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Transverse Measurements of Polarization in Optically-Pumped Rb Vapor Cells

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Abstract: We have developed a simple, novel, heuristic method for determining the polarization of an optically-pumped alkali-metal vapor. A linearly polarized probe beam traverses a vapor cell perpendicular to the pump beam propagation direction, and the transmission is monitored for orthogonal linear polarizations. As the probe beam is scanned in frequency across the D_1 transition, its linear-polarization-dependent transmission can be used as a measure of the atomic orientation of the vapor. We analyze these transmission differences and their dependence on the alkali number density in the vapor.

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I. Introduction

Optical pumping of alkali-metal vapor is ubiquitous in atomic physics and is used for a variety of applications. Among these are storage of light [1]; atomic clocks [2] and magnetometers [3]; the production of polarized ions [4, 5, 6], neutrons [7], and solids [8]; gas targets for nuclear physics studies [9], and the generation of polarized noble gases through spin-exchange optical pumping [10]. Each of these experiments requires significantly different operating conditions. For example, storage of light in a warm alkali vapor is effected with little or no buffer gas and with spectrally narrow, low-power lasers, while systems that use spin-exchange optical pumping to generate polarized noble gases tend to use high buffer gas pressures (~1000 Torr) and broad, high-power lasers. The work reported here deals with a third regime, using somewhat broad, high-power lasers with low pressures (0.1-20 Torr) of buffer gas and an alkalimetal density of 10¹² to 10¹³ cm⁻³ [11 - 13]. Among other possible applications, such as gas-cell atomic clocks [14], these conditions are necessary to generate a beam of electrons polarized through spin exchange with a spin-polarized optically-pumped alkali target [12]. The necessity of passing the electrons through the alkali (Rb) vapor requires that the buffer gas pressures be modest to maintain an appreciable electron current. We hope to use this technology to produce a "turnkey" polarized electron source.

The Rb polarization, P_{Rb} , in its ground state is given by

$$P_{Rb} = \frac{n_{\uparrow} - n_{\downarrow}}{n_{\uparrow} + n_{\downarrow}} , \qquad (1)$$

where n_{\uparrow} (n_{\downarrow}) is the number of atoms with $m_J = \pm 1/2$ (-1/2) in the Rb 5s ${}^{2}S_{1/2}$ fine-structure level. This is equivalent to the Rb valence electron polarization and is typically determined by Faraday rotation measurements [13, 15]. In such a measurement, a linearly-polarized probe beam well detuned from line-center is passed through a cell of polarized vapor in a direction near parallel to the pumping beam. The angle of rotation of the linear polarization, $\Delta \phi_{P}$, is measured to determine the polarization of the sample with the equation

$$P_{Rb} = \frac{56\pi\delta(\Delta\phi_p)}{3\lambda_0^{2}\Gamma_{nat}LN} , \qquad (2)$$

where *N* is the Rb number density, λ_0 is the Rb D_1 line-center wavelength, Γ_{nat} is the natural line-width of the transition, *L* is the length over which the probe interacts with the vapor, and δ is the detuning of the probe beam wavelength from the line-center.

In such a measurement, the spin-polarization is sampled along the entire length of the vapor through which the probe propagates. Thus Eq. 2 yields an average polarization along the cell length. Additionally, the measurement demands optical access through both ends of the vapor cell and can result in inconvenient configurations of optical elements in order to provide the required near-colinearity of the probe and pump beams.

We report here a new, simple, heuristic method to determine the polarization of an optically-pumped alkali-metal vapor, using a probe beam tuned to the D_1 transition and oriented perpendicular to the pump beam. This scheme is optically simple and has the advantage that it can provide spatially-resolved polarization information in cells containing moderate Rb density.

