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Tune-out wavelengths of alkali-metal atoms and their applications

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Using first-principles calculations, we identify "tune-out" optical wavelengths, $\lambda_{\rm zero}$, for which the ground-state frequency-dependent polarizabilities of alkali-metal atoms vanish. Our approach uses high-precision, relativistic all-order methods in which all single, double, and partial triple excitations of the Dirac-Fock wave functions are included to all orders of perturbation theory. We discuss the use of tune-out wavelengths for sympathetic cooling in two-species mixtures of alkalis with group-II and other elements of interest. Special cases in which these wavelengths coincide with strong resonance transitions in a target system are identified.

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I. INTRODUCTION

The realization of mixtures of trapped ultracold atomic gases [1–5] has opened new paths towards the formation of ultracold diatomic molecules [6–10], quantum-state control of chemical reactions [11], prospects for quantum computing with polar molecules [12–14], tests of fundamental symmetries [15–17] and studies of fundamental aspects of correlated many-body systems [18], and dilute quantum degenerate systems [19–23]. Cotrapped diamagnetic-paramagnetic mixtures have also made possible experimental realization of interspecies Feshbach resonances [24–26], two-species Bose-Einstein condensates and mixed Bose-Fermi and Fermi-Fermi degenerate gases [18, 27–29].

In an optical lattice, atoms can be trapped in the intensity maxima or minima of the light field by the optical dipole force [30]. This force arises from the dispersive interaction of the induced atomic dipole moment with the intensity gradient of the light field, and is proportional to the ac polarizability of the atom. When its ac polarizability vanishes, as can happen at certain wavelengths, an atom experiences no dipole force and thus is unaffected by the presence of an optical lattice. Our present work provides accurate predictions of the $\lambda_{\rm zero}$ which lead to zero Stark shifts for alkali-metal atoms. These wavelengths have been introduced as "tune-out wavelengths" by LeBlanc and Thywissen [31].

We suggest some possible uses for such wavelengths, all of which take advantage of the fact (demonstrated below), that tune-out wavelengths are highly dependent upon atomic species and state. For a given atomic species and state A, let L_A designate an optical lattice or trap made with light at one of the tune-out wavelengths of A. We start with a model configuration consisting of the gas A embedded in L_A and confined by another trap, T.

Some process is performed on the gas, after which T is turned off. Members of A will depart and L_A may confine whatever is left. For example, one might photoassociate some A atoms into dimers during the initial period, and thereby be left with a nearly pure population of dimers trapped in L_A at the end. LeBlanc and Thywissen [31] have pointed out the advantage of tune-out wavelengths for traps containing two species. If another species, B, is added to the model configuration, it will ordinarily be affected by L_A, so B can be moved by shifting L_A, while A remains unaffected. Schemes of this type have been used for entropy transfer and controlled collisions between ⁸⁷Rb and ⁴¹K [32–34]. For bichromatic optical lattice schemes, such as those discussed by Brickman Soderberg, et al. [35, 36], it could be useful to incorporate L_B into the model configuration, so as to be able to move A and B completely independently. In another application, a Sr lattice at a ³P₀ tune-out wavelength was suggested for realization of quantum information processing [37].

In the next section, we briefly discuss the calculation of frequency-dependent polarizabilities of alkali-metal atoms. In section III, we present the tune-out wavelengths for the alkalis from Li to Cs and discuss some of their applications.

II. FREQUENCY-DEPENDENT POLARIZABILITIES

The background to our approach to calculation of atomic polarizabilities is treated in a recent review article [38]. Here we summarize points salient to the present work. The frequency-dependent scalar polarizability, $\alpha_0(\omega)$, of an alkali-metal atom in its ground state v may be separated into a contribution from the core elec-

trons, $\alpha_{\rm core}$, a core modification due to the valence electron, α_{vc} , and a contribution from the valence electron, $\alpha_0^v(\omega)$. Since core electrons have excitation energies in the far-ultraviolet region of the spectrum, the core polarizability depends weakly on ω for the optical frequencies treated here. Therefore, we approximate the core polarizability by its dc value as calculated in the random-phase approximation (RPA) [39], an approach that has been quite successful in previous applications. The core polarizability is corrected for Pauli blocking of core-valence excitations by introducing an extra term α_{vc} . For consistency, this is also calculated in RPA. Therefore, the ground state polarizability may be separated as

$$\alpha_0(\omega) = \alpha_{\text{core}} + \alpha_{vc} + \alpha_0^v(\omega). \tag{1}$$

