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Tunable type-II BiVO₄/g-C₃N₄ nano-heterostructures for photocatalysis applications

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BiVO₄/g-C₃N₄ heterostructures combining the advantages of bismuth vanadate and graphitic carbon nitride have recently emerged as a promising material system for photocatalytic applications. Further performance improvement will require in-depth understanding and fine tuning the near-edge electronic properties of these heterostructures. In this work, we have investigated the electronic properties, in particular the band edge states that control the optical and transport properties, of BiVO₄/g-C₃N₄ nano-heterostructures using the Heyd, Scuseria, and Ernzerhof (HSE) hybrid functional approach. Our results demonstrate that BiVO₄/g-C₃N₄ heterostructures have a desired type-II band alignment, which may greatly facilitate rapid separation of photogenerated carriers. We find that the BiVO₄ subsystem responsible for the robust and strong optical absorption observed experimentally. Our calculated absorption edge of about 2.5 eV agrees remarkably well with the experimental value of 2.45 eV. We have also investigated the effect of external electric field on the band edge states, band alignment, and the optical and fundamental band gaps of the BiVO₄/g-C₃N₄ heterostructures. The band edge states of the BiVO₄ and g-C₃N₄ subsystems respond very differently to the applied electric field, resulting in electric-field tunable band offsets and band gap of the BiVO₄/g-C₃N₄ heterostructures. The contrasting response of the fundamental and optical gaps to electric field suggests a novel avenue for future experimental optimization of the optical absorption and carrier separation dynamics of these heterostructures for photoelectrochemical catalysis applications.

I. INTRODUCTION

Semiconductor-based photocatalysis has received tremendous research attention in wake of concerns about global environmental pollution and energy crisis [1]. In the past few decades, several methods[2-4] have been developed to overcome the serious shortcomings of fast charge recombination and limited visible-light absorption of semiconductor photocatalysts. One of the most widely explored strategies is the use of photocatalytic heterojunctions[2,5-7]. Previous work[8,9] has demonstrated that the construction of two semiconductors with suitable electronic structures may exhibit superior photoactivity than single photocatalysts. In particular, a type II band alignment at the heterostructure interface can facilitate rapid separation of photogenerated electron-hole pairs, resulting in significantly improved photocatalytic performance.

Bismuth vanadate (BiVO_4) is one of the most promising photocatalytic materials for water oxidation[10-14] due to its moderate band gap, high optical absorption, and being abundance, low cost, and highly stable[15-18]. On the other hand, graphite-phase carbon nitride $\text{g-C}_3\text{N}_4$ also exhibits good visible-light response[19,20] and has attracted a great deal of scientific interest for its applications in photocatalytic water splitting[19,21-26] and organic pollutant degradation[27-31]. Therefore, it is plausible that the $\text{BiVO}_4/\text{g-C}_3\text{N}_4$ heterostructures[9,32-39], which combine the advantages of $\text{g-C}_3\text{N}_4$ and BiVO_4 , might give rise to superior photocatalytic performance. Experimentally, it is found that the $\text{BiVO}_4/\text{g-C}_3\text{N}_4$ heterojunction with different weight ratios of $\text{g-C}_3\text{N}_4$ resulted in varying photocatalytic efficiency. For example, Kong *et al.* reported that a $\text{BiVO}_4/\text{g-C}_3\text{N}_4$ heterostructure (26.94 wt.% of BiVO_4) exhibits an excellent oxygen evolution rate of $750 \mu\text{mol h}^{-1}\text{g}^{-1}$ under visible light irradiation, which represents a 129% increase compared to that of pristine BiVO_4 , and a photonic efficiency of 19%[40]. Che and co-workers[41] concluded that a 50/50 mass ratio $\text{BiVO}_4/\text{g-C}_3\text{N}_4$ heterojunction was the best for photocatalysis, showing remarkably higher photocatalytic activities in degrading rhodamineB (RhB) compared with pure C_3N_4 or BiVO_4 . Sui and co-workers[39] demonstrated that a $\text{BiVO}_4/\text{g-C}_3\text{N}_4$ heterojunction with 7 wt% $\text{g-C}_3\text{N}_4$ was seven times more efficient than pristine BiVO_4 . On the other hand, Sun *et al.* [37] showed that a $\text{BiVO}_4/\text{g-C}_3\text{N}_4$ heterojunction with 3% BiVO_4 exhibited the highest photocatalytic efficiency. Therefore, it is clear that optimal $\text{BiVO}_4/\text{g-C}_3\text{N}_4$ heterostructures have not been identified and there is still

much room for improving their photocatalytic efficiency.

To better understand the improved photocatalytic performance of the BiVO₄/g-C₃N₄ heterojunctions, it is important to carry out systematic studies of their electronic properties and how they may be tuned, for example, with different weight ratios of the sub-systems or with an external field. Theory is able to provide useful insight for understanding experimental results and guidance for experimental design of heterostructure for improved photocatalytic performance.

Experimentally, it is difficult to realize tunable band gap by controlling the weight ratio of g-C₃N₄ in the BiVO₄/g-C₃N₄ heterojunction. For example, Sui and co-workers[39] concluded that the optical band gaps of BiVO₄ and BiVO₄@g-C₃N₄ (with 3, 5, 7, 10 wt% g-C₃N₄) are basically the same (about 2.45 eV) since they observed little change to the absorption edge among the samples. Their conclusion is consistent with several other experimental results[33,38,42]. However, it is often desirable to tune the electronic properties of heterostructures for optimal performance in different applications and conditions, and applying electric field is one of most convenient and effective approaches. Indeed, Kan and coworkers[43] have demonstrated that the band gap of bilayer g-C₃N₄, thus the optical properties, can be easily tuned by an external electric field.