II. Method

The experimental setup we used in this work is shown both schematically (Fig. 1) and in more detail (Fig. 2). A circularly-polarized pump beam passed along the axis of a cylindrical vapor cell and was oriented parallel to an imposed magnetic field along the z quantization axis. A linearly-polarized probe beam was directed through the side of vapor cell, perpendicular to the pump beam. With a photodiode detector and digital oscilloscope, transmission *vs.* frequency profiles were obtained for the probe beam with its polarization axis parallel to the *z*-axis (π linear polarization) and with its polarization axis normal to both the pump and probe propagation directions (π_y linear polarization). Typical data for the probe transmission profile are shown in Fig. 3.

The profile of the π probe was subtracted from that of the π_y probe to give a difference trace *D* which provides information about *P*_{*Rb*}. As seen in Fig. 3, two

particularly prominent features in the difference profile correspond to π_y light being more strongly absorbed than π light near the ⁸⁷Rb $F = 2 \rightarrow F = 1$ transition and π light being more strongly absorbed than π_y light near the ⁸⁷Rb $F = 3 \rightarrow F = 3$ transition. The extrema of these features are referred to as D_{min} and D_{max} , respectively.

Fig. 4 depicts the allowed atomic transitions for polarized light in the dipole approximation. If $\sigma^+(\sigma^-)$ circularly-polarized light is absorbed by an atom, it will cause an electronic transition with $\Delta m_F = +1$ (-1). Linearly-polarized π light drives a $\Delta m_F = 0$ transition, while π_y light drives a transition to a state which is a coherent superposition of $\Delta m_F = +1$ and $\Delta m_F = -1$ states.

The data of Fig. 3 can be explained qualitatively in the following way. Consider a Rb vapor for which we label the ground and excited states F_g and F_e , respectively. If the vapor is maximally-polarized, with all atoms having $|m_F| = F$ in the ground state, the population will not affect a π -polarized probe beam tuned to a transition with $F_g >$ F_e , but can absorb π_y light of the same frequency (Fig. 5a). This explains the negative feature associated with D_{min} near the ⁸⁷Rb $F = 2 \rightarrow F = 1$ transition. Fig. 5b illustrates the case of the probe tuned to a transition for which $F_g = F_e$, in the same spin-polarized vapor. For atoms having $m_F = +F$ ($m_F = -F$), absorption of the π_y light component giving the transition $\Delta m_F = +1$ ($\Delta m_F = -1$) is not allowed, but the absorption of π light displays no such suppression. Thus, the positive feature associated with D_{max} occurs near the ⁸⁵Rb *F* = 3 \rightarrow *F* = 3 transition.

III. Atomic Orientation and Alignment

In the excitation of atoms by light, two important quantities are the atom's orientation (*O*):

$$0 = \frac{\sum_{m_F} m_F n_{m_F}}{\sqrt{F(F+1)} \sum_{m_F} n_{m_F}} ,$$
 (3)

a measure of its magnetic dipole moment, and alignment (A):

$$A = \frac{\sum_{m_F} [3m_F^2 - F(F+1)] n_{m_F}}{F(F+1) \sum_{m_F} n_{m_F}},$$
(4)

a measure of its electric quadrupole moment [16, 17]. In the above equations, m_F and F are the usual quantum state numbers for the atom's total angular momentum, and n_{m_F} is the population of the state with m_F . Eq. 3 is equivalent to Eq. 1, but with hyperfine states now shown explicitly. For an oriented atom, the state populations with $+m_F$ differ from those with $-m_F$. On the other hand, an aligned atom has unequal populations for different $|m_F|$ values [18]. Optical pumping of an alkali-metal vapor with circularly-polarized light will generally result in both an alignment and orientation of the atoms. In the dipole approximation, however, a vapor pumped with σ^+

polarized light will have the same alignment as a vapor pumped with σ ⁻ polarized light. Therefore, the $|m_F|$ distribution, i.e. alignment, is independent of pump helicity.

For both π and π_y light, the probability of photon absorption is independent of the sign of m_F [19]. Thus, monitoring their relative absorption yields information about the alignment of the sample, not its orientation. Indeed, our method cannot determine the sign of P_{Rb} . It is akin to the measurement of linear polarization (Stokes parameter *P*, P_1 , *M*/*I*, *Q*/*I*, *S*₁/*S*₀, η_3 , etc.) of fluorescence produced in a cylindrically-symmetric collision geometry, which uniquely determines alignment [16]. It is different because it is affected by absorption of the probe laser.

