  RBS/C spectra for the high concentration sample, before and after RTA under the same conditions as (a); and XTEM taken after RTA at  $750^{\circ}$ C for 3 minutes on (c) the low concentration sample and (d) the high concentration sample.

stitutionality decreases monotonically with the annealing temperature. Although not shown here, we observed the same qualitative behaviour for a range of Au-hyperdoped samples with implant energies ranging from 50 keV to 300 keV, and doses ranging from  $7 \times 10^{14}$  cm<sup>-2</sup> to  $6 \times 10^{15}$  $\rm cm^{-2}.$ 

To quantify the change of substitutional Au loss, we normalise the change in Au substitutionality,  $\triangle X$ , to the substitutionality of the sample measured directly after PLM (i.e. no subsequent annealing) using

$$
\triangle X = \frac{X_{PLM} - X(T)}{X_{PLM}},\tag{1}
$$

where  $X_{PLM}$  is the substitutional Au fraction in the pulsed laser melted sample (no anneal) and  $X(T)$  is that after subsequent annealing at temperature T.

In Fig. [3,](#page-4-1) the natural log of  $\frac{\Delta X}{t}$  (i.e. average rate of substitutionality loss) is plotted against  $\frac{1}{T}$  for both samples. For the linear regions on the right (annealing temperature  $\langle 500^{\circ}$ C), the average rate at which the Au substitutionality decreases can be described by the Arrhenius equation,

It is interesting to note that the activation energy ex- tracted for the loss of substitutional Au in hyperdoped



<span id="page-4-1"></span>FIG. 3. Arrhenius plot of the loss of substitutionality for both low and high Au concentrations. Linear fits are obtained by total least square fitting using the York error-in-variable model<sup>[\[31\]](#page-8-28)</sup> for T<500 $^{\circ}$ .

$$
\frac{\triangle X}{t} = Ae^{\frac{E_a}{kT}},\tag{2}
$$

where  $t$  is the annealing duration,  $A$  is a rate constant,  $E_a$  is the activation energy for the process and k is the Boltzmann constant. In Fig. [3,](#page-4-1) an annealing duration  $t = 180$  s is used for all annealing temperatures and we assume that the rate of substitutionality loss is constant during this time  $[32]$ . Thus, the activation energy for the loss in Au substitutionality is reasonably approximated by the slope of the straight line, where activation energies of  $E_a = 1.6 \pm 0.1$  eV and  $1.7 \pm 0.2$  eV can be extracted from the data for the low and high concentration samples, respectively. The activation energy extracted from samples with other Au concentrations, as tabulated in Table [I,](#page-5-0) is also found to be consistent within experimental error. Thus, the process that is characterised by this activation energy for the initial change in Au substitutionality appears to be the same for all Au concentrations studied here. At annealing temperatures above 500◦C, the curves shown in Fig. [3](#page-4-1) become non-linear and can no longer be characterised by the same activation energy. This suggests that additional, thermally-activated processes are occurring concurrently with the loss of substitutionality in this temperature regime  $(T > 500^{\circ}$ C).

<span id="page-5-0"></span>TABLE I. Activation energies  $(E_a)$  extracted from various Au hyperdoped samples after a 3 minute isochronal rapid thermal anneal at annealing temperatures  $\langle 450^{\circ}$ C. [Au]<sub>P</sub> is the peak sub-surface Au concentration,  $X_{PLM}$  is the sub-surface substitutional Au fraction.