In this work, we first investigate the structural and electronic properties of the BiVO₄/g-C₃N₄ heterojunctions with different number of g-C₃N₄ layers. This study provides an in-depth understanding of the important electronic structures features such as band gap, band edge states, band alignment, and the effect of the g-C₃N₄ layer thickness on the electronic and structural properties of these structures. We then study the effects of the electric-field on the electronic structure and interfacial properties of the BiVO₄/g-C₃N₄ heterojunctions. We find that BiVO₄/g-C₃N₄ heterojunctions have a desired type-II band alignment and that the BiVO₄ subsystem is responsible for the robust optical gap observed in experiment. In addition, the fundamental (minimum) band gap of the BiVO₄/g-C₃N₄ heterojunction can be effectively tuned by applying an external E-field, and a transition from semiconductor to metal is observed; the optical band gap, on the other hand, remains rather robust, but can also be tuned between 2.05 to 2.55 eV with a moderate E-field. More interestingly, the greater the number of the g-C₃N₄ layers, the more effective the E-field in tuning the band gap becomes.

II. COMPUTATIONAL

Density functional theory (DFT) based first-principles calculations are performed using the projected augmented wave (PAW)[44] method implemented in the Vienna *ab initio* simulation package (VASP).[45,46] The Kohn-Sham one-electron states are expanded using the plane wave basis set with a kinetic energy cutoff of 500 eV. The Perdew-Burke-Ernzerhof (PBE)[47] exchange-correlation (XC) functional within the generalized gradient approximation (GGA) is employed for the geometrical optimization. Since the van der Waals (vdW) interaction is expected to be important in these layered structures, in this work, we adopted the DFT-D3(BJ)[48] method with a Becke and Johnson (BJ) damped[49,50] vdW correction.

Since the GGA approach usually underestimates the band gap of semiconductors, we use the screened hybrid functional of Heyd, Scuseria, and Ernzerhof (HSE) [51] for a more accurate description of the electronic structure. In this work, we use the HSE06 functional [51] with a screening parameter $\omega = 0.2\text{\AA}^{-1}$ and a small mixing parameter α ($\alpha = 0.175$) for the short-range Hartree-Fock exchange instead of the commonly used value of 0.25. Using these parameters (i.e., $\omega = 0.2\text{\AA}^{-1}$ and $\alpha = 0.175$), the calculated band gaps of isolated monolayer g-C₃N₄ (2.70 eV) and bulk BiVO₄ (2.45eV) compare well with experimental results (2.7 eV[22] for g-C₃N₄ and 2.5 eV[52] for bulk BiVO₄) and previous theory (2.7 eV[9,53] for g-C₃N₄ and 2.4 eV[54] for bulk BiVO₄).

We mention that one should be cautious when comparing the theoretical band gap calculated here with experiment since the measured band gap includes several renormalization effects[55,56], including (but not limited to) electron-phonon renormalization, lattice polarization, and spin-orbit coupling effects. However, accurate calculations of the quasiparticle band gaps are not the main focus of this work. We expect that the band gap renormalization effects do not change the main results of this work since we attempt to model the already renormalized gap and band alignments, which are reproduced reasonably (admittedly fortuitously) using the HSE functional with appropriately chosen the HF mixing parameter.

The Brillouin-zone (BZ) integration is carried out using the Monkhorst-Pack [57] sampling method with a density of $2\times 6\times 1$ for the BiVO₄/g-C₃N₄ heterostructures. A vacuum layer of 15 Å is included to avoid the interaction between neighboring slabs.

The external electric field is introduced by adding a planar dipole layer in the middle of the vacuum layer in the periodic supercell[58] as implemented in VASP. The effects of the applied electric field on the atomic structure are neglected as they are very small. All atoms are fully relaxed until the maximum magnitude of the force acting on the atoms is smaller than 0.03 eV/Å. We define the positive direction of the E-field as pointing from BiVO₄ (010) to g-C₃N₄, as shown in the inset of Fig. 1(f).

Note that there is substantial lattice mismatch between BiVO₄ and g-C₃N₄. For the heterostructures studied in this work, we use the averaged lateral lattice constants (of the supercells) to minimize the strains on both subsystems to within ±3.5%. This strain introduces a small enhancement to the band gap of the BiVO₄ slab from 2.45 eV to about 2.7 eV. For the g-C₃N₄ over-layer, the strain and interfacial interaction cause the structure to buckle as shown in Fig. 1. The buckling effects significantly enhances the band gap of g-C₃N₄ to about 3.1 eV, to be compared with about 2.7 eV for the flat g-C₃N₄.

The imaginary part $\varepsilon_2(\omega)$ of the dielectric function $\varepsilon(\omega)$ is calculated using the standard formulation:

$$\varepsilon_2(\omega) = \frac{Ve^2}{2\pi\hbar m^2 \omega^2} \int d^3k \sum_{n,n'} |\langle n\vec{k} | \vec{p} | n'\vec{k} \rangle|^2 f_{n\vec{k}}(1 - f_{n'\vec{k}}) \delta(E_{n\vec{k}} - E_{n'\vec{k}} - \hbar\omega), \quad (1)$$

where V is the cell volume, $\hbar\omega$ is the energy of the incident photon, \vec{p} is the momentum operator, $|n\vec{k}\rangle$ the electronic state, and $f_{n\vec{k}}$ is the Fermi occupation function. The real part $\varepsilon_1(\omega)$ is related to $\varepsilon_2(\omega)$ by the Kramer–Krönig transformation. The absorption coefficient $a(\omega)$ can be derived from $\varepsilon_1(\omega)$ and $\varepsilon_2(\omega)$ as follows[59]

$$\alpha(\omega) = \frac{\sqrt{2}\omega}{c} [\sqrt{\varepsilon_1^2(\omega) + \varepsilon_2^2(\omega)} - \varepsilon_1(\omega)]^{1/2}. \quad (2)$$