There are multiple population distributions yielding a given sample orientation, and likewise there are multiple ways to get a particular alignment. Thus, a one-to-one mapping between orientation and alignment does not exist. Consider, for example, a possible time evolution of state populations tending towards 100% polarization, illustrated in Fig. 6. In this scheme, the population migrates to a final extreme value of m_F in such a way that, for the populated states, $n_{m_F+1} - n_{m_F}$ is constant. Fig. 7 shows the alignment of this example as a function of its orientation. On the same graph is shown the alignment vs. orientation for a sample where the dominant process is spin exchange, a system that can be described by a spin-temperature [20] common in some regimes of optical pumping. The graph also displays the near-linear relationship between orientation and alignment that occurs with optical pumping under our conditions, derived from the individual Zeeman sublevel populations found with numerical calculations (described below). We note that, although it is fortunate that we are working in a regime where the orientation and alignment are almost proportional, this condition is not necessary for side-probing to serve as a useful indicator of orientation (and therefore P_{Rb}); the relationship between orientation and alignment will simply take a different functional form.

IV. Experimental Details

A ~10 W beam from a Coherent Verdi laser was used to pump a Spectra Physics 3900 Ti:sapphire laser. The output of this laser was ~1 mm in diameter with a typical power of 800 mW. The spectral profile of our pump laser was "trident-shaped" comprising three laser cavity modes equally spaced ~200 MHz apart. The beam passed through a clean-up linear polarizer and quarter-wave plate before entering a cylindrical test cell containing Rb vapor of natural isotopic abundance. The cell was 4.3 cm long and 2.5 cm in diameter and contained 10 Torr of N₂ buffer gas. A magnetic field of strength ~1 mT was applied by electromagnets along the direction of the pump beam to maintain the orientation of the polarized Rb. The pump beam was carefully aligned to within 2 degrees of the magnetic field direction, detuned positively (~2 GHz) from the center of the *D*₁ transition, and circularly polarized to > 99.5% to avoid the polarization reversal effect that has been observed in some systems lacking a "repump" laser [11, 21]. The temperature of the Rb cell was varied to alter *N*, and *P*_{*Rb*} was changed by adjusting the power of the pump laser beam. Both *P*_{*Rb*} and *N* were measured with Faraday rotation techniques [13, 15] and therefore represent quantities averaged over the cell length along the *z*-axis. We estimate the systematic uncertainty in both measurements to be ~10% due to the fact that we occasionally made measurements of polarization as high as 110%. Because polarization is inversely proportional to density, we assign the same uncertainty to our density measurements.

The probe laser (New Focus tunable diode Vortex laser, model 6017) had a spectral width of ~300 kHz. Its power was typically reduced to ~20 μ W. Using an infrared-sensitive camera, optimal overlap of pump and probe beams was achieved by comparing images of the cell when the pump was blocked and unblocked. Additionally, a separate investigation of *P*_{*Rb*} as a function of radial distance from the pump beam revealed that the probe was well within the region of maximum polarization.

Transmission profiles were obtained for both the π and π_y beam polarizations (Fig. 3). When scanning the probe frequency, the power varied somewhat, and the transmission changed due to etalon effects of the glass cell walls. This did not affect the overall results. The transmission signal was normalized to the maximum value of

the unabsorbed beam intensity occurring just to the right of the ⁸⁷Rb $F = 1 \rightarrow F = 2$ transition.