Implant energy	Dose $\rm (cm^{-2})$	$[Au]_P$ $(at.\%)$	$X_{PLM}$	Inhomogeneous?	$E_a$ (eV)
$50 \text{ keV}$	$7\times10^{14}$	0.09	87\%	No	$1.5 \pm 0.3$
$50 \; \mathrm{keV}$	$1 \times 10^{15}$	0.18	75%	No	$1.4 + 0.2$
$200 \text{ keV}$	$1 \times 10^{15}$	0.10	87\%	No	$1.6 \pm 0.1$
$200 \text{ keV}$	$4 \times 10^{15}$	0.44	67\%	Yes	$1.5 \pm 0.2$
$300 \text{ keV}$	$6 \times 10^{15}$	1.4	$50\%$	Yes	$1.7 \pm 0.2$

Si (∼1.6 eV) is similar to the activation energy (∼1.7  $\pm$  0.1 eV) for the diffusion of Au extracted from nearequilibrium annealing experiments on Au-implanted Si [\[33\]](#page-9-1). One plausible interpretation is that both processes are controlled by the same thermally-activated step, which we discuss below in relation to the diffusion of Au in Si.

Two indirect substitutional-interstitial mechanisms have been proposed to explain the diffusion behaviour of Au in Si. In the kick-out mechanism  $[34]$ , a diffusing interstitial Au atom 'kicks out' a Si atom in the lattice, takes its place and creates a Si self-interstitial. This is described by

<span id="page-5-1"></span>
$$
Au_i \leftrightarrow Au_s + I,\tag{3}
$$

where I denotes a Si self-interstitial. Analogously, the dissociative or Frank-Turnbull mechanism, which was originally proposed for Cu diffusion in Ge [\[35\]](#page-9-3), has subsequently been suggested for Au diffusion in Si [\[36\]](#page-9-4): it involves the production of a vacancy,  $V$ . In this scenario,  $Au<sub>s</sub>$  is dissociated into a  $Au<sub>i</sub>$  and a V. This process is described by

<span id="page-5-2"></span>
$$
Au_s \leftrightarrow Au_i + V. \tag{4}
$$

Although there is a preponderance of evidence for the kick-out mechanism, the literature does not show unanimous agreement (see, for instance, Refs. [\[37,](#page-9-5) [38\]](#page-9-6) and references within). However, it has been demonstrated that when the sample contains a supersaturation of sinks for diffusing  $I$  or  $V$ , (i.e. when  $I$  in Eq. [3](#page-5-1) and  $V$  in Eq. [4](#page-5-2) are removed sufficiently quickly via recombination and does not limit the diffusion), the diffusion profile for the two mechanisms become identical and the exchange of substitutional and interstitial Au becomes the rate-limiting process instead [\[39\]](#page-9-7). This latter exchangelimited regime is likely to be operative during the diffusion of ion-implanted Au, from which an activation energy of  $\sim$ 1.7 ± 0.1 eV was extracted in Ref. [\[33\]](#page-9-1), because ion-implanted Si is known to contain sinks for point defects. For instance, the so-called  $\frac{R_P}{2}$  defects, which are excess vacancies created by the implantation process, are found to cluster into thermally-stable small voids in ionimplanted and thermally-annealed Si [\[40\]](#page-9-8).

Furthermore the release of Au from substitutional lat-

tice positions can be written as:

$$
Au_s \to Au_i + V,\tag{5}
$$

where  $V$  denotes a vacancy. In this case, the exchange process between  $Au<sub>s</sub>$  and  $Au<sub>i</sub>$  would also be the ratelimiting process assuming (a) the migration of  $Au_i$  and (b) further creation of vacancies do not limit the reaction. Such assumptions are not unreasonable because (a)  $Au_i$  is known to have an extremely high diffusivity in Si [\[41\]](#page-9-9), and (b) excess vacancies in Si are known to cluster at favourable sites, as mentioned earlier [\[40\]](#page-9-8). While the analysis above strongly suggests that the release of Au from substitutional sites is the rate-limiting step (characterised by an  $E_a$  of around 1.6 eV) for both the thermal diffusion of ion-implanted Au in Si and the loss of Au substitutionality in Au-hyperdoped Si, further work is required to fully validate this interpretation. Regardless of the physical origin of the extracted  $E_a$ , however, the  $E_a$  value of  $\sim 1.6$  eV is consistent for all Au concentrations studied [\[42\]](#page-9-10). However, the apparent difference in the final relaxation behaviour (precipitation) between the low and high-concentration samples (as shown in Fig. [1\)](#page-3-0) now needs to be addressed.