The valence contribution to the static ac polarizability is calculated using the sum-over-states approach [40]:

$$\alpha_0^v(\omega) = \frac{2}{3(2j_v + 1)} \sum_k \frac{\langle k \| D \| v \rangle^2 (E_k - E_v)}{(E_k - E_v)^2 - \omega^2}, \quad (2)$$

where $\langle k \parallel D \parallel v \rangle$ is the reduced electric-dipole (E1) matrix element. In this equation, ω is assumed to be at least several linewidths off resonance with the corresponding transitions. We use shorter designation, α_0 , for frequency-dependent scalar polarizability below. Unless stated otherwise, we use the conventional system of atomic units, a.u., in which $e, m_e, 4\pi\epsilon_0$ and the reduced Planck constant \hbar have the numerical value 1. Polarizability in a.u. has the dimension of volume, and its numerical values presented here are expressed in units of a_0^3 , where $a_0 \approx 0.052918$ nm is the Bohr radius. The atomic units for α can be converted to SI units via $\alpha/h \, [\mathrm{Hz/(V/m)^2}] = 2.48832 \times 10^{-8} \alpha \, [\mathrm{a.u.}]$, where the conversion coefficient is $4\pi\epsilon_0 a_0^3/h$ and the Planck constant h is factored out.

The calculation of the ground state frequencydependent polarizabilities in alkali-metal atoms has been previously discussed in [41, 42], and we give only brief summary of the approach. The sum over intermediate k states in Eq. (2) converges rapidly. Therefore, we separate the valence state polarizability into two parts, $\alpha_{\rm main}$, containing the contributions from the few lowest np states, and the remainder, α_{tail} . We note that our calculations are carried out with the finite basis set constructed using B-splines [43] making the sum finite. In the calculation of α_{\min} , we use the experimental values compiled in Ref. [44] along with their uncertainties for the first ns - np matrix elements, for example the $4s - 4p_i$ matrix elements in K. For all other terms, we use the relativistic all-order values [44, 45] of the matrix elements and the experimental values of the energies [46– 48]. In the relativistic all-order method, all single-double (SD) or single-double and partial valence triple (SDpT) excitations of the Dirac-Fock (DF) wave function are included to all orders of perturbation theory [40, 44, 49]. We conduct additional semi-empirical scaling of our allorder values (SD_{sc}) where we expect scaled values to be

TABLE I: 5s - np contributions to the frequency-dependent polarizability of the ground state of Rb at $\lambda_{\rm Zero} = 423.0448$ nm = $1/(23638.16~{\rm cm}^{-1})$. Absolute values of electric-dipole matrix elements are expressed in a.u. (ea_0) , and the corresponding energy differences are expressed in conventional wavenumber units (cm⁻¹).

Contribution	$ \langle 5s D np_{1/2} \rangle $	$E_{np_j} - E_{5s}$	α_0
$5p_{1/2}$	4.231	12579.0	-41.130
$6p_{1/2}$	0.325	23715.1	50.235
$7p_{1/2}$	0.115	27835.0	0.124
$8p_{1/2}$	0.059	29835.0	0.023
$np_{1/2}$ tail			0.085
$5p_{3/2}$	5.978	12816.5	-84.938
$6p_{3/2}$	0.528	23792.6	66.140
$7p_{3/2}$	0.202	27870.1	0.383
$8p_{3/2}$	0.111	29853.8	0.081
$np_{3/2}$ tail			0.285
$\alpha_{\rm core}$			9.076
α_{vc}			-0.367
$lpha_0^v$			-8.712
Total $\alpha_0(\omega)$			0.00

