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Route to Direct Multiphoton Multiple Ionization

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Abstract

We address the concept of direct multiphoton multiple ionization in atoms exposed to intense, short wavelength radiation and explore the conditions under which such processes dominate over the sequential. Their contribution is shown to be quite robust, even under intensity fluctuations and interaction volume integration, and reasonable agreement with experimental data is also found.

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The quest for direct multiple excitation/ionization of several electrons bound in atoms or molecules under the influence of intense laser radiation dates back to the early 80's [1–5]. Until the recent appearance of the FEL-based intense XUV and X-ray sources [6], however, the hitherto available infrared and optical sources, although quite intense, proved inadequate for the task. Multiple ionization has of course been observed in a number of experiments [1–5], but the mechanism has been the sequential stripping of electrons, beginning with the valence shell and proceeding inwards.

The only notable exception to the sequential stripping, under long wavelength radiation ($\sim 800\text{nm}$), came about with the advent of ultrashort (subpicosecond) TiSa sources, which led to the observation of non-sequential double ionization [7]. Still, the basic mechanism relies on a valence electron pulled out by the field, set into oscillatory motion thereby causing the ejection of a second, or perhaps third, electron by collision, as it returns towards the core; hence the term recollision [7]. For this to be possible, the ponderomotive energy (cycle-averaged kinetic energy) of a quasifree electron under the field must be larger than the binding energy of a second electron.

The situation has now changed dramatically with the appearance of XUV to X-ray intense sources which has made feasible for the first time the observation of a number of non-linear processes in that wavelength range [8–11]. The decisive developments in that respect are the large peak intensity and sub-picosecond pulse duration. The latter is of central importance to our considerations in this work. An early, small scale so to speak, development in that direction has been the direct 2-photon double ionization of Helium which has grown into a subfield with tens of theoretical [12] and a few experimental studies [13], limited mainly by the present early stage of the sources. The chief difference between this process and its counterpart under long wavelength is that no recollision is involved, as the ponderomotive energy is totally negligible. The two electrons are pulled out by the field while, electron-electron interaction although present, is not necessary; in contrast to single-photon double ionization. The information on this process, collected so far, can serve as a calibration for the larger scale generalization proposed in this paper.

Although the idea, under suitable conditions, is applicable to essentially any atom, in the interest of providing a quantitative assessment of the underlying physics, we focus on the specific context of Neon under radiation of photon energy 93 eV ($\approx 13.3\text{ nm}$). In fact, some experimental data have already appeared in the literature [14]. For this photon energy, even

at a peak intensity $10^{18}\text{W}/\text{cm}^2$, the ponderomotive energy U_p is about 10 eV, which is much smaller than both the photon energy and the binding energy of any electron in Neon, thus guaranteeing the validity of LOPT (Lowest non-vanishing Order of Perturbation Theory) [3, 4, 15]. In addition, for the notion of the cross section (generalized cross section of the appropriate order) to be valid, the pulse duration must be at least 10 cycles of the field. For photon frequencies of the order of 90-100 eV, even a pulse duration of 1fs amply satisfies this condition. If the data are limited only to populations of the ionic species produced in the process, a set of kinetic (rate) equations are sufficient for the interpretation, as well as for our purpose in this paper. This is a set of differential equations governing the evolution of the populations of the various ionic species during the pulse [4, 15]. The complete set of such equations involving sequential, as well as direct processes from the neutral, leading to the ejection of up to 8 electrons are of the form [16]

$$\frac{dN_0}{dt} = - \sum_{j=1}^8 \sigma_{0,j}^{(n_0,j)} F^{n_0,j} N_0 \quad (1a)$$

$$\begin{aligned} \frac{dN_j}{dt} = & \sigma_{0,j}^{(n_0,j)} F^{n_0,j} N_0 + \sigma_{j-1,j}^{(n_{j-1,j})} F^{n_{j-1,j}} N_{j-1} \Theta[j-2] \\ & - \sigma_{j,j+1}^{(n_{j,j+1})} F^{n_{j,j+1}} N_j \Theta[7-j] \end{aligned} \quad (1b)$$

with $1 \leq j \leq 8$ and $\Theta[j]$ the discrete Heaviside function.

