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High thermoelectric power factor in intermetallic CoSi arises from energy filtering of electrons by phonon scattering

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Intermetallic compounds are usually poor thermoelectrics due to high electronic densities-of-states at the Fermi level and concomitantly low Seebeck coefficients. However, intermetallic *B20*-type CoSi has been experimentally shown to attain remarkably large negative values of the Seebeck coefficient. We provide a theoretical explanation for this surprising fact using state-of-the-art first-principles calculations with explicit treatment of electron-phonon interactions. We find that the unique band structure of CoSi, which has both massless and heavy fermion bands near the Fermi level, facilitates strong scattering of the low-energy electrons by phonons into the heavy band, resulting in effective energy filtering and high thermal voltage. Our study predicts that a very large thermoelectric power factor of $80 \mu\text{W cm}^{-1} \text{K}^{-2}$ or higher is experimentally accessible in the $300 \sim 600 \text{ K}$ range and highlights a general principle for identifying intermetallic compounds with large thermopower.

I. INTRODUCTION

Promising advances have been made in the last decade towards increasing the efficiency of thermoelectric materials for their potential applications in waste-heat recovery and thermal cooling [1–5]. The thermoelectric efficiency is characterized by the figure of merit defined as $zT = \sigma S^2 T / (\kappa_e + \kappa_l)$. Here, S is the Seebeck coefficient, σ is electrical conductivity, κ_e and κ_l are, respectively, thermal conductivities due to electrons and lattice vibrations; σS^2 is referred to as the thermoelectric power factor (PF). The central challenge is the simultaneous optimization of these properties, since their changes in response to design parameters often have competing (“contraindicated”) effects on zT [1, 2, 6]. The relatively decoupled relation between the electronic conductivity and phonon-mediated heat transport has led to several major successes in improving zT by reducing κ_l . Enhancement of the phonon scattering by utilizing strong intrinsic anharmonicity, nanostructures, and localized phonon modes has succeeded in significant reduction of κ_l [7–11], sometimes to as low as the amorphous limit [12]. The general consensus is that further improvement in zT must come from the enhancement of the PF.

It is well known that sharply varying electronic density-of-states (DOS) near the Fermi level greatly benefits S and the PF [13, 14]. The underlying mechanism is best illustrated by the well-known Mott formula [15], which for metals and heavily doped semiconductors sim-

plifies to

$$S = -\frac{\pi^2 k_B^2 T}{3e} \frac{d \ln \sigma(E)}{dE} = -\frac{\pi^2 k_B^2 T}{3e} \left[\frac{N'(E)}{N(E)} + \frac{\langle v^2(E) \rangle'}{\langle v^2(E) \rangle} + \frac{\tau'(E)}{\tau(E)} \right], \quad (1)$$

with the transport distribution function $\sigma(E) = e\tau(E)N(E)\langle v^2(E) \rangle$, where $N(E)$, $\tau(E)$ and $\langle v^2(E) \rangle$ are energy-dependent DOS, carrier lifetime, and mean of the squared group velocity, respectively. Clearly, large $N'(E)$ leads to high S . Ideas have been proposed to take advantage of this effect, such as designing for quantum confinement [16], introducing resonant impurity levels “virtual bound states”) [14, 17], aligning light and heavy band pockets, and increasing valley degeneracy [18, 19]. These methods, however, are limited to semiconductors, which have inherent band gaps that effectively separate the contributions of holes from those of electrons. Intermetallics naturally lack such gaps, allowing mutually excited electrons and holes to negate each others’ contributions, leading to negligible S . Yet, since high electrical conductivity is usually guaranteed for intermetallics, even a modest improvement in S could lead to very high PF. The question is how such an improvement can be made in spite of the unfavorable band structures.