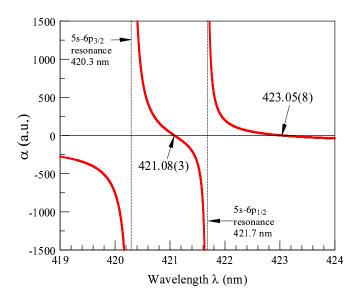


FIG. 1: The frequency-dependent polarizability of the Rb ground state. The first two tune-out wavelengths are marked with arrows.

more accurate or for more accurate evaluation of the uncertainties. Our scaling procedure and evaluation of the uncertainties of the all-order results have been recently discussed in Ref. [50]. Briefly, the uncertainties of the all-order matrix elements are given by the spread of their SD, SDpT, SD_{sc} and SDpT_{sc} values. These are also used to calculate the uncertainties in the state-by-state contributions to the frequency-dependent polarizability. The tail contributions, $\alpha_{\rm tail}$, are calculated in the DF approximation using complete basis set functions that are linear combinations of B-splines [51]. In the cases treated here, the tail contribution is of the order of 1% of the net va-

TABLE II: Tune-out wavelengths $\lambda_{\rm zero}$ for alkali-metal atoms from Li to Cs. The resonant wavelengths $\lambda_{\rm res}$ for relevant transitions are also listed. The wavelengths (in vacuum) are given in nm.

Atom	Resonance	$\lambda_{ m res}$	$\lambda_{ m zero}$
ьГі	$2s - 2p_{1/2}$	670.992478	650 005 AF(1)
	$2s - 2p_{3/2}$	670.977380	670.987445(1)
⁷ Li	$2s - 2p_{1/2}$	670.976658	
	$2s - 2p_{3/2}$	670.961561	670.971626(1)
Li	,		324.18(6)
	$2s - 3p_{1/2}$	323.3576	
	$2s - 3p_{3/2}$	323.3566	274 011(7)
	$2s - 4p_{1/2}$	274.2001	274.911(7)
Na	$3s - 3p_{1/2}$	589.7558	
			589.5565(3)
	$3s - 3p_{3/2}$	589.1583	221 007(2)
	$3s - 4p_{1/2}$	330.3929	331.905(3)
	$3s - 4p_{1/2}$	550.5929	330.3723
	$3s - 4p_{3/2}$	330.3319	333.37.23
			285.5817(8)
	$3s - 5p_{1/2}$	285.3850	
K	$4s - 4p_{1/2}$	770.1083	
	4 4	766 7000	768.971(3)
	$4s - 4p_{3/2}$	766.7009	405.98(4)
	$4s - 5p_{1/2}$	404.8356	400.30(4)
	¥ -/ -		404.72(4)
	$4s - 5p_{3/2}$	404.5285	
			344.933(1)
	$4s - 6p_{1/2}$	344.8363	
Rb	$5s - 5p_{1/2}$	794.9789	700 024(7)
	$5s - 5p_{3/2}$	780.2415	790.034(7)
	$3s - 3p_{3/2}$	100.2410	423.05(8)
	$5s - 6p_{1/2}$	421.6726	(-)
	,		421.08(3)
	$5s - 6p_{3/2}$	420.2989	950 49(9)
	5.0 7m	359.2593	359.42(3)
	$5s - 7p_{1/2}$		
Cs	$6s - 6p_{1/2}$	894.5929	880.25(4)
	$6s - 6p_{3/2}$	852.3472	000.29(4)
		•	460.22(2)
	$6s - 7p_{1/2}$	459.4459	
		APP 0222	457.31(3)
	$6s - 7p_{3/2}$	455.6557	380 020(4)
	$6s - 8p_{1/2}$	388.9714	389.029(4)
	56 OP1/2	300.0111	

lence contribution α_0^v .

We define the tune-out wavelength $\lambda_{\rm zero}$ as the wavelength where the ac polarizability of the ground state vanishes. In practice, we calculated $\alpha_0(\omega)$ for a range of values in the vicinity of relevant resonances and identified values of ω where the polarizability turned to zero

with sufficient numerical accuracy.