V. Model Calculations

To understand more quantitatively the relative absorption of the π - and π_{y} polarized probe across the frequency span, it is necessary to incorporate the sublevel-tosublevel relative transition probabilities of the different polarizations [22]. The system
was thus modeled by solving rate equations to describe each *F*, *m_F* ground- and excitedstate sublevel for ⁸⁵Rb and ⁸⁷Rb, and the transmission of the transverse probe beam for
each polarization state was calculated. These rate equations included the optical
pumping process by the pump beam, spontaneous emission, spin relaxation, and
optical pumping by the probe beam. We used the interpretive language Mathematica
to solve the rate equations. A sample equation for ⁸⁷Rb for one ground-state sublevel
population *n*₁, where *n*₁ = *n*(²S_{1/2}, *F*=2, *m_F* = -2), and a probe polarization of π_y is

$$\frac{\partial n_1}{\partial t} = \Gamma_{\text{pump}2 \to 2}(n_b - n_1) + \Gamma_{\text{pump}2 \to 1}(n_h - n_1) + A_{\text{Einstein}} \frac{(4n_a + 2n_b + 6n_h)}{12} + \Gamma_{\text{mix}}(N - n_1)$$

$$+\Gamma_{\text{probe2}\to2}\frac{(2n_b-2n_1)}{8} + \Gamma_{\text{probe2}\to1}\frac{(6n_h-6n_1)}{8}.$$
 (5)

Here, $n_b = n({}^2P_{1/2}, F=2, m_F = -1)$, $n_h = n({}^2P_{1/2}, F=1, m_F = -1)$, $n_a = n({}^2P_{1/2}, F=2, m_F = -2)$, A_{Einstein} is the spontaneous decay rate of 87 Rb, and the spin relaxation rate is Γ_{mix} . The optical pumping rate $\Gamma_{pump2\rightarrow 2}$ was calculated with an integral between the spectral profile of the laser and a Voigt profile convolution of the Doppler-broadened Gaussian line shape and collisionally-broadened Lorentzian line shape. Its value took into account the center frequency of the laser and the excited-state F = 2 level to ground-state F = 2 level frequencies. The other optical pump rates, $\Gamma_{pump2\rightarrow 1}$, $\Gamma_{probe2\rightarrow 2}$, and $\Gamma_{probe2\rightarrow 1}$, were defined similarly. Thus, we used sixteen equations to describe each of the ground-and excited-state sublevels of ⁸⁷Rb and twenty-four equations to describe ⁸⁵Rb, along with the normalization forcing the sum of all populations to equal *N*.

The calculations were simplified with a number of assumptions. Spin exchange collisions [21, 23, 24] within and between the isotopes were neglected; modeling the pumping with a broadband laser on atoms collisionally broadened by the buffer gas sufficiently describes the polarization of both isotopes [25, 26]. Previous work with this system indicates that 10 Torr of N₂ buffer gas substantially reduces problems associated with radiation trapping [12, 13], so such effects were not considered. The pump and probe lasers were approximated with spectrally-flat beams of width 550 MHz and 300 kHz, respectively, and their intensities were taken to be spatially flat in both radius and depth into the cell. We neglected individual velocity subgroups and described each atom with the Voigt profile idealized absorption line shape. The spin relaxation rate is the beam-crossing rate for atoms in vacuum joined smoothly to the beam-crossing rate for atoms in vacuum joined smoothly to the transition from the

molecular flow to diffusion regimes. Since spin-exchange collisions are not very important and we assumed a spatially-flat laser profile, our calculated populations are independent of *N*.

An example of the calculations of the transmission of the two orthogonal probe polarizations and the resultant D curve is shown in Fig. 8. The calculations nicely reproduce the main features of the difference curve, including the negative- and positive-going peaks associated with D_{min} and D_{max} .

VI. Results

The goal of this work is to find a simple, useful way to map out and monitor the polarization of an alkali-metal vapor. While our calculations reproduce the major features of the *D* curve in Fig. 3, it would be inconvenient to do real-time modeling of entire scans of both probe polarizations in order to extract values of P_{Rb} . Thus, we present a more heuristic method to determine the polarization using D_{min} and/or D_{max} and their correlation with P_{Rb} . We choose not to use the features that occur at positive detunings since they are inherently smaller and can exhibit complex behavior caused by the pump laser being in the same frequency range. In fact, in the limit of perfect Rb polarization, these features disappear altogether because they represent transitions out of the lower *F* level of the ground state, which is actively depleted by the optical pumping process.