We observe from Eq. (1) that while (i) the first two terms in the square brackets are fully determined by the static electronic band structure, (ii) the remaining term $\tau'(E)/\tau(E)$ is governed by dynamical processes, namely carrier scattering mechanisms such as electron-phonon interaction (EPI), ionized impurity and defect scattering. Then another way to increase S is for $\tau'(E)/\tau(E)$ to be large via preferential scattering of low-energy electrons, a phenomenon commonly known as electron energy filtering [14, 20]. To engineer strongly energy-dependent scattering, experimental studies have used “counter-doping” or potential energy barriers in 2D structures [21, 22],

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but these only led to limited success. A question remains whether an intrinsic scattering process, such as EPI, can lead to strong enough energy filtering such that the $\tau'(E)/\tau(E)$ term dominates Eq. (1). Recently, it has been proposed by Xu *et al.* [23] that sizable S associated with boundary states in topological insulators is theoretically achievable, which arises from the strong energy dependence of the lifetime caused by edge-bulk interactions [23]. However, such effects have been hardly investigated and reported in conventional bulk thermoelectrics.

In this work, we report that the $B20$ -type intermetallic CoSi exhibits strong EPI near the Fermi level that scatters low-energy electrons, thereby attaining large negative S and high PF. Though experimental studies have measured these previously [24–27], the underlying mechanism has not yet been well understood. Through state-of-the-art first-principles calculations, we attribute the strong EPI to the presence of a heavy band crossing the linear, massless (Dirac-like) bands just above the Fermi level, offering a scattering path for low-energy electrons. The band also bends below the Fermi level rather than above, providing a large phase space for hole scattering by phonons across a wide energy range but allowing electrons to maintain generally high lifetimes. Combined with large Fermi velocities of the massless bands, a remarkable power factor higher than $80 \mu\text{W cm}^{-1} \text{K}^{-2}$ is predicted at temperatures higher than 300 K. Our study constitutes a proof of concept that coexistence of massless and heavy bands can lead to very high PFs in intermetallics.

II. THEORY AND COMPUTATIONAL DETAILS

Electron transport coefficients were calculated using the semiclassical Boltzmann transport equation (BTE) under relaxation time approximation (RTA) [28–30]. The key quantity required to compute Seebeck coefficient S and electrical conductivity σ is the transport distribution function $\sigma(E)$

$$\sigma(E) = \frac{1}{N} \sum_{i,\mathbf{k}} e^2 \tau_{i,\mathbf{k}} \mathbf{v}_{i,\mathbf{k}} \otimes \mathbf{v}_{i,\mathbf{k}} \delta(E - E_{i,\mathbf{k}}), \quad (2)$$

where N , e , $\tau_{i,\mathbf{k}}$, $E_{i,\mathbf{k}}$ and $\mathbf{v}_{i,\mathbf{k}}$ are the number of \mathbf{k} -points sampled, absolute charge of an electron, lifetime, energy and group velocity for electronic state with band and wave vector indexed by i and \mathbf{k} , respectively. The temperature T and chemical potential μ dependent S and σ are

$$S(T, \mu) = -\frac{1}{eT} \frac{\int \sigma(E) (E - \mu) \left(\frac{-\partial f(T, E)}{\partial E} \right) dE}{\int \sigma(E) \left(\frac{-\partial f(T, E)}{\partial E} \right) dE}, \quad (3)$$

and

$$\sigma(T, \mu) = \frac{1}{\Omega} \int \sigma(E) \left[-\frac{\partial f(T, E)}{\partial E} \right] dE, \quad (4)$$

where Ω is the volume of unit cell and $f(T, E)$ is the Fermi-Dirac distribution. Since CoSi is metallic, carriers are expected to be dominantly scattered via interactions with phonons at finite temperature. Therefore, $\tau_{i,\mathbf{k}}$ can be estimated using the imaginary part of electron self-energy from the first-order electron-phonon diagrams [31, 32],

