

## Shedding light on pilot-wave phenomena

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Droplets walking on a vibrating fluid bath, discovered over a decade ago [1], represent a macroscopic realization of the pilot-wave mechanics proposed for microscopic quantum particles

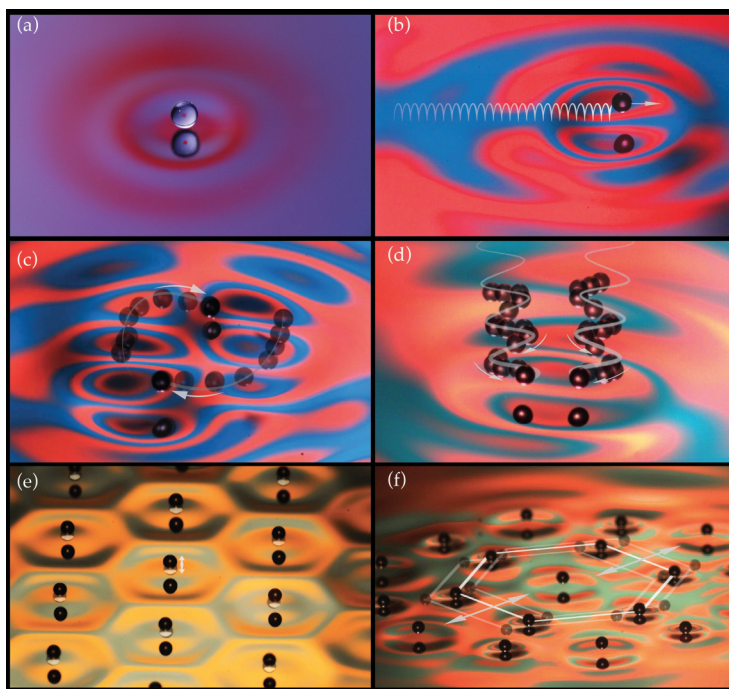


FIG. 1. (a) A droplet of an approximate diameter of 1 mm bounces on the surface of a vibrating oil bath. (b) For sufficiently large values of the vertical forcing, a droplet may spontaneously self-propel across the interface. Droplet pairs may interact through their wave fields, either (c) locking into orbits or (d) walking side by side in a promenade mode. (e) Multiple drops may organize into hexagonal lattices that (f) destabilize for sufficiently large values of the forcing acceleration. White streaks indicate the (b)–(e) complete or (c), (d), and (f) strobed droplet trajectories. DOI: <http://dx.doi.org/10.1103/APS.DFD.2015.GFM.V0064>

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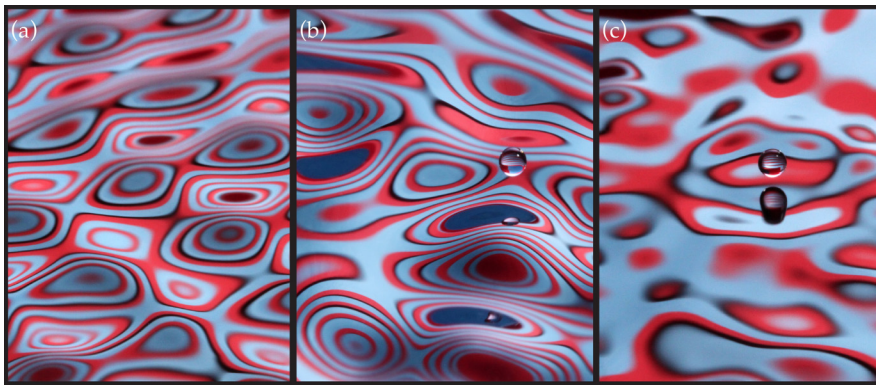


FIG. 2. (a) Faraday waves arise above a critical threshold in vibrational acceleration. (b) and (c) A droplet bouncing on the Faraday wave field moves in an unpredictable fashion and is at risk of coalescing. DOI: <http://dx.doi.org/10.1103/APS.DFD.2015.GFM.V0064>

by de Broglie [2]. This hydrodynamic pilot-wave system is of growing interest as it exhibits many of the peculiarities of quantum systems (see [3,4] for reviews).

We present here images of droplets bouncing on a vibrating bath. While the droplets are millimetric, the waves they generate have a characteristic amplitude of  $10\ \mu\text{m}$  and so are not easily discernible with the naked eye. We use the experimental setup reported in Ref. [5] that includes a bath of 20-cSt oil vibrated sinusoidally at 80 Hz. In order to illuminate the bath, a high-intensity light is placed behind striped colored patterns printed on paper and mounted on a light diffuser. The resulting images of the droplet and its pilot-wave field are captured with a high-speed camera.

Figure 1 has typical views of the bouncing droplets and accompanying wave fields when the bath vibration is below the Faraday threshold. Static bouncing and rectilinear walking states of single droplets are shown, as are bound states consisting of orbiting [6] or promenading [7] droplet pairs and stable and unstable crystal structures [8]. Above the Faraday threshold (Fig. 2), Faraday waves arise even in the absence of the droplet, so the droplet moves in an irregular fashion.

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## SHEDDING LIGHT ON PILOT-WAVE PHENOMENA

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