The quantity D_{min} is plotted *vs.* P_{Rb} and is displayed in Fig. 9 along with values of D_{min} obtained from our model. Seven values of N between 10^{12} and 10^{13} cm⁻³ were investigated. For clarity, the results from only four densities are plotted; the remaining data is consistent with that shown. Our model fit the data better if we used N values twice what we measured, indicating N variation in the cell or a current problem with the model.

The two quantities P_{Rb} and D_{min} exhibit an approximately linear relationship, although for lower *N* the simple linear dependence fails at lower polarizations, yielding a non-zero value of the intercept, $D_{min}(P_{Rb} = 0; N)$. Notwithstanding this complication, a method to determine P_{Rb} by heuristically fitting the D_{min} data for a given *N* is suggested by the results of Fig. 9. Hyperbolic fits of the form

$$D_{min}(P_{Rb}, N)^2 = D_{min}(P_{Rb} = 0; N)^2 + P_{Rb}^2 * A(N)^2$$
(6)

adequately estimate D_{min} for our particular set of experimental parameters (Fig. 10). (Note that Eq. 6 can easily be rearranged to obtain P_{Rb} as a function of D_{min} .) To estimate the statistical uncertainties of our measurements, we assign a common uncertainty to the difference signal data for a given density to provide a reduced chi-squared value equal to one for the fit. This value is then used to calculate the uncertainties of the hyperbolic fit coefficients $D_{min}(P_{Rb} = 0; N)$ and A(N) shown in Fig. 10. The utility of this technique is limited by the size of the cell and the intensity of the probe beam. For $N\sigma_{\lambda}d \gg 1$, where σ_{λ} is the absorption cross-section at wavelength λ and d is the cell diameter, both polarizations are almost completely absorbed and their transmission difference becomes small compared to the experimental noise. Conversely, for $N\sigma_{\lambda}d \ll 1$, there is not enough absorption to reliably measure a difference signal. Experiments could easily be designed to obviate these problems.

Fig. 11 shows the intercept $D_{min}(P_{Rb} = 0; N)$ and the asymptotic slope A(N) of the hyperbolic fits for the data set shown in Fig. 10. For our experimental conditions, the N-dependence of these coefficients can be described empirically by

$$D_{min}(P_{Rb} = 0; N) = \frac{1}{E + F \cdot N}$$

$$\tag{7}$$

and

$$A(N) = \frac{1}{G + H \cdot N'} \tag{8}$$

where $E = 2.7 \pm 1.7$, $F = -5.6 \pm 1.5 \text{ cm}^3$, $G = -2.07 \pm 0.05$, and $H = -0.64 \pm 0.02 \text{ cm}^3$, and N is measured in units of 10^{12} cm⁻³. Eqs. 7 and 8 allow determination of the polarization based upon measured values of D_{min} and N. Different experimental configurations would of course require different fitting parameters. Both $D_{min}(P_{Rb} = 0; N)$ and $D_{min}(P_{Rb} = 1.0; N)$ are decreasing functions of number density in our experiment. At low densities, these quantities would be expected to increase with increasing N, and our model calculations confirm this. However, since our measurements are based upon a transmission signal near the D_1 absorption lines, all the probe light is absorbed for high N. Thus, the signal is attenuated and the values of $D_{min}(P_{Rb} = 0)$ and $D_{min}(P_{Rb} = 1.0)$ are reduced to zero, as shown in Fig. 12.

It is desirable to understand and eliminate the non-zero values of $D_{min}(P_{Rb} = 0)$. This behavior initially surprised us. The value of D_{min} is directly related to the atomic alignment in the system, as discussed earlier, but what causes this alignment in the absence of a pump beam? Although it is true that the longitudinal magnetic field breaks the y,z symmetry of the experiment, it is too weak (~1 mT) to produce the alignment we observe by itself. In other words, $kT \gg \Delta E$, where ΔE is a characteristic Rb Zeeman energy shift. We note that, strictly speaking, in the absence of any laserdriven process, a magnetic field, which is a pseudovector, must cause orientation.