$$\begin{aligned} \frac{1}{\tau_{i,\mathbf{k}}} = & \frac{2\pi}{\hbar} \sum_{j,\nu} \int_{BZ} \frac{d\mathbf{q}}{\Omega_{BZ}} |g_{ji,\nu}(\mathbf{k}, \mathbf{q})|^2 \left(1 - \frac{\mathbf{v}_{\mathbf{k}} \cdot \mathbf{v}_{\mathbf{k}+\mathbf{q}}}{|\mathbf{v}_{\mathbf{k}}| |\mathbf{v}_{\mathbf{k}+\mathbf{q}}|} \right) \\ & \times [(n_{\nu,\mathbf{q}} + f_{j,\mathbf{k}+\mathbf{q}}) \delta(E_{i,\mathbf{k}} + \omega_{\nu,\mathbf{q}} - E_{j,\mathbf{k}+\mathbf{q}}) \\ & + (1 + n_{\nu,\mathbf{q}} - f_{j,\mathbf{k}+\mathbf{q}}) \delta(E_{i,\mathbf{k}} - \omega_{\nu,\mathbf{q}} - E_{j,\mathbf{k}+\mathbf{q}})], \end{aligned} \quad (5)$$

where ν , \mathbf{q} , n and ω are phonon mode index, wave vector, population and frequency, respectively. The velocity factor $\left(1 - \frac{\mathbf{v}_{\mathbf{k}} \cdot \mathbf{v}_{\mathbf{k}+\mathbf{q}}}{|\mathbf{v}_{\mathbf{k}}| |\mathbf{v}_{\mathbf{k}+\mathbf{q}}|} \right)$ defines the momentum relaxation time in the BTE [31] and $g_{ji,\nu}(\mathbf{k}, \mathbf{q})$ is EPI matrix element.

We used QUANTUM ESPRESSO [33, 34] to perform electronic structure calculations based on density function theory [35]. Troullier-Martins norm-conserving pseudopotentials [36] using the Perdew-Burke-Ernzerhof (PBE) [37] exchange-correlation (xc) functional [38] within the generalized gradient approximation (GGA) [39] was adopted. A kinetic energy cutoff of 75 Ry with Methfessel-Paxton smearing [40] width of 0.015 Rydberg and Monkhorst-Pack grids of $8 \times 8 \times 8$ for \mathbf{k} -point sampling were used to ensure the convergence of total energy in self-consistent calculations. The lattice constant of the fully relaxed structure is 4.465 Å, which is in good agreement with experimentally measured value of 4.450 Å [41]. The slight overestimation of about 0.3% is typical within GGA. The band structure accounting for spin-orbit coupling was calculated using the fully relativistic pseudopotentials constructed using ONCVSP package [42].

The relaxation times limited by EPI were computed using the EPW package [32, 43, 44], which utilizes maximally localized Wannier functions (MLWFs) for efficient interpolation of EPI matrix elements onto a fine \mathbf{k} -point mesh [32, 45–49]. This interpolation scheme yields accurate EPI matrix element at arbitrary sets of electron and phonon wavevectors at a much less computational cost compared to direct linear response calculations, thus allowing dense sampling in both electron and phonon momentum space and ensuring good convergence of electron self-energy. Afterwards, the momentum- and band-resolved relaxation time, i.e. $\tau_{i,\mathbf{k}}$ was used in BoltzTrap [29] to compute S and σ using densely sampled \mathbf{k} -point and tetrahedron smearing method [50]. Hereinafter we refer to the results obtained from this computational scheme as RTA. For detailed description of the theory and further technical details, refer to the supplemental material [51].

To further elucidate the impact of the energy dependence of $\tau(E)$ on S , we also performed calculations under

two other frequently used approximations, namely, (i) the constant relaxation time approximation (CRTA) where a single effective relaxation time is used in Eq. (2) and (ii) the DOS^{-1} approximation which assumes that the relaxation time is only energy dependent and scales inversely to DOS. The DOS^{-1} approximation is generally superior to CRTA since it at least approximates the EPI phase space in evaluating $\tau(E)$, and has been used by Xu *et al.* to successfully explain the nontrivial origin of positive S observed in lithium [52].