III. RESULTS AND DISCUSSION

A. Structural properties

In order to reduce the in-plane lattice mismatch, the heterostructure models are created by placing the g-C₃N₄ layers with a $2\sqrt{3}\times 1$ supercell and different thickness onto a 12-layer-thick 3×1 BiVO₄ (010) slab. In addition, we use the averaged lattice constants of the subsystems for the heterostructure models to minimize the effects on the lattice mismatch. The bottom 6 layers of the BiVO₄ (010) slab are fixed at the

bulk structure while the top 6 layers are allowed to relax. We will denote the single-layer, double-layer, and tri-layer g-C₃N₄ on BiVO₄ (010) surface models as BiVO₄/SL-g-C₃N₄, BiVO₄/BL-g-C₃N₄, and BiVO₄/TL-g-C₃N₄, which are illustrated in Figs. 1 (a), (c), (e), respectively. We have studied several nonequivalent structures, namely, four for BiVO₄/SL-g-C₃N₄, eight for BiVO₄/BL-g-C₃N₄, and sixteen for BiVO₄/TL-g-C₃N₄. The lowest energy structures of BiVO₄/SL-g-C₃N₄, BiVO₄/BL-g-C₃N₄, and BiVO₄/TL-g-C₃N₄ are shown in Fig. 1(b), (d), and (f), respectively. These low energy structures we found are by no means the most stable structures. However, our main results should not be affected significantly if slightly different structures are used. In the following, we will focus on these lowest energy structures. It should be pointed out that both I2/b and C2/c space groups are commonly used to describe the monoclinic scheelite structure of BiVO₄[14]. Here we use the C2/c space group notation. The (010) surface using the C2/c space group notation is equivalent to (001) surface using the I2/b notion, which has been shown to be the most stable one [60]. **Ideally, theoretical studies of photocatalysis should consider surface hydration effects as adsorption of water may modify the surface electronic properties. In addition, hydration may also cause degradation of photocatalysts. The issue of hydration effects is beyond the scope of this study but definitely deserves further investigations.**

In order to address the stability of the heterostructures, we define an interface adhesion energy:

$$E(\text{ad.}) = [E(\text{hetero}) - E(\text{g-C}_3\text{N}_4) - E(\text{BiVO}_4)]/S, \quad (3)$$

where $E(\text{hetero})$, $E(\text{g-C}_3\text{N}_4)$, and $E(\text{BiVO}_4)$ are the total energies of the relaxed BiVO₄/g-C₃N₄ heterostructure, g-C₃N₄ (001), and BiVO₄ (010) slabs, respectively; S is the area of the interface. The calculated adhesion energies for BiVO₄/SL-g-C₃N₄, BiVO₄/BL-g-C₃N₄, and BiVO₄/TL-g-C₃N₄ heterostructures are -0.20 eV/Å², -0.25 eV/Å², and -0.18 eV/Å², respectively, suggesting that these structures are stable. These adhesion energies are consistent with those for g-C₃N₄ (001) on the Zn₂GeO₄ (110) surface (-0.18 eV/Å²)[61] and graphene-coupled Bi₂WO₆ (010) surface (-0.18 eV/Å²)[8]. It should be noted that the calculated adhesion energy is significantly greater than that for typical vdW systems such as graphite, suggesting that both physical and chemical effects contribute to the surface adhesion. However, chemical

hybridization effects are rather weak and there are no chemical bonds formed at the interface.

After structural optimization, the g-C₃N₄ layers show considerable distortion, as shown in Fig. 1(b), (d) and (f). The structural distortions, in particular, the wavy distortion features, are due in part to the lattice mismatch, which is about 3%. The local distortions and the small interfacial distances, however, suggest significant interfacial chemical interactions at the interface, which is similar to the results for g-C₃N₄ (001)/ZnWO₄ (010) heterostructure[62] and bilayer-g-C₃N₄/MoS₂ heterostructure[53]. We would like to mention that the lattice mismatch has minimal effects on the electronic structures. The vertical separation between the g-C₃N₄ layer and the BiVO₄ (010) surface is 1.85Å (h₁ in Fig. 1(b)) for the BiVO₄/SL-g-C₃N₄ structure, 2.24Å (h₂ in Fig. 1(d)) for BiVO₄/BL-g-C₃N₄, and 1.89Å (h₃ in Fig. 1(f)) for BiVO₄/TL-g-C₃N₄. These interlayer separations are smaller than typical vdW interaction distance. For example, the interlayer separation is 2.89 Å for the graphene/g-C₃N₄ heterostructure[63], 2.87 Å for g-C₃N₄/TiO₂(100)[64] and 3.16 Å for DL-g-C₃N₄/MoS₂[53]. The shorter interlayer distance implies a stronger interlayer interaction between the BiVO₄ and g-C₃N₄ layers.

B. Electronic structure and band alignment

Electronic structures of the BiVO₄/g-C₃N₄ heterostructures are calculated using the HSE06 screened hybrid functional method. Figure 2 shows the calculated total density of state (TDOS, shown in green in Fig. 2) of the heterostructures and the partial density of state (PDOS) for the subsystems BiVO₄ (shown in orange) and g-C₃N₄ (dark blue). The position of the valence band maximum (VBM) is placed at zero for all three heterostructures for better comparison. The calculated band gaps of the BiVO₄/SL-g-C₃N₄, BiVO₄/BL-g-C₃N₄, and BiVO₄/TL-g-C₃N₄ heterostructures are 1.27eV, 1.24eV, and 1.37eV, respectively, indicating that the number of g-C₃N₄ layers has little effect on the heterojunction bandgap. The calculated band gap (~ 1.2 to 1.4 eV), however, is significantly smaller than the experimentally measured optical gap of about 2.45 eV[39]. We will address this issue in Section C.