It is well-known that lattice imperfections such as point defects, cavities and free surfaces are effective sinks for metal impurities in Si [\[43\]](#page-9-11). In particular, atomic trapping has been previously observed for equilibriumconcentration Au in Si, during which Au atoms are found to be trapped onto cavity walls through a chemisorptionlike process. Similarly, other imperfect regions in the lattice (such as dislocations and other defects) are also likely to be active trapping sites as a result of poorlycoordinated Si atoms in/around such regions. Such local lattice disorder and excess vacancies are expected to trap diffusing  $Au_i$  atoms. Although the hyperdoped layer is near-perfect crystalline Si (as seen in high-resolution TEM $[25]$ , in a separate study  $[44]$ , we demonstrate that it does contain excess vacancies and is hence not defectfree. Due to the presence of such traps, the excess Au (above the equilibrium solubility limit) that was initially frozen-in to near-substitutional lattice sites following PLM would, after being released from substitutional sites, diffuse to favourable, local trapping sites within the hyperdoped layer. While this behaviour is expected at both Au concentrations studied, we believe that the differing size, distribution and binding energy of the trap sites between the two concentration regimes is the cause of the apparent difference in precipitation behaviour seen in Fig. [2.](#page-4-0)

Unlike the trapping effect observed on equilibriumconcentration ion-implanted samples during thermal annealing, where long range diffusion of Au to cavities or the wafer surfaces occurs [\[29,](#page-8-26) [43\]](#page-9-11), the trapping sites in Au-hyperdoped Si (for example, vacancies) are confined to the hyperdoped layer (i.e. within the PLM melt depth). Hence, the migration and trapping of the Au, for both Au concentrations, is also expected to be local within the hyperdoped layer. For the high concentration case, the most favourable trap sites (i.e. with the highest binding energy) are presumably concentrated within the top ∼110 nm, in which Au-rich filaments and a variety of associated lattice defects can be observed [see Fig. [1](#page-3-0) (b)]. As the annealing temperature further increases, the trap sites with the highest binding energy (such as vacancies and small cavities [\[29\]](#page-8-26)) may then cluster and become nucleation sites for subsequent Au precipitation and growth, resulting in skewing and broadening of the Au profile. Conversely, the lack of profile-broadening observed in the low concentration sample on annealing [Fig. [1](#page-3-0) (a)] suggests very local Au trapping where the migration length is within the resolution of RBS. The homogeneity observed in TEM in Fig. [1](#page-3-0) (a), in contrast to that of the high concentration sample in Fig. [1](#page-3-0) (b), suggests a more uniform concentration of trapping sites interspersed within the melt depth at sufficiently high density that none of them attracts enough Au atoms to form a visible precipitate. Rather, we suggest that the multitudinous trapping sites, all of which are small compared with the sinks in the high concentration case, give rise to a greater number of much smaller Au complexes that pin Au sufficiently strongly to prevent the formation of visible precipitates at temperatures up to 750◦C.

Although previous high-resolution TEM indicated the formation of spherical precipitates as the final stage of annealing [\[25\]](#page-8-22), experimental observation of the atomistic evolution of this process is difficult even with highresolution TEM, considering that the transient configurations of the trapped Au may consist of only up to a few Au atoms. However, a first-principles analysis by density functional theory (DFT) has been recently employed to simulate the defect formation energetics for different atomic configurations of supersaturated Au in Si [\[26\]](#page-8-23). Since DFT gives the equilibrium configuration when all the atoms are relaxed, the simulated system can give insight into the relaxation process of the Au-hyperdoped Si system following subsequent thermal annealing. We now use these first-principles DFT results to aid the understanding of the atomistic behaviour of Au-hyperdoped Si during thermal relaxation.