III. RESULTS AND DISCUSSIONS

A. Crystal and electronic structures

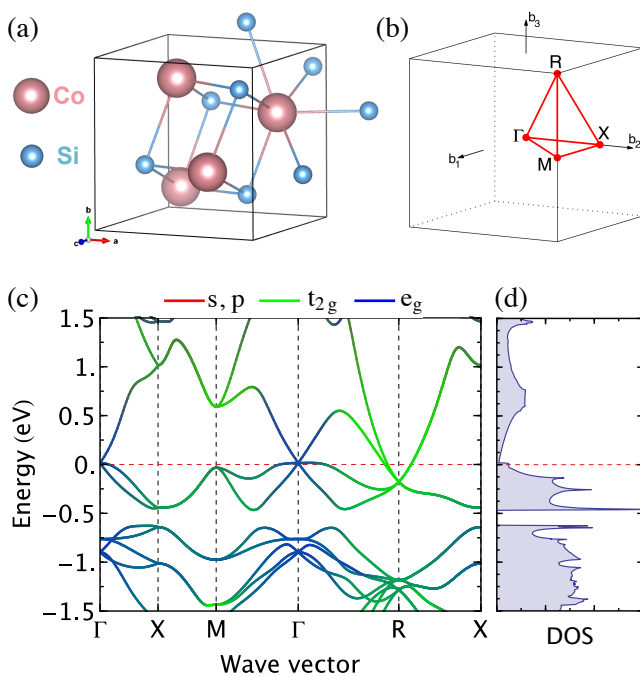


FIG. 1. (a) Crystal structure, (b) Brillouin zone with high symmetry points, (c) Electronic band structure and (d) Density of states (DOS) of $B20$ -type CoSi. The Co and Si atoms are colored in red and blue respectively. The band structure is color coded according to different orbitals shown in the legend, namely, s , p , e_g and t_{2g} states.

The $B20$ -type CoSi belongs to space group $P2_13$, bearing a simple cubic structure with 4 Co and 4 Si atoms in a primitive cell, as shown in Fig. 1(a). The corresponding Brillouin zone is displayed in Fig. 1(b). We plot the band structure projected onto s , p , e_g and t_{2g} states in Fig. 1(c). Near the Fermi level (± 1.5 eV), the bands are mainly composed of Co $3d$ states. Away from the Γ point, the band character shifts from e_g to t_{2g} states. The point of interest is that massless bands and a heavy band appear at and around the Γ point near the Fermi level, giving rise to a quadratic increase in DOS followed by a

sharp step [see Fig. 1(d)]. Spin-orbit coupling is found to split the energies of the linear bands slightly, but largely preserve the Dirac-like and flat bands (see Fig. S1 in supplemental material [51]). We did not include spin-orbit coupling in evaluating EPI due to the formidable computational cost and the minor effect on the band structure. It is worth noting that, however, the presence of SOC could induce nontrivial topology of electronic structure in $B20$ -type CoSi, which has been recently reported by Tang *et al.* [53].

B. Seebeck coefficient, resistivity and power factor

The calculated S under the CRTA, RTA and DOS^{-1} approximation compared with experimental measurements are shown in Fig. 2 (a). We see that the CRTA yields small positive S and that changes sign to negative near 500 K. The positive S seems intuitively consistent with the larger DOS below the Fermi level than above. In contrast, all experimental measurements display negative S from modest $20 \mu\text{V/K}$ at 100 K to much larger $80 \mu\text{V/K}$ at 300 K and above. We find that the RTA results, which fully account for the momentum- and energy-resolved EPI, agree excellently with experiments and reproduce the observed temperature dependence of S . The DOS^{-1} approximation, which only accounts for the EPI phase space, is a significant improvement upon the CRTA and leads to S comparable with that obtained by the RTA, save for the overestimation of S at low temperatures (≈ 100 K).