We illustrate the cancellation of all contributions to 5sRb polarizability at λ_{zero} =423.0448 nm in Table I. Since this wavelength is between $5s - 5p_{3/2}$ and $5s - 6p_{1/2}$ resonances, the contributions of the $5p_j$ and $6p_j$ terms strongly dominate. However, the contribution from the core is significant (11% of the largest valence term). This table shows that $\lambda_{\rm zero}$ is located where the valence contribution to the polarizability cancels the adjusted core contribution, a feature that is common to all the cases treated here. The zero crossing point is in the close vicinity of the $5s - 6p_{1/2}$ resonance owing to the relative size of the $5s - 5p_j$ and $5s - 6p_j$ reduced electric-dipole matrix elements given in the second column of Table I. The 5s-6p matrix elements are more than an order of magnitude smaller than the 5s - 5p matrix elements. Since polarizability contributions are proportional to the square of the matrix element, the denominators of the $6p_i$ terms have to become very small to cancel out the 5p contributions.

This tune-out wavelength is illustrated in Fig. 1 where we plot ground-state polarizability of Rb atom in a.u. in the vicinity of the $5s-6p_j$ resonances. Another zero crossing point shown in the figure is located between $5s-6p_{1/2}$ and $5s-6p_{3/2}$ resonances, as expected. The next tune-out wavelength will be located close to the $5s-7p_{1/2}$ resonance since the values of the matrix elements continue to decrease with n.

III. RESULTS AND APPLICATIONS

In Table II, we list the vacuum $\lambda_{\rm zero}$ wavelengths for alkali-metal atoms from Li to Cs. For convenience of presentation, we also list the resonant wavelength $\lambda_{\rm res}$ in vacuum in the relevant range of wavelengths. We order the lists of the resonant wavelengths and $\lambda_{\rm zero}$ to indicate the respective placements of $\lambda_{\rm zero}$ and their distances from resonances. The resonant vacuum wavelength values are obtained from energy levels from National Institute of Standards and Technology (NIST) database [46] with the exception of the $2s-2p_{1/2}$ and $2s-2p_{3/2}$ transition wavelengths for ⁶Li and ⁷Li that are taken from recent measurements [52].

Since alkali ground states have electric dipole transitions only to p states, their polarizabilities will cross zero only between two ns-n'p resonances. We set the wavelength of the $ns-(n+2)p_{1/2}$ resonance as a lower wavelength bound for our search. The fine structure of the (n+2)p level is sufficiently small for all alkalis to make the zero point between $ns-(n+2)p_{1/2}$ and $ns-(n+2)p_{3/2}$ relatively difficult to use in practice, so we do not list it. We omit the $\lambda_{\rm zero}$ between $2s-3p_j$ resonances for the same reason. The wavelengths of the next zero-crossing near the $ns-(n+3)p_{1/2}$ resonances are in the ultraviolet, and not as readily accessible in most laboratories, so we have not calculated them. However, this would be

TABLE III: Wavelength (in vacuum) of selected transitions in	Mg, Ca, Zn, Cd, Sr, Ba, Hg, Yb, Dy, Ho, and Er in nm.
Comparison of these values with tune-out wavelengths listed in	Γable II yields many instances of resonant transitions that are
very close to $\lambda_{\rm zero}$ in alkali.	