The terms in the right hand side represent various processes contributing to the rate of change of the species whose time derivative appears on the left hand side. Thus N_j indicates the j th ionic species of charge $(+j)$, while a term like $\sigma_{j,k}^{(n)} F^n N_j$ represents an n -photon process leading from species j to species k , with the corresponding n -photon (generalized) cross section $\sigma_{j,k}^{(n)}$, where $F(t)$ is the time-dependent photon flux in photons/cm²sec. These equations are to be solved under a pulse, as realistic as possible, dictated by the conditions of operation of the source; in this case the FEL.

The simplest scenario consists of retaining only sequential processes in the equations, which means that only the sequence of channels leading from ion j to $j+1$, by successive single electron ejections, is retained in the equations. At relatively low peak intensity and long pulse duration, these will be the dominant channels. As a point of calibration for things to follow, we present in Fig. 1 the ion yields as a function of peak intensity, at the end of deterministic pulses of duration 30 fs [Fig. 1(a)] and 5 fs [Fig. 1(b)]. In both figures, the dashed lines represent the yields for the sequential channels alone. These figures depict the

typical single atom behavior, illustrating the appearance and disappearance of ionic species as they give rise to higher ones with rising intensity.

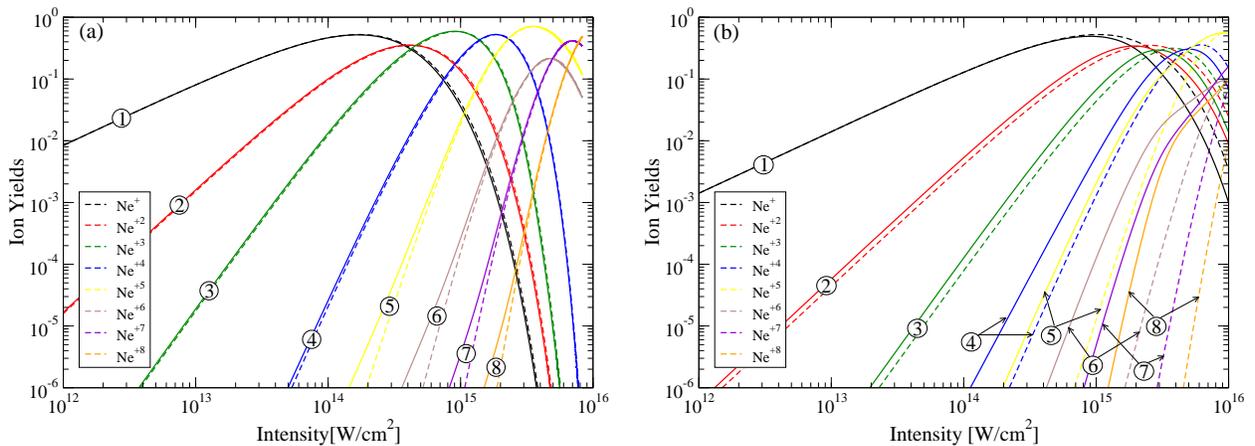


FIG. 1: (Color online) Ionization of Ne at 93 eV under a deterministic pulse with duration (a) 30 fs and (b) 5 fs. Solution of Eqs. (1) in the presence of sequential channels alone (dashed lines) and with both direct and sequential processes included (solid lines).

For Ne under 93 eV photons, however, an entirely new class of channels are energetically possible. These are direct, several electron multiphoton (of the appropriate order) processes, leading from the neutral to the corresponding ion. Specifically, 2 photons can eject 2 electrons leading to Ne^{+2} , 3 photons can eject 3 electrons leading to Ne^{+3} , etc., up to 6 photons leading directly to Ne^{+6} . These are higher order generalizations of 2-photon 2-electron ejection in He [12]. Moreover, we have included an 8-photon 7-electron transition $\text{Ne} \rightarrow \text{Ne}^{+7}$, and an 11-photon 8-electron transition $\text{Ne} \rightarrow \text{Ne}^{+8}$. Direct n -photon m -electron ejection can in principle always occur, for $n \geq m$, as long as it is energetically allowed. It can in fact occur, from any ionic species, during the interaction, but it is mostly from the neutral, where all of the population resides at $t = 0$, that such processes are expected to play an important role. In our equations above, those processes are represented by the terms in the right hand side which contain the population N_0 of the neutral, involving also multiphoton cross sections of the appropriate order.