To further verify the RTA results, we compare the predicted and experimentally measured hole-doping-induced sign change of S as a function of the Al substitution ratio on the Si site [see Fig. 2 (b)]. We find that 4% Al substitution is the critical point that induces a sign change of S from negative to positive, again agreeing well with experiments [54, 55]. At high Al concentration ($>10\%$) the calculated S is about one half of the experimental values [54, 55]. We ascribe this discrepancy mainly to the possible distortions in the electronic structure due to heavy doping. Fig. 2 (c) compares the calculated and experimental electrical resistivity. Clearly our calculations agree better with measurements performed on single crystals [56], while polycrystalline samples exhibit higher resistivity due to grain boundaries [25, 26]. Experimentally measured values of the PF vary widely, as shown in Fig. 2 (d), but our calculations agree reasonably well with Ref. [26], showing that a maximum PF of about $80 \mu\text{W cm}^{-1} \text{K}^{-2}$ for pristine CoSi is obtainable at 600 K.

Having confirmed the validity of RTA, we proceed to clarify the origin of the large negative S . A previous theoretical study on the $B20$ -type CoGe with similar electronic structure has concluded that the large negative S originates from the asymmetric band structure about the Fermi level [57]. However, without considering energy-dependent carrier lifetimes, temperature and

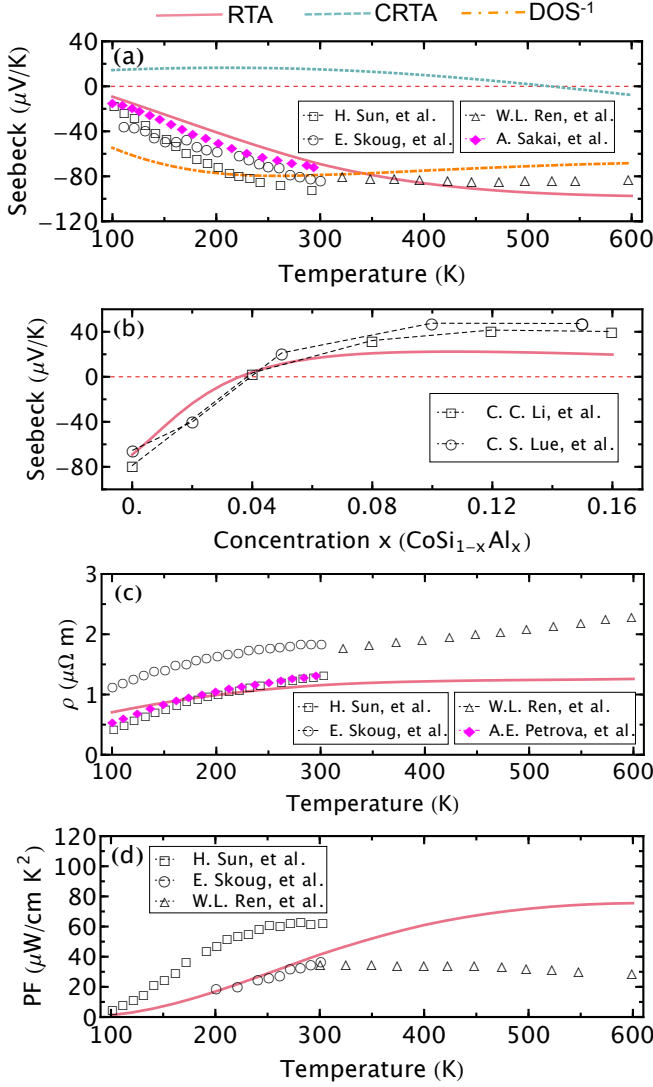


FIG. 2. (a) Calculated temperature-dependent Seebeck coefficient of pristine CoSi under RTA (red solid lines), CRTA (blue dashed lines) and DOS^{-1} approximation (orange dash-dotted lines) in comparison with experimental measurements [24–27]. (b) Calculated Seebeck coefficient of $\text{CoSi}_{1-x}\text{Al}_x$ at various fractions of Al substitution on Si site at 300 K compared with experiments [54, 55]. The black dashed lines are given as guides to the eye. (c) Calculated temperature-dependent electrical resistivity of pristine CoSi in comparison with experiments [24–26, 56]. (d) Calculated temperature-dependent power factor of pristine CoSi compared with experimental measurements [24–26]. In (a) and (c) experimental measurements performed on single crystals are denoted by magenta solid diamonds.