Band alignment is very important in understanding the enhanced photocatalytic properties in these nano-heterojunctions since it controls the separation of photo-generated carriers, which can be conveniently obtained by plotting the partial DOS of the subsystems across the interfaces. Dashed lines in Fig. 2 indicate the VBM

and CBM of the BiVO_4 and $\text{g-C}_3\text{N}_4$ subsystems, and the resulting band alignment diagrams are shown in Fig. 2(d). It is clear that all three heterostructures have a type-II[65,66] band alignment. Therefore, photo-generated lowest-energy electrons and holes will spontaneously separate in these structures, making them suitable for photocatalysis applications. Our theoretical results are consistent with experimental observation[33,34,38]. For comparison, we also show in Fig. 2(e) the band alignment diagrams calculated using the PBE functional. Although the band gap of the heterostructures are severely underestimated with the PBE functional, the qualitative features of the band alignments are similar to those calculated using the HSE functional. We would like to mention that calculating the band alignments of bulk solids typically involves several steps due to the need to line up the electrostatic potential of the individual bulk solids[67]. For finite systems, however, band alignments at the interface can be obtained by inspecting the atomic resolved density of states.

To gain further insight into the electronic properties of these heterostructures, we show in Fig. 3(a) atomically resolved projected DOS using $\text{BiVO}_4/\text{BL-g-C}_3\text{N}_4$ as a representative system. It is evident that the VBM state is primarily of N-2*p* character with some contribution from C-2*p* states while the CBM is mostly of V-3*d* character with a small admixture of O-2*p* states. A more vivid picture of these atomically (therefore spatially) distinct characters of the VBM and CBM states is shown with the real-space charge density plot of the VBM and CBM states [Fig. 3(b)]. These results clearly reveal that the CBM and VBM states are localized in different layers of the $\text{BiVO}_4/\text{g-C}_3\text{N}_4$ heterostructures, thus facilitating the separation of electrons and holes when photo-carriers are generated. As a result, the undesirable rapid electron-hole recombination can be greatly suppressed in these structures. Similar results are found for other systems by Niu et al.[68]

C. Optical properties of $\text{BiVO}_4/\text{g-C}_3\text{N}_4$ heterostructures

As we have mentioned earlier, the experimentally measured optical gap is about 2.45 eV for the $\text{BiVO}_4/\text{g-C}_3\text{N}_4$ heterostructures whereas the calculated HSE minimum gap ranges from 1.2 to 1.4 eV. Therefore, there appears to be a significant discrepancy between theory and experiment. Although in principle the Kohn-Sham gap cannot be compared directly with the optical excitation gap, we still expect a better agreement

with experiment considering that our HSE calculations reproduce well the experimental gap for both BiVO_4 and $\text{g-C}_3\text{N}_4$ subsystems. To this end, we have carried out optical absorption calculations for the $\text{BiVO}_4/\text{g-C}_3\text{N}_4$ heterostructures at the DFT (HSE) level. Figure 4 shows the calculated optical absorption coefficient for the three heterostructures studied in this work. Interestingly, our calculations predict a sharp absorption starting at about 2.5 eV, regardless of the number of the $\text{g-C}_3\text{N}_4$ layers, which agree remarkably well with the experimental result of 2.45 eV[39].

The significant difference between the calculated minimum (fundamental) band gap and the optical absorption gap can be understood with the projected DOS shown in Fig.2 and 3. As we have discussed in the previous section, the VBM states are mostly derived from the $\text{g-C}_3\text{N}_4$ subsystem whereas the CBM states are from BiVO_4 . The optical dipole matrix elements between these spatially separated VBM and CBM states are greatly suppressed due to the minimal overlap between the initial and final state wave functions. It is evident that strong absorption occurs when the photon energy exceeds the band gap of BiVO_4 , and the BiVO_4 subsystem is responsible for the optical absorption at 2.45 eV.

We would like to mention that for layered systems such as those studied here both the quasiparticle self-energy and excitonic effects are important because of the relatively weak screening in the system. Ideally, one needs to carry out higher level calculations[69] beyond DFT to compare with optical experiments. Interestingly, it was found that the quasiparticle self-energy and the excitonic effects largely cancel out as far as the minimum absorption gap is concern. Therefore, although the excitonic effects will strongly modify the features of the optical absorption spectrum, the overall optical band gap can be compared satisfactory with DFT based calculations.

D. Tuning the band edge states with electric field

The robust optical gap may be considered as an advantageous property of the $\text{BiVO}_4/\text{g-C}_3\text{N}_4$ heterostructures. On the other hand, it may also be desirable that this optical gap (shown in Fig. 4) as well as the fundamental gap (shown in Fig. 2) be tunable to suit different application needs. In this regard, the nearly constant optical

and fundamental gap may become a drawback. Applying an external electric field is one of the most effective ways for tuning the electronic properties of nanostructures such as the heterostructures studied in this work.

We have investigated the effect of external electric field on the band edge states and the optical and fundamental band gap of the $\text{BiVO}_4/\text{g-C}_3\text{N}_4$ heterostructures. The external electric field (\mathbf{E}) is applied perpendicularly to the layer plane, which is important in practical applications[43,70,71]. We mention that we neglect the additional lattice distortions due to the applied electric field since they are found to be very small in our study. For example, with an applied field of 0.6 V/\AA , additional relaxation only amounts to about 2 meV/atom change in the calculated energy. The lack of a large permanent dipole moment of the model structure helps to explain the small structural distortion effects. The calculated permanent dipole along the direction of the applied electric field is only about 1.0 Debye for the whole $\text{BiVO}_4/\text{SL-g-C}_3\text{N}_4$ system. From comparison, that permanent dipole moment of a single LiF molecule is about 6.5 Debye . The evolution of the fundamental (minimum) band gap with the applied external electric field \mathbf{E} for the three $\text{BiVO}_4/\text{g-C}_3\text{N}_4$ heterostructures is shown in Fig. 5. All three $\text{BiVO}_4/\text{g-C}_3\text{N}_4$ heterostructures show a similar electric field dependent of the fundamental band gap, with the band gap of the $\text{BiVO}_4/\text{TL-g-C}_3\text{N}_4$ structure showing the strongest field dependence. The band gap can be tuned between 0 and 2.1 eV with the electric field changing from -0.3 to 0.3 V/\AA for the $\text{BiVO}_4/\text{TL-g-C}_3\text{N}_4$ structure. This widely tunable band gap with a moderate electric field makes these structures an ideal choice for applications where improved performance may be achieved through band gap optimization. In addition, the electric field induced semiconductor-metal transition may find new applications for these structures beyond photocatalysis such as switching devices.