Atom	Transition	Wavelength	Transition	Wavelength
Mg	$3s^2 {}^1S_0 - 3s3p {}^1P_1$	285.3	$3s^2 {}^1S_0 - 3s3p {}^3P_1$	457.2
Ca	$4s^2 {}^1S_0 - 4s4p {}^1P_1$	422.8	$4s^2 {}^1S_0 - 4s4p {}^3P_1$	657.5
Sr	$5s^2 {}^1S_0 - 5s5p {}^1P_1$	460.9	$5s^2 {}^1S_0 - 5s5p {}^3P_1$	689.5
$_{\mathrm{Ba}}$	$6s^2 {}^1S_0 - 6s6p {}^1P_1$	553.7	$6s^2 {}^1S_0 - 6s6p {}^3P_1$	791.4
Zn	$4s^2 {}^1S_0 - 4s4p {}^1P_1$	213.9	$4s^2 {}^1S_0 - 4s4p {}^3P_1$	307.7
Cd	$5s^2 {}^1S_0 - 5s5p {}^1P_1$	228.9	$5s^2 {}^1S_0 - 5s5p {}^3P_1$	326.2
$_{ m Hg}$	$6s^2 {}^1S_0 - 6s6p {}^1P_1$	184.9	$6s^2 {}^1S_0 - 6s6p {}^3P_1$	253.7
Yb	$6s^2 {}^1S_0 - 6s6p {}^1P_1$	398.9	$6s^2 {}^1S_0 - 6s6p {}^3P_1$	555.8
Dy	$4f^{10}6s^2 {}^5I_8 - 4f^{10}({}^5I_8) 6s6p ({}^1P_1) J = 9$	421.3		
Er	$4f^{12}6s^2 {}^3H_6 - 4f^{11}({}^3H_6) 6s6p ({}^3P_1) J = 7$	582.8		
Но	$4f^{11}6s^2 {}^4I_{15/2} - 4f^{11}({}^4I_{15/2}) 6s6p ({}^3P_1) J = 17/2$	598.5		
Но	$4f^{11}6s^{2} {}^{4}I_{15/2} - 4f^{11}({}^{4}I_{15/2}) 6s6p ({}^{1}P_{1}) J = 13/2$	416.4		

a routine matter for future work. There are no $\lambda_{\rm zero}$ at wavelengths greater than those of the primary $ns-np_{1/2}$ resonances. Within these constraints, we have found four $\lambda_{\rm zero}$ for Na, K, Rb, and Cs and three $\lambda_{\rm zero}$ for Li, as shown in Table I.

The stated uncertainties in the $\lambda_{\rm zero}$ values are taken to be the maximum difference between the central value and the crossing of the $\alpha_0 \pm \delta \alpha_0$ with zero, where $\delta \alpha_0$ is the uncertainty in the ground state polarizability value at that wavelength. The uncertainties in the values of polarizabilities are obtained by adding uncertainties in the individual polarizability contributions in quadrature.

We find small but significant differences in the first tune-out wavelengths of ⁶Li and ⁷Li due to the isotope shift. These values refer to the centers of gravity of all hyperfine states and do not take into account the hyperfine structure. Therefore, this λ_{zero} and the corresponding $2s - 2p_i$ resonance wavelengths are listed separately. We verified that isotope shift of the 2s-2p traditions in Li does not affect the next tune-out wavelength, 324.18(6)nm, so we use NIST data for the other transitions. We also investigated possible dependence of the first tune-out wavelengths on the isotope shift for ³⁹K, $^{40}\mathrm{K},~^{41}\mathrm{K}$ and $^{85}\mathrm{Rb},~^{87}\mathrm{Rb}.$ The D1 $(4s-4p_{1/2})$ and D2 $(4s-4p_{3/2})$ line wavelengths for ³⁹K, ⁴⁰K, and ⁴¹K have been measured using a femtosecond laser frequency comb by Falke et al. [53]. We carry out three calculations of the first tune-out wavelength using D1, D2 wavelengths for the specific isotope in our calculations. The resulting value for 39 K and 40 K, 768.971(3)nm, is the same as the value quoted in Table II. The ⁴¹K value is 768.970(3)nm, with the difference being well below our quoted uncertainty. The calculations of the first tune-out wavelength in Rb using D1 and D2 frequencies for ⁸⁵Rb and ⁸⁷Rb listed in [54, 55] gave results identical to result from Table II, 790.034(7)nm that was obtained using NIST data. We note that our values for the first tune-out wavelengths are in good agreement with LeBlanc and Thywissen [31] calculations with the exception of their value for ⁴⁰K.

The first tune-out wavelength in Rb has been measured to be 789.85(1)nm in [32]. Some discrepancy with our result is most likely due to approximate linear polarization of the beam in [32]. The difference is compatible with a shift in the tune-out wavelength caused by few percent spurious σ^- polarization component [56].