doping dependencies deviate considerably from experimental results. A key quantity that determines S and σ [see Eq. (3) and (4)] is the transport distribution function $\sigma(E)$. For S to be large, asymmetric $\sigma(E)$ is required while for σ to be large, an overall high $\sigma(E)$ in the energy window spanned by the Fermi-Dirac distribution near the Fermi level is all that is needed. Fig. 3 (a) displays the

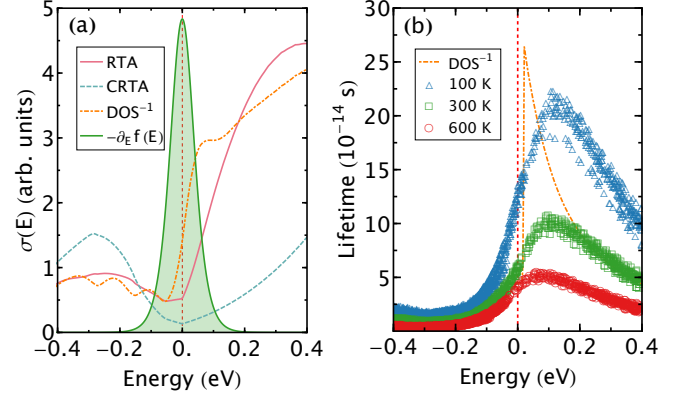


FIG. 3. (a) Calculated transport distribution function $\sigma(E)$ under RTA (red solid lines), CRTA (blue dashed lines) and DOS^{-1} approximation (orange dash-dotted lines) at 300 K. The light green shaped area indicates the energy window restricted by the energy derivative of Fermi-Dirac distribution. (b) Calculated energy-dependent carrier lifetimes at 100 K (blue triangles), 300 K (green squares) and 600 K (red circles) compared with scaled DOS^{-1} approximation (orange dash-dotted lines).

calculated $\sigma(E)$ under the CRTA, RTA and DOS^{-1} approximation at 300 K. It is evident that $\sigma(E)$ under the CRTA deviates significantly from those under the other two approximations. The latter two are strongly asymmetric about the Fermi level while the former fails to capture this. Since the CRTA already takes into account both the $N(E)$ and $\langle v^2(E) \rangle$ terms in Eq. (1), it is conclusive that the strong energy dependence of $\tau(E)$ plays the central role in determining the overall transport behavior, as evidenced by comparing the RTA and CRTA results in Fig. 2(a). Fig. 3 (b) clearly shows the otherwise long electron lifetimes dropping quickly near the Fermi level. Analysis of the band structure elucidates that it is the abrupt change of DOS slightly above the Fermi level, which arises from the flat band, that leads to preferential scattering of low-energy electrons in the massless bands (energy filtering), thus creating a large gradient in $\tau(E)$. In addition, the hole lifetimes are short due to the much larger hole DOS near the Fermi level, allowing electrons to dominate transport. The DOS^{-1} approximation, despite its simplicity, qualitatively reflects the energy dependence of $\tau(E)$ and thereby the asymmetric behavior of $\sigma(E)$. This suggests that EPI phase space probably dominates over the specific strength of EPI matrix elements in determining the energy dependence of carrier lifetimes.