Since the band edge states of the BiVO_4 and $\text{g-C}_3\text{N}_4$ subsystems have distinct characters, we expect that they respond differently to the applied electric field. Thus, not only the fundamental band gap but also the band offsets and optical absorption gap may be tuned by an electric field. Figure 6(a) illustrates how the band edge states of the subsystems BiVO_4 and $\text{g-C}_3\text{N}_4$ in the $\text{BiVO}_4/\text{TL-g-C}_3\text{N}_4$ structure vary with the electric field. There are a few interesting observations that deserve mentioning. Both the CBM and VBM of the BiVO_4 subsystem move higher with increasing electric field, indicating that the electric dipole of these states is opposite to the positive direction defined in Fig. 1. The small nonlinear behavior is a result of second-order

effects. The band edge states of the g-C₃N₄ subsystem, on the other hand, show very different response to the electric field. The VBM of g-C₃N₄ does not shift appreciably with the electric field, indicating that this state has a negligible dipole moment. The CBM of g-C₃N₄, however, shows an interesting parabolic behavior around zero electric field, suggesting that second order effects play an important role.

The different response of the subsystem band edge states to the electric field also suggests field-tunable band offsets. Figure 6(b) shows the band gap (E_g), optical gap (band gap of BiVO₄, E_{g_BiVO4}) and the conduction and valence band offsets (ΔE_V and ΔE_C) of BiVO₄/TL-g-C₃N₄ as a function of the external electric field. Both band offsets decrease monotonically with increasing E field, and they can both be tuned from positive to negative values. The semiconductor-metal transition is a result of the lowering of the CBM state of BiVO₄ with negative electric field, which eventually merges with the VBM of the g-C₃N₄ subsystem. As we have shown in Fig. 4, BiVO₄ is mostly responsible for the optical absorption of the BiVO₄/g-C₃N₄ heterostructures. Our analysis of the electric-field dependent band edge states also suggests that the optical band gap (E_{g_BiVO4}) of these structures can be tuned with electric field from about 2.05 to 2.5 eV as shown in Fig. 6(b) (orange curve). Therefore, although the fundamental gap can be widely tuned from 0 to 2.1 eV with an external field changing from -0.3 to 0.3 V/Å, the optical gap remains rather robust.

IV. SUMMARY

In summary, we have carried out an in-depth analysis of the electronic properties, in particular, the band edge states that control the optical and transport properties, of the BiVO₄/g-C₃N₄ nano-heterostructures using the HSE hybrid density functional approach. The distinct atomic character of the band edge states clearly indicates a type-II band alignment in these structures, which is beneficial for the separation of photogenerated carriers. Although the fundamental gap (1.2 ~ 1.4 eV) of the BiVO₄/g-C₃N₄ heterostructures is considerably smaller than that of the BiVO₄ or g-C₃N₄ subsystem, we find that strong optical absorption starts at about 2.5 eV for all three heterostructures investigated in this work. This result agrees remarkably well with the experimental observation of robust optical absorption at 2.45 eV.

We have also studied the effect of external electric field on the band edge states, band alignment, and the optical and fundamental band gaps of the BiVO₄/g-C₃N₄ heterostructures. The band edge states of the BiVO₄ and g-C₃N₄ subsystems respond

very differently with the applied electric field, resulting in electric-field tunable band offsets and band gap of the BiVO₄/g-C₃N₄ heterostructures. The fundamental gap can be widely tuned from over 2.0 eV to zero, suggesting an electric-field induced semiconductor-metal transition in these structures. The optical gap, although can also be tuned slightly by electric field from 2.0 to 2.5 eV, remains rather robust. This contrasting response of the fundamental and optical gap to electric field may be exploited in future experiments to optimize the optical absorption and carrier separation dynamics in these heterostructures for photoelectrochemical catalysis applications.