In fact, $D_{min}(P_{Rb} = 0) \neq 0$ in the absence of a pump beam is caused by the probe itself. (This is different from the orientation caused by an intense, linearly-polarized side pump beam in the Paschen-Back regime [27]). When the probe is tuned to the ⁸⁷Rb $F = 2 \rightarrow F = 1$ transition (Fig. 5a) with π polarization, it can pump the atoms into the stretched state, or "hollow out" the z-basis m_F ground-state distribution for ⁸⁷Rb F = 2 atoms, leaving only m_F values equal to $\pm F$. At this transition frequency, the sample would become transparent to the π probe, but the π_y probe can always be absorbed. This differential absorption yields the non-zero $D_{min}(P_{Rb} = 0)$. Ground-state populations are maintained by the longitudinal (z-axis) magnetic field, which holds atoms in a given z-basis m_F state once they reach it by a photonic transition. This is equivalent to the classical picture of magnetic m_F dipoles precessing about the magnetic field. Only in the cases of a magnetic field aligned along $\hat{y} \pm \hat{z}$ or one that vanishes (i.e. is so small that any precession time is much longer than a characteristic depolarization time) will $D_{min}(P_{Rb} = 0)$ approach zero in the absence of a pump beam.

These considerations lead to two ways to avoid the offset of $D_{min}(P_{Rb} = 0)$ for measurements of low polarizations. First, a probe of very low intensity would not interfere with the polarization measurement. Fig. 13 shows the result of our model calculation indicating that $D_{min}(P_{Rb} = 0)$ approaches zero at sufficiently low probe powers. The detection sensitivity and the quality and curvature of our cell walls required probe intensities in the regime where the D_{min} intercept became measurable, but experiments could be designed with much lower probe intensities than those shown here.

A second way to eliminate the offset would be to choose a feature on the difference curve where the probe beam does not optically pump the sample, such as at D_{max} . The ⁸⁷Rb $F = 3 \rightarrow F = 3$ transition does not allow the probe to create a dark state for either π or π_y polarization states. Fig. 14 shows experimental data and model

calculations for the use of D_{max} to predict polarization. The results display a signal directly proportional to P_{Rb} without any offset at low P_{Rb} , even at probe laser intensities problematic for D_{min} measurements. Unfortunately, the model for D_{max} fails at higher densities where the location of D_{max} becomes ambiguous amongst the multiple positive peaks in the D curve. In future work we plan to study the efficacy of a D_{max} method more thoroughly.

Either a low probe power or use of D_{max} ensures a zero-intercept value of D for $P_{Rb} = 0$, enabling a measurement of P_{Rb} with a single N-dependent slope parameter. Having a signal directly proportional to P_{Rb} also opens the possibility of measurements fast enough to perform real-time tuning of P_{Rb} or mapping of the transverse spatial variation of P_{Rb} .

VII. Conclusion

We have demonstrated a heuristic method to determine P_{Rb} of an opticallypumped vapor by analyzing the difference of transmission for orthogonally linearlypolarized probe beams oriented perpendicular to the quantization axis. This transmission difference is understood qualitatively by considering the allowed photonic transitions for an atomic vapor that is polarized and quantitatively by detailed modeling of the polarized vapor with relevant rate equations. For measuring P_{Rb} , a system of given dimensions, buffer gas pressure, N, and probe intensity would first need calibration or modeling in order to determine P_{Rb} as a function of D_{min} or D_{max} . This scheme has advantages over traditional Faraday rotation in that it is relatively simple to set up and is compact. The method could map the spatial variation of the polarization in a cell, enables a polarization measurement if the cell is not accessible at both ends along the z-axis, and offers the potential of a fast, real-time indicator for optimizing the polarization of a sample.