The values for direct n -photon m -electron ejection cross sections represent new territory. There is, however, a basis for conjecturing reasonable values. We argue that the cross section for n -photon, m -electron ejection (with $m < n$) in a given atom, is of the same order of magnitude as an n -photon one-electron ejection, for the same photon energy [16].

The reasoning here rests on the following properties of a generalized cross section: (a) The n -photon transition matrix element from the ground state connecting to n electrons in the continuum requires no correlation. (b) As a consequence, the summation over intermediate states is dominated, in both cases, by single electron matrix elements. (c) All intermediate states are in the continuum, with no intermediate resonances of any significance. E.g., for 2-photon, 2-electron ejection from an initial state $1s^2$, one would have

$$\sum_{\mathbf{k}} \frac{\langle \mathbf{k}'p, \mathbf{k}p | \hat{\mathbf{r}}_1 + \hat{\mathbf{r}}_2 | \mathbf{k}p; 1s \rangle \langle \mathbf{k}p; 1s | \hat{\mathbf{r}}_1 + \hat{\mathbf{r}}_2 | 1s^2 \rangle}{E_{\mathbf{k}p} - E_{1s^2} - \hbar\omega}, \quad (2)$$

with $\hat{\mathbf{r}}_i$ the electronic coordinates, and the summation extending over all allowed 1-electron excited states. This is non-zero even for non-interacting electrons, reducing to the product $\langle \mathbf{k}'p | \hat{\mathbf{r}}_2 | 1s \rangle \langle \mathbf{k}p | \hat{\mathbf{r}}_1 | 1s \rangle$ of 1-electron matrix elements. One example of applicability of this conjecture is found in the cross section of two-photon double ionization of Helium which turns out to be roughly equal to the two-photon one electron ejection [17]; while in contrast the cross section for one-photon two-electron ejection is smaller than the one-photon one-electron ejection by a factor of about 50. The reason of course has to do with the fact that ejecting m electrons by n -photon absorption, for $n < m$, is impossible without correlation. A second example is 4-photon double ionization of Carbon [4]. Adopting the above conjecture, we obtain single-photon and two-photon cross sections through a calculation and higher order cross sections through a procedure of scaling [4, 15].

The result of a calculation including these direct higher non-linearity channels is shown by solid lines in Fig. 1. Their presence does not alter significantly the ion yields for the 30 fs pulse, but for the 5 fs pulse it does increase rather dramatically the yields of the higher charge species, beginning with Ne^{+4} . There is a clear physical interpretation of these results. The effect of the direct channels is more pronounced for the shorter pulse, because the sequential channels do not have as much a chance to drain the neutral — from which the direct channels originate — as they have in the rising wing of the longer pulse. And the direct channels, being of higher non-linearity, will dominate only if exposed to higher intensity, provided there is still enough population left in the neutral; which is the case for the shorter pulse. For the same reason, the yields of lower charge ions (up to Ne^{+4}) are not affected much because, in their case, even the direct channels are of low order.