Due to the abrupt change of DOS (see Fig. S5 in the supplemental material [51]), we also find it crucial to use an accurately determined Fermi level at each temperature by accounting for the Fermi-Dirac distribution. Our calculated resistivity exhibits unusual temperature dependence, that is, it is nearly independent of temperature above 300 K [see Fig. 2 (c)]. This contrasts

the typical behavior of increasing resistivity with temperature due to intensifying EPI. To no surprise, the reduction in lifetime with increased temperature is observed, as shown in Fig. 3 (b). However, the Fermi level also shifts towards higher energy due to the broadening Fermi-Dirac distribution (see Fig. S5 in the supplemental material [51]). Concomitantly, the mean Fermi velocity increases as more electrons are excited into the Dirac bands, partially counteracting the effect of lifetime reduction. The net effect is a nearly temperature-independent electrical resistivity from 300 to 600 K. To further confirm our theoretical prediction, experimental measurements on high-quality single crystal CoSi at temperatures above 300 K are suggested.

C. Effects of temperature and doping

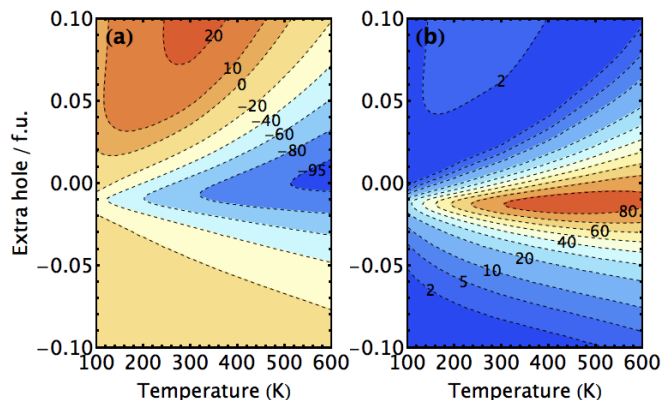


FIG. 4. Contour plot of calculated (a) Seebeck coefficient in $\mu\text{V K}^{-1}$ and (b) power factor in $\mu\text{W cm}^{-1} \text{K}^{-2}$ as a function of temperature and extra hole per formula unit ($\text{CoSi}_{1-x}\text{Al}_x$).

Finally, we map out the temperature and doping dependence of S and PF in Fig. 4. While S can still be optimized with slight electron doping at low temperatures, it is already nearly optimal in pristine CoSi at high temperatures. Increasing the temperature tends to enhance S for samples with both electron and hole doping. As we observed previously, hole doping tends to shift S to positive value as it reduces the asymmetric behavior of $\sigma(E)$ near the Fermi level. Concerning the PF, a value larger than $60 \mu\text{W cm}^{-1} \text{K}^{-2}$ can be achieved at temperature as low as 200 K with slight electron doping ($\approx 0.01/\text{f.u.}$). Increasing the temperature above 300 K can further lead to optimal PF of $80 \mu\text{W cm}^{-1} \text{K}^{-2}$ or higher, while hole doping tends to rapidly decrease PF. Heavy hole doping, which leads to small positive S and high electrical resistivity, significantly reduces the PF. Our study highlights the possibility to achieve large S and PF in metallic compounds with simultaneous occurrence of Dirac-like bands for mobile transport and a flat band as an energy filter near the Fermi level.

To further illustrate the high PF of CoSi, in Fig. 5

we compare the theoretically maximized temperature-dependent PF of CoSi to the PFs of two classical thermoelectric materials, namely, Bi_2Te_3 [58] and PbTe [59], and SnSe [60], a recently identified high-performance thermoelectric with record zT , as well as two other compounds FeNbSb [61] and YbAl_3 [62], which currently hold the record PFs for bulk semiconductors and intermetallics, respectively. Compared to Bi_2Te_3 , PbTe and SnSe , CoSi has a much higher PF across the whole temperature range from 300 to 600 K, majorly due to the low electrical resistivity in spite of relatively small Seebeck coefficient. Our theoretically optimized PF of CoSi is comparable with that of FeNbSb which is recently reported to possess a record output power density of about 22 W cm^{-2} [61]. The intermetallic YbAl_3 exhibits an ultrahigh PF at 300 K where the anomalous Seebeck coefficients arises from Kondo resonance [63] and virtual bound states [64]. However, the PF of YbAl_3 decreases sharply with increased temperature, making it significantly smaller than that of CoSi at 600 K. Considering the fact that the high PF of CoSi remains almost constant in the entire temperature range, CoSi may be used as Peltier cooler with potential application for electronic cooling, where both large PF and thermal conductivity are desired [65].

