Universal aspects of the phase diagram of QCD with heavy quarks

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(Received 30 May 2018; revised manuscript received 10 September 2018; published 26 November 2018)

The flavor dependence of the QCD phase diagram presents universal properties in the heavy quark limit. For the wide class of models where the quarks are treated at the one-loop level, we show, for arbitrary chemical potential, that the flavor dependence of the critical quark masses—for which the confinement-deconfinement transition is second order—is insensitive to the details of the (confining) gluon dynamics and that the critical temperature is constant along the corresponding critical line. We illustrate this with explicit results in various such one-loop models studied in the literature: effective matrix models for the Polyakov loop, the Curci-Ferrari model, and a recently proposed Gribov-Zwanziger-type model. We further observe that the predictions which follow from this one-loop universality property are well satisfied by different calculations beyond one-loop order, including lattice simulations. For degenerate quarks, we propose a simple universal law for the flavor dependence of the critical mass, satisfied by all approaches.

DOI: [10.1103/PhysRevD.98.094020](https://doi.org/10.1103/PhysRevD.98.094020)

Understanding the properties of strongly interacting matter in extreme conditions of temperature, density, magnetic field, etc., is a question of topical interest with various implications, e.g., in early universe cosmology and astrophysics [1]. This relates to some of the most profound aspects of quantum chromodynamics (QCD), namely, the physics of (de)confinement and of chiral symmetry breaking/restoration. Past, present, and upcoming heavy-ion collision experiments at RHIC, CERN, FAIR, NICA and J-PARC, accompanied by an intense theoretical effort, aim at unravelling the phase diagram and the thermodynamic properties of QCD [2,3].

First-principle calculations based on numerical lattice simulations have demonstrated a crossover between a mostly confined to a mostly deconfined phase as the temperature T is increased [4]. Such calculations are, however, restricted to small baryon chemical potential μ_B due to the infamous sign problem that prevents the use of standard Monte Carlo algorithms [5]. A major open question of both theoretical and experimental research programs concerns the possible existence of a first order transition line in the (T, μ_B) plane, ending at a critical point [6,7]. Continuum approaches can avoid the strong sign problem of the lattice but necessarily

rely on approximations or model building that must be tested in situations where lattice results are under control.

In this context, it is of interest to study QCD-like theories, by varying parameters such as the number of colors and flavors (N_f), the quark masses, etc. Investigating the phase structure of the theory in such an extended parameter space, beyond its own theoretical interest, may contribute to our understanding of the phase diagram of the physical theory. An example is the investigation of the Columbia plot, which aims at describing the phase structure of the SU(3) color theory with two degenerate quark flavors u and d and one strange quark s , as a function of the quark masses $M_u = M_d$ and M_s [8–10].

The most commonly accepted scenario at zero chemical potential and in the limit of vanishing quark masses is that of a first order transition governed by the restoration of chiral symmetry at large temperatures [8]. This transition weakens as one increases the quark masses and it eventually becomes second order for critical values of the latter. The physical point lies beyond this critical line in the Columbia plot, where the transition is a crossover. A question is, therefore, to study how this critical line evolves with nonzero chemical potential [9].

Also of interest is the limit of infinite quark masses, corresponding to the pure Yang-Mills theory. For three colors, the latter presents a first order confinement-deconfinement phase transition in temperature [11]. Again, this transition weakens for large but finite quark masses and eventually becomes second order for critical values of the quark masses [12]. Contrarily to the light

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quark case, the heavy quark system can be simulated also at nonzero chemical potential because the sign problem can be evaded by using a large mass expansion [13]. In that case, the critical line is known to shrink toward larger quark masses as the chemical potential increases.

Not only does QCD with heavy quarks provide a framework where one can explicitly study the role of the chemical potential, but it also yields a stringent test case for approximate continuum approaches based either on first-principle calculations or on models of the QCD dynamics. Existing calculations include truncations of the Dyson-Schwinger equations (DSE) or functional renormalization group techniques [14], one- and two-loop perturbative calculations in the Curci-Ferrari (CF) model (a massive extension of the Faddeev-Popov Lagrangian in the Landau gauge) [15,16], and effective models for the Polyakov loop, the order parameter of the confinement-deconfinement transition [7,17,18].

In the present article, we discuss generic features of the phase diagram of QCD with heavy quarks. It has been observed, both in lattice simulations [12,13] and in matrix models [18,19], that the critical temperature is approximately independent of the quark content and that the flavor dependence of the critical quark masses (which defines the critical line/surface in the Columbia plot) is essentially independent of the details of the gluon dynamics. We recall how the latter comes about for the wide class of models where the quarks are treated at the one-loop level and we explicitly show, in that case, that both the critical temperature and the critical values of the order parameters are constant along the critical line. We further show that these observations extend to finite chemical potential.

We illustrate these features on various results from the literature, such as the CF model at one-loop [15] and the matrix model of Ref. [18]. We also provide results for a model of the glue dynamics recently proposed in Refs. [20,21], based on the Gribov-Zwanziger (GZ) quantization scheme [22]. We further show that our generic findings for the critical line extend beyond one-loop as exemplified by the results of the CF model at two-loop order [16] and by the DSE results of Ref. [14]. Regulator and renormalization effects complicate the comparison between the various continuum and lattice results