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FIG. 1. (Color online) Schematic of the experimental setup. A circularly-polarized beam propagating along the z-axis optically pumps the alkali-metal vapor. A magnetic field is imposed along the z-axis. The transmission of a linearly-polarized, perpendicularly-oriented probe beam is measured with a photodiode detector for two polarizations: π (polarization axis parallel to the z-axis) and π_y (polarization axis parallel to the y-axis).



FIG. 2. (Color online) Apparatus details: (1) linear polarizer, (2) quarter-wave plate, (3) beam sampler, (4) photodiode.



FIG. 3. (Color online) Measured transmission for transverse π_y and π light and the difference signal (*D*) for a Rb density of 2.4·10¹² cm⁻³ with 10 Torr of N₂ buffer gas. The detunings from line center of the ground-to-excited hyperfine level transitions are indicated at the bottom of the graph; from left to right: ⁸⁷Rb F = 2 \rightarrow F = 1, ⁸⁷Rb 2 \rightarrow 2, ⁸⁵Rb 3 \rightarrow 2, ⁸⁵Rb 3 \rightarrow 3, ⁸⁵Rb 2 \rightarrow 2, ⁸⁵Rb 2 \rightarrow 3, ⁸⁷Rb 1 \rightarrow 1, ⁸⁷Rb 1 \rightarrow 2. The values of *D*_{min} and *D*_{max} are indicated.



FIG. 4. (Color online) Allowed atomic transitions for polarized light in the dipole approximation.



FIG. 5. (Color online) Allowed and forbidden transitions (the latter crossed out) from the ⁸⁷Rb F = 2, m_F = 2 ground state to a) the F = 1 excited state and b) F = 2 excited state driven by linearly-polarized transverse probe light. Transitions designations as in Fig. 4.



FIG. 6. (Color online) A possible evolution of state populations from an initially unpolarized state to a final, maximally-polarized one.



FIG. 7. (Color online) Correlation between alignment and orientation for three different state population evolution schemes.



FIG. 8. (Color online) Calculated transmission curves for a transverse 20 mW probe with polarizations π_y and π along with their difference curve (*D*). The calculations are for $N = 1.4 \cdot 10^{12}$ cm⁻³ and $P_{Rb} = 70\%$ in a cell of diameter 2.5 cm with 10 Torr N₂ buffer gas.



FIG. 9. (Color online) The negative of D_{min} plotted *vs.* P_{Rb} as measured by longitudinal Faraday rotation. The curves show our calculations of D_{min} ; the symbols correspond to our measurements with densities half those used in the calculations. Densities indicated in the legend are in units of 10^{12} cm⁻³.



FIG. 10. (Color online) The negative of D_{min} plotted *vs.* P_{Rb} measured by longitudinal Faraday rotation. A best fit curve for each density using Eq. 6 yielded the fit coefficients $D_{min}(P_{Rb} = 0)$ and *A* plotted in Fig. 11. Densities indicated in the legend are in units of 10^{12} cm⁻³.



FIG. 11. (Color online) Dependence of fit coefficients $-D_{min}(P_{Rb} = 0)$ and -A from Eq. 6 *vs.* Rb density. The fits shown above correspond to Eqs. 7 and 8.



FIG. 12. (Color online) The values of $-D_{min}(P_{Rb} = 0)$ (solid line) and $-D_{min}(P_{Rb} = 1.0)$ (dashed line) *vs.* P_{Rb} as a function of *N* for 50 µW probe power. The shaded area corresponds to the range of densities used in our experiments.



FIG. 13. (Color online) A sample of graphs showing the calculated value of the difference function *D* as a function of the probe laser detuning for a span of probe laser powers in the absence of a pump beam for $N = 4 \cdot 10^{12}$ cm⁻³. The minimum value of each curve corresponds to *D*_{min}.



FIG. 14. (Color online) The maximum value of the difference signal, D_{max} , plotted *vs.* P_{Rb} measured by longitudinal Faraday rotation. The curves show calculations of D_{max} . Densities indicated in the legend are in units of 10^{12} cm⁻³.