A first conclusion at this point is that, if the temporal shape of the pulse were deterministic, shortening its duration would enhance the contribution of the direct channels. It

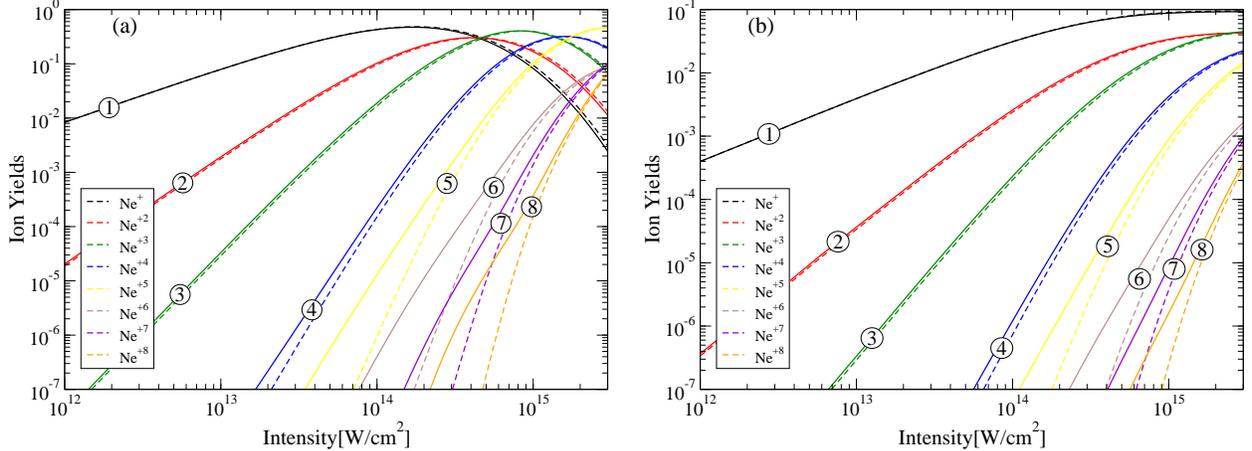


FIG. 2: (Color online) Ionization of Ne at 93 eV under chaotic pulses of duration 30 fs and coherence time 6 fs. (a) Ion yields obtained by solving Eqs. (1) for randomly chosen $F(t)$, in the presence of sequential (dashed) and sequential+direct (solid) channels. The presented yields are averaged over 10^4 realizations. (b) As in (a) with volume expansion effects included.

is, however, well known that, at least for the time being, the pulses of the FEL sources are not deterministic but exhibit strong intensity fluctuations. Qualitatively speaking, they can be considered chaotic [6]. Specifically, the overall pulse envelop is known to contain spikes of random height and duration, which can be as short as 5fs. This means that the atom is indeed exposed to spikes of duration sufficiently short to enhance the direct channels. The implications for the theory is that Eqs. (1) become stochastic, owing to the stochastic nature of the intensity. The simplest way to account for this, is to recall that n -photon ionization, within LOPT, is proportional to the n -th order intensity correlation function $G^{(n)}$ [18], which for a chaotic field is given by $n!\bar{F}^n$, where $\bar{F}(t)$ is the average intensity (flux). We could thus replace F^n by $n!\bar{F}^n$ in Eqs.(1), which amounts to effectively increasing the n -photon ionization cross section by a factor of $n!$. Obviously, this favors processes of higher order.

This procedure would be rigorous if we had a single n -photon process and in addition the field were truly chaotic. What we have, however, is a set of differential equations coupling processes of various orders. Multiplying the cross sections by $n!$ and using a deterministic pulse amounts to a decorrelation approximation, valid if the ionic populations do not change appreciably on the scale of the intensity fluctuations. An alternative but rigorous approach is to introduce an appropriate stochastic model for the radiation, and solve the differential

equations for a sufficiently large number of realizations of the radiation, taking in the end the average over such runs. This corresponds exactly to the manner experimental data are obtained. By comparing the results with those obtained through the above mentioned decorrelation, we can also assess the limits of validity of the latter. Space does not allow a detailed comparison of the two models, nor a detailed description of our stochastic modeling.

In the following we focus on results obtained within the ab initio stochastic modeling of the field, relying on theoretical as well as experimental information about the FEL pulses (e.g., see [6, 16, 19]). Comparing the averaged ion yields of Fig. 2(a), to those of Fig. 1(a), we note a dramatic increase of the higher charge species in the presence of chaotic light, when the direct channels are included. We have thus shown that intensity fluctuations will also enhance the direct channels over the sequential, even for the longer pulse of 30fs.