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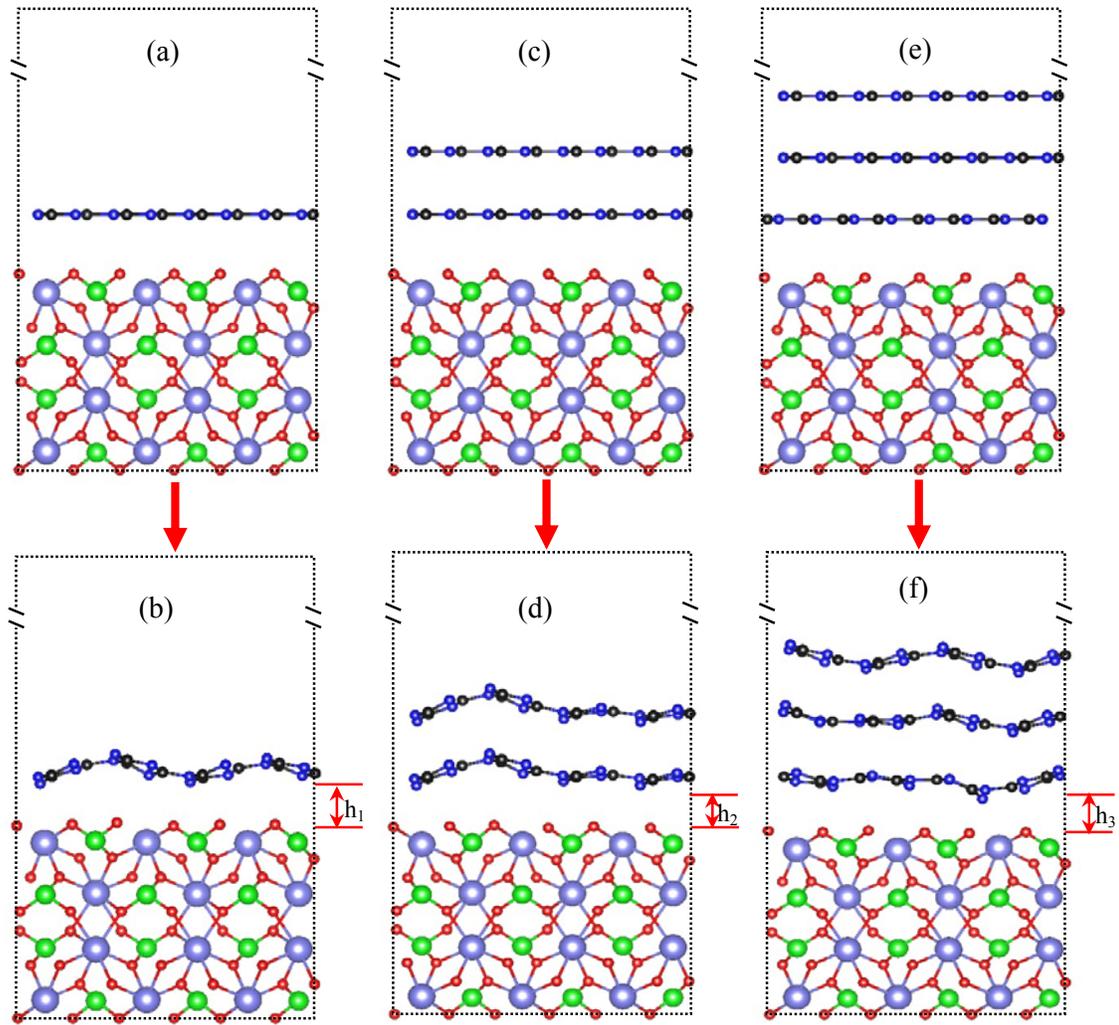


Fig. 1. Side view of the BiVO₄/SL-g-C₃N₄, BiVO₄/BL-g-C₃N₄, and BiVO₄/TL-g-C₃N₄ heterostructure: (a), (c), (e) are structures before optimization and (b), (d), (f) are after optimization, respectively. Red, green, light blue, blue and black balls represent O, V, Bi, N and C atoms, respectively. The blue arrows indicate the direction of the applied electric field.