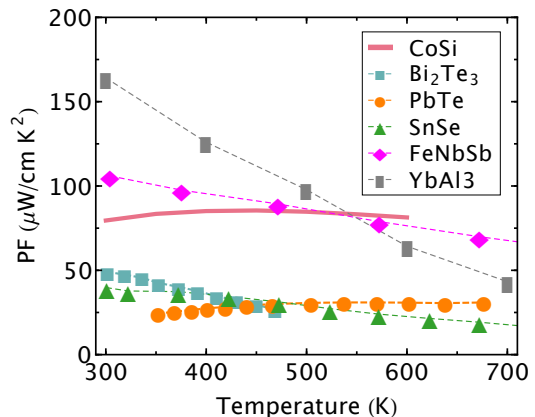


FIG. 5. Theoretically optimized temperature-dependent power factor of CoSi compared to several state-of-the-art thermoelectric materials with experimentally achieved high power factors, namely, semiconducting Bi_2Te_3 [58], PbTe [59], SnSe [60], FeNbSb [61] and intermetallic YbAl_3 [62].

D. General remarks

Instructive comparisons can be drawn between CoSi and some relevant cases. Recently, it has been brought to light that for Dirac-like bands, the electron mean free path (MFP) monotonically decreases with energy, leading to the concept of filtering electrons by long MFP, which automatically filters out low-energy electrons [66]. However, this has required nanostructuring of 10-nm grains in SnTe . Energy filtering by inherent EPI as in

CoSi does not require such an expensive process, another advantage. Nonetheless, some degree of nanostructuring of CoSi would still benefit zT by reducing lattice thermal conductivity, since its zT is severely handicapped by the large bulk κ_l that exceeds 10 W/mK at 300 K [67]. Furthermore, the coexistence of massless and heavy bands in CoSi is reminiscent of flat-and-dispersive, “low-dimensional” band structures, which has been a concept for high-PF semiconductor thermoelectrics [68, 69]. However, recent work suggests that such a band structure is not as beneficial as purely dispersive bands for semiconductors [70]. This owes partly to the fact that bipolar transport is not an issue for doped semiconductors, and S is naturally large. Therefore, while the flat band may contribute DOS and function as a low-energy electron filter, both to the potential extra benefit of S , it is eclipsed by the general surge in scattering rates (reduction of lifetimes), a severe detriment to mobility. Ultimately, the presence of the flat band is likely to cause more overall harm than good for the PF in semiconductors. This directly contrasts the case of intermetallics, for which the categorical need to sustain non-negligible S outweighs the loss of lifetimes due to scattering, especially since high conductivity is ensured.

IV. CONCLUSIONS

In summary, we have used a first-principles approach with explicit calculations of electron-phonon interaction to investigate the thermoelectric properties of the $B20$ -type intermetallic CoSi, with the main goal of identifying the origin of the large negative Seebeck coefficient.

We find that the large Seebeck coefficient arises from the heavily energy-dependent carrier lifetimes due to strong electron-phonon interaction. The strong electron-phonon interaction is invited by a heavy band that crosses linear bands near the Fermi level, providing a large phase space for electron-phonon scattering. Combined with the large Fermi velocity of the massless bands, remarkable power factors of $80 \mu\text{W cm}^{-1} \text{ K}$ or higher are predicted over a wide temperature range from 300 to 600 K with slight adjustments in the Fermi level. Our study shows that efficient energy filtering by electron-phonon interactions can generate large Seebeck coefficient and high power factor in metallic compounds. We hope that these results will serve as a motivation for renewed efforts in identifying high-performance thermoelectrics among intermetallic compounds.

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