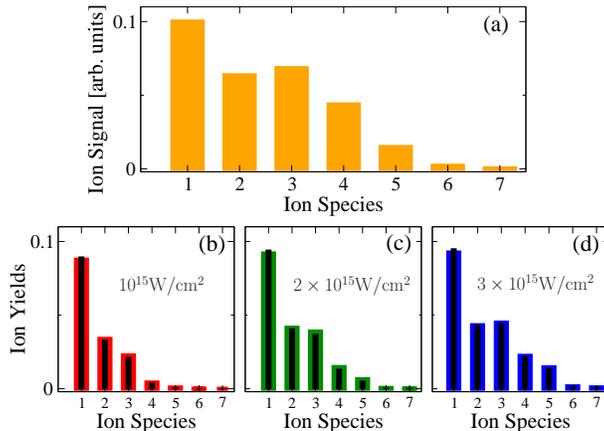


FIG. 3: (Color online) Ionization of Ne under chaotic pulses of duration 30 fs and coherence time 6 fs. (a) Data obtained by [14]. (b-d) Ion yields at three different intensities, as obtained by Fig. 2(b). The thin (black) bars correspond to sequential ionization whereas the broad (colored) bars refer to the case of open direct and sequential ionization channels.

To compare with experimental data on Neon [14], we have performed an integration over the spatial distribution of the radiation in an interaction volume approximating the experimental arrangement. The result of a calculation for a 30 fs pulse, corresponding to that of the experiment, including fluctuations, is shown in Fig. 2(b). As expected, the populations of the ionic species do not decrease beyond the saturation intensity, but exhibit a slow increase, due to the contribution of more atoms from the periphery of the interaction volume, where the intensity is lower than in the center. The crucial point, however, is that

the contribution of the direct channels is found to dominate, for the higher species, even upon spatial integration. It is therefore evident that the effect of the multielectron direct channels is quite robust, as it survives practically intact, beyond the deterministic pulse. Since only peaks of TOF (Time of Flight) results, at a single laser intensity, have been given in [14], we have estimated the relative magnitude of those peak heights and have plotted as a histogram the corresponding values in Fig. 3(a). The histograms of Figs. 3(b-d), correspond to the ion yields at three different intensities, at and around the nominal experimental one, as obtained from our Fig. 2(b). The comparison with the experimental data demonstrates an overall reasonable agreement, especially for intensities $\sim 3 \times 10^{15} \text{W/cm}^2$, but does also point to the sensitivity of the results to the value of the intensity. In the absence of experimental laser intensity dependences of the ionic species, we cannot offer at this time a more detailed evaluation of the agreement between theory and experiment.

We can nevertheless attempt to address the question of whether there are traces of the direct channels in the limited experimental data at our disposal. To this end, in Figs. 3(b-d) we present the relative heights due to the sequential channels alone (narrow black bars) as well as the ones when both direct and sequential channels are present (broad colored bars). Depending on the exact intensity, the effect of the direct channels, although rather small, is noticeable particularly for higher ions in Figs. 3(b,c). The reason for the small contribution of the direct channels is that the data have been obtained at or beyond the saturation intensity; not the optimal conditions for detecting the contribution of the direct, as clearly demonstrated in Figs. 1(a) and 2. Data over a range of intensities, below saturation, would provide a much clearer picture. Finally, somewhat surprising at first glance, for all three intensities the yield for the first ion (Ne^+) in the case of sequential ionization only, seems to be larger than the corresponding yield in the case of sequential+direct ionization. This, however, is consistent with the underlying physics, since the absence of direct channels leads to a much slower depletion of the neutral, from which direct channels originate, in favor of Ne^+ . For all other ions, the situation is reversed for all three intensities.

In summary, we have introduced the idea of direct multiple ionization, have explored its contribution in a specific realistic context, having incorporated all relevant aspects, such as intensity fluctuations and spatial radiation distribution. Reasonable agreement with existing but limited experimental data has been found, highlighting at the same time the need for more detailed data. The results in this work provide a benchmark case and guide for the

planning of future experiments with the new FEL sources which are undergoing an explosive expansion.

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