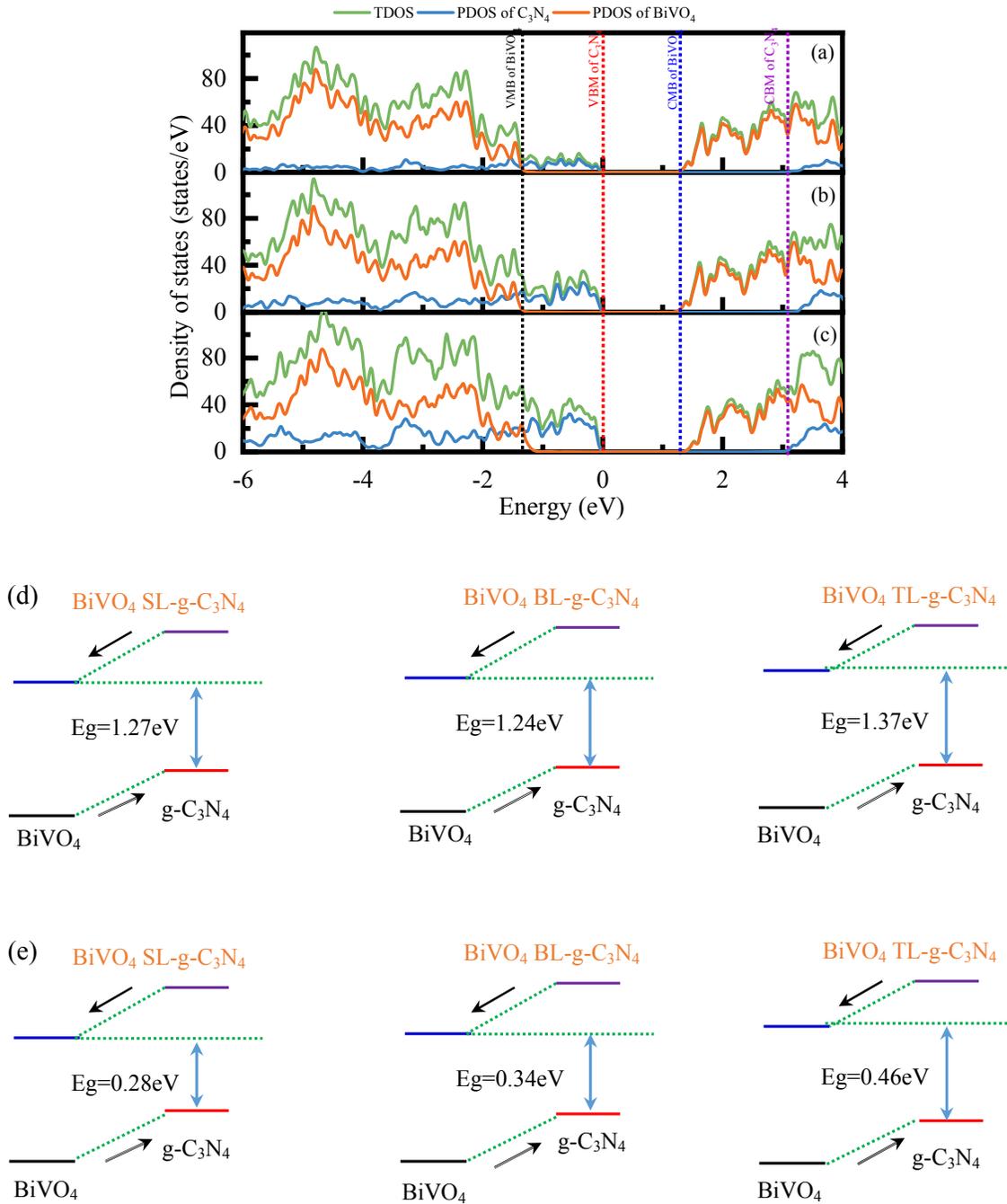


Fig. 2. Calculated TDOS and the corresponding PDOS of the C₃N₄ and BiVO₄ subsystems for (a) BiVO₄/SL-g-C₃N₄, (b) BiVO₄/BL-g-C₃N₄, and (c) BiVO₄/TL-g-C₃N₄ heterojunction using the HSE06 functional. (d) Band alignment of the heterojunctions obtained from the PDOS analysis using the HSE06 functional. (e) Band alignment obtained using the PBE functional. Relevant electronic parameters are also given in the figure. The position of the VBM is placed at zero for easy comparison.

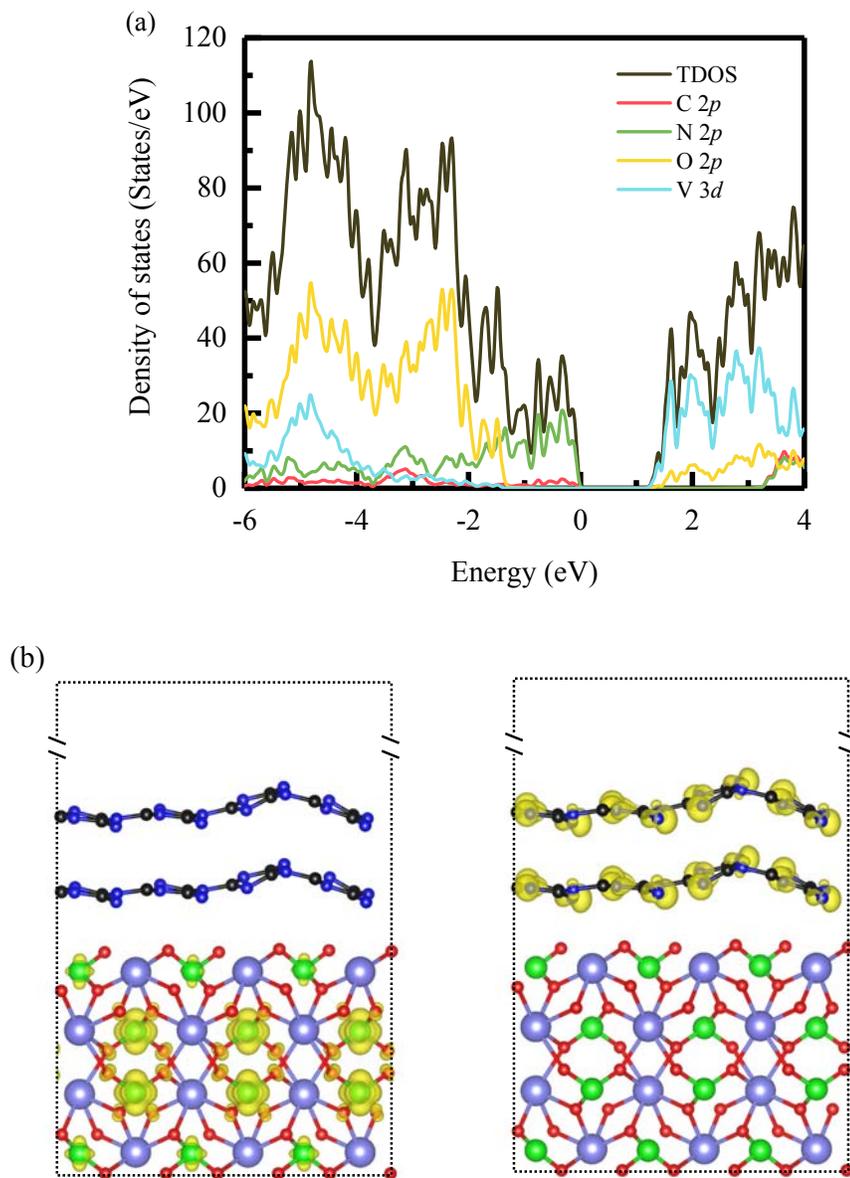


Fig. 3. (a) Calculated TDOS and atomically resolved PDOS of the $\text{BiVO}_4/\text{BL-g-C}_3\text{N}_4$ heterojunction using the HSE06 functional. Only dominant contributions from atomic states are shown in the figure. The VBM is placed at zero. (b) Isosurface charge density plots for the CBM (left panel) and VBM (right panel) in $\text{BiVO}_4/\text{BL-g-C}_3\text{N}_4$ with an isosurface value of 0.02 e/au^2 .