During the initial stage of relaxation, the loss of Au substitutionality observed in RBS measurements is ratelimited by the release of Au from substitutional lattice sites and subsequent local migration to adjacent trapping



<span id="page-6-0"></span>FIG. 4. Sub-band gap absorption of the low-concentration sample after 3 minute anneals at temperatures ranging from  $450^{\circ}$  to 750°. The absorption of the high concentration sample has been reported elsewhere [\[25\]](#page-8-22).

sites such as lattice disorder and especially vacancy-type defects [\[44\]](#page-9-12). Because the substitutional Au dimer configuration is found to be the most energetically favourable defect reported in Ref. [\[26\]](#page-8-23), the Au that is released from isolated substitutional sites will strongly favour the formation of a dimer, after they become locally trapped (at isolated vacancies, for example) and relax in adjacent sites. Other migrating Au atoms in proximity to the dimer complex are expected to be attracted to the dimer in a similar fashion to lower the free energy $[45]$ , evolving into trimers, and so on, ultimately leading to the nucleation of observable precipitates. Compared with the low-concentration sample, the trap sites in the high concentration sample are inhomogeneous and larger, which may result in larger Au-decorated zones that can nucleate and grow into larger, well-defined Au precipitates. This process is consistent with the continual broadening of the Au concentration profile with increasing annealing temperature for  $T > 500^{\circ}$ C, as shown in Fig. [1](#page-3-0) (b).

Finally, DFT results indicate that different Au configurations in the Si lattice are associated with different defect levels within the Si band gap. In particular, isolated substitutional Au, which is experimentally found to be the primary Au configuration in an unrelaxed system, is expected to give rise to optically active mid-gap states that are responsible for the observed sub-band gap optical absorption [\[26\]](#page-8-23). Au dimers, on the other hand, are not expected to introduce such mid-gap states based on DFT calculations. This result is qualitatively consistent with the reduction in sub-band gap optical absorption observed in annealed samples with a high Au concentration, as reported previously [\[25\]](#page-8-22). Similarly, as is shown in Figure [4,](#page-6-0) the sub-band gap optical absorption for the low-concentration sample studied here also decreases with annealing temperature. The upward tail from ∼1500 nm that is observed following the 450◦C and 550◦C anneals has also been observed previously on the high-concentration sample, and is hypothesized to be related to other, non-Au related defects in the Si lattice that anneal away at temperatures higher than 550◦C. Note that the sub-band gap absorption never drops to the virgin level even after a 750◦C anneal. As discussed previously [\[25\]](#page-8-22), this is a result of a small fraction of the Au diffusing throughout the  $450\mu m$  thick wafer and subsequently occupying substitutional sites up to the equilibrium solubility limit throughout the sample at 750◦C (approximately  $1 \times 10^{14}$  cm<sup>-3</sup>).

#### IV. CONCLUSION

In conclusion, we have shown that the thermal relaxation of Au-hyperdoped Si is a multi-step process. The first step of relaxation is marked by a loss in the Au substitutionality through a process that is characterised by an activation energy of ∼1.6 eV, a value that may be related to the rate-limiting step in the thermal diffusion of Au in Si. This suggests that the rate-limiting step in both cases may be the exchange between substitutional and interstitial Au. As the relaxation progresses, our observations of the Au profile broadening and local lattice environment strongly suggest local Au trapping at lattice imperfections, such as vacancies, within the hyperdoped layer. The trapped Au could then evolve into the more energetically favourable configurations of Au dimers and trimers. The system becomes fully relaxed when all the excess Au atoms that were initially incorporated during solidification into substitutional lattice sites beyond the solubility limit evolve into observable Au precipitates (at high concentrations). Although these observations are only conclusive for Au-hyperdoped Si, it is conceivable that similar thermal behaviours could also take place in other hyperdoped materials.

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