Below, we identify two main applications of tuneout wavelengths. First, these wavelengths are advantageous for cooling of group-II and other more complicated atoms, by sympathetic cooling using an accompanying alkali atom.

Recently, group II atoms have been the subject of various experiments and proposals in atomic clock research and quantum information. BEC of ⁸⁴Sr has been reported recently by two groups [57, 58]. The element Yb has four boson and two fermion isotopes, all of which have been cooled into the microkelvin range. Several exciting new prospects for quantum information processing with the ground state nuclear spin have recently been identified in group II elements [37]. Also, Sr or Yb are useful for polarized mixtures of fermions, or Bose-Fermi mixtures, where isotopic mixtures can be studied.

More complex systems have become of interest in the development of frequency standards and quantum information processing schemes. For example, the rare earth holmium is a candidate for quantum information applications [59] due to its rich ground-state hyperfine structure. Erbium has been a subject of recent experimental work [60, 61], stimulated by its possible use in a variety of applications, including narrow linewidth laser cooling and spectroscopy, unique collision studies, and degenerate bosonic and fermionic gases with long-range magnetic dipole coupling.

Some species, particularly fermions, are difficult to cool by themselves due to unfavorable ultracold collisional dynamics. In such cases, it may be possible to use sympathetic cooling in a mixture of the target species and one of the alkalis, where the alkali-metal atom is cooled directly by standard techniques. This has recently been demonstrated in Yb:Rb mixtures [62]. Use of $\lambda_{\rm zero}$ trap wavelengths could allow one to release alkali atoms after the target atoms of the other species are sufficiently cold, in a hybrid trap configuration that combines optical and magnetic traps or bichromatic optical traps. If the final trap configuration utilizes a $\lambda_{\rm zero}$ wavelength, strong trapping of the target atom is possible while alkali atoms will be released by turning off its separate trapping potential. Since placement of the resonances varies significantly among the alkali-metal atoms, a wide range of $\lambda_{\rm zero}$ is available as shown in Table III.

We list the resonant wavelengths for variety of atomic systems in Table III. For consistency with the other tables, we list vacuum wavelengths obtained from the NIST energy levels database [48]. Both strong and intercombination lines that can be used for trapping of these species are listed. Comparing Tables II and III yields many instances of resonant transitions that are very close to $\lambda_{\rm zero}$. Here are few of the very close cases: Mg 285.3 - Na 285.6, Sr 460.9 - Cs 460.2, Dy 421.3 - Rb 421.1, Ho 598.5 - Na 589.6.

Tune-out wavelength laser light may be also useful in three-species cooling schemes such as reported in Ref. [63] by allowing easy release of one of the species from the trap. The work [63] demonstrated that the efficiency of sympathetic cooling of the ⁶Li gas by ⁸⁷Rb was increased by the presence of ⁴⁰K through catalytic cooling.

Measurements of the tune-out wavelengths may be used as high-precision benchmark tests of theory and determination of the excited-state matrix elements that are difficult to measure by other methods. Matrix elements of ns - n'p transitions of alkali-metal atoms, where ns

is the ground state, are difficult to calculate accurately owing to large correlation corrections and small values of the final numbers. Experimental measurements of the $\lambda_{\rm zero}$ predicted in this work will serve an an excellent benchmark test of the all-order calculations. Moreover, it will be possible to combine these measurements with theoretical calculations to infer the values of these small matrix elements. Only one high-precision measurement of such matrix elements $(6s-7p_j$ transitions in Cs) has been carried out to date [64].

IV. CONCLUSION

In summary, we calculate tune-out wavelengths in alkali-metal atoms from Li to Cs and estimate their uncertainties. Applications of these tune-out wavelengths to sympathetic cooling of group-II and other more complicated atoms with alkalis are discussed. Special cases where these wavelengths coincide with strong resonance transition in group-II atoms, Yb, Dy, Ho, and Er are identified. Measurements of the tune-out wavelengths for benchmark tests of theory and experiment are proposed.

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