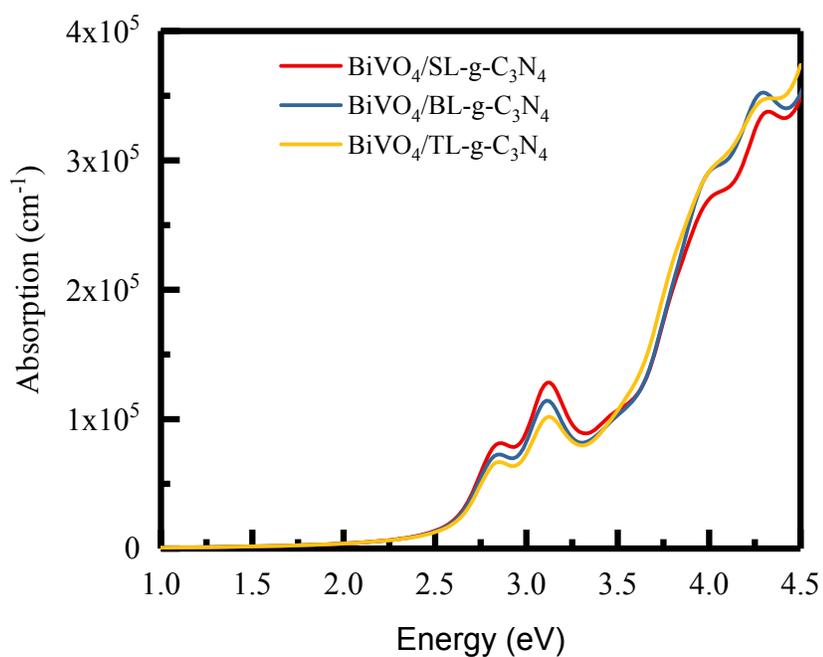


Fig. 4. Absorption coefficients of $\text{BiVO}_4/\text{SL-g-C}_3\text{N}_4$, $\text{BiVO}_4/\text{BL-g-C}_3\text{N}_4$, and $\text{BiVO}_4/\text{TL-g-C}_3\text{N}_4$ heterojunctions calculated using the HSE06 functional.

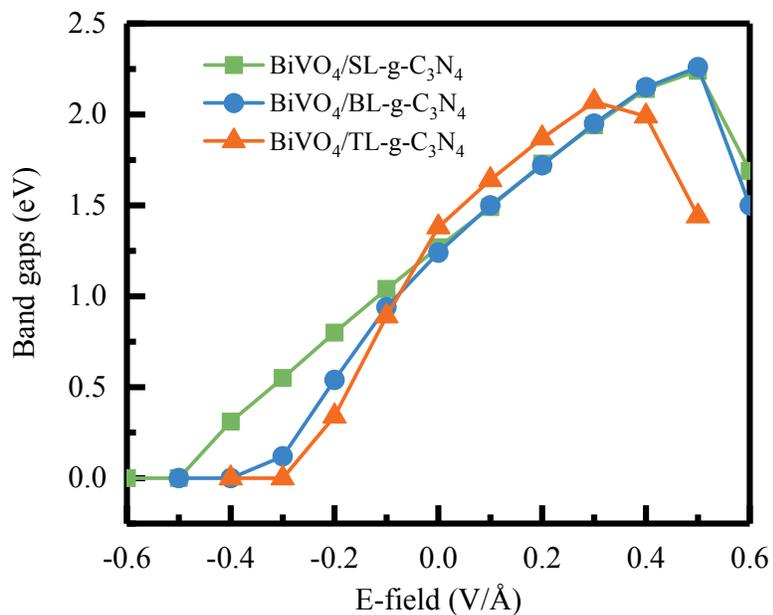


Fig. 5. Calculated fundamental band gaps of $\text{BiVO}_4/\text{SL-g-C}_3\text{N}_4$, $\text{BiVO}_4/\text{BL-g-C}_3\text{N}_4$, and $\text{BiVO}_4/\text{TL-g-C}_3\text{N}_4$ heterostructure as a function of the external field.

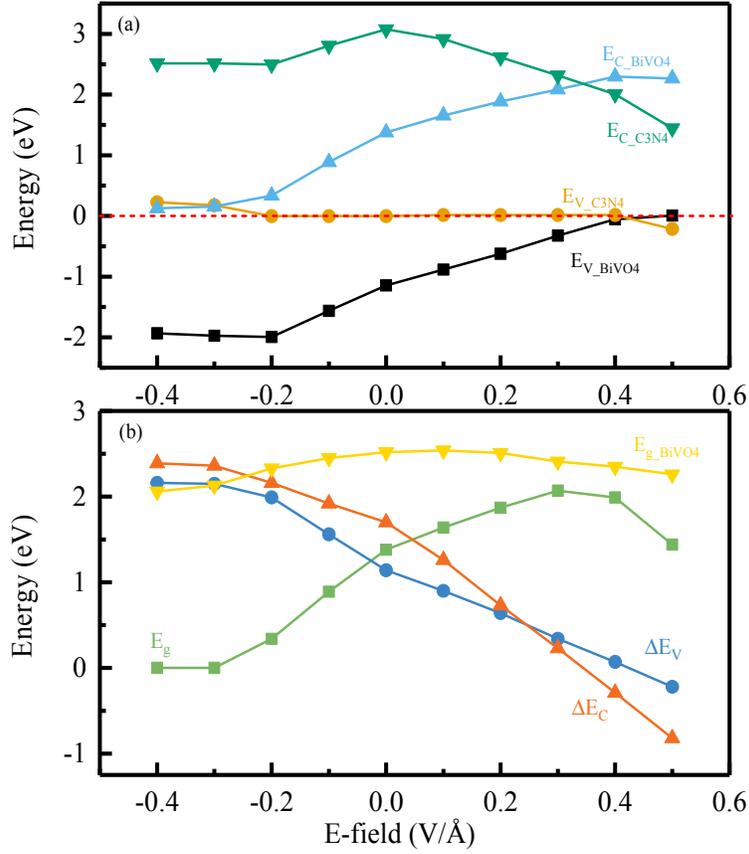


Fig. 6. (a) Band edge positions of the BiVO_4 and $\text{g-C}_3\text{N}_4$ subsystems in the $\text{BiVO}_4/\text{TL-g-C}_3\text{N}_4$ heterostructure as a function of the external field E . E_{C_BiVO4} (E_{C_g-C3N4}) and E_{V_BiVO4} (E_{V_g-C3N4}) are the CBM and VBM of BiVO_4 ($\text{g-C}_3\text{N}_4$) in the $\text{BiVO}_4/\text{TL-g-C}_3\text{N}_4$ heterostructure. The position of the VBM at zero field is placed at zero. (b) Evolution of the fundamental band gap (E_g), optical gap of the BiVO_4 subsystem (E_{g_BiVO4}) and the band offsets of $\text{BiVO}_4/\text{TL-g-C}_3\text{N}_4$ heterostructure as a function of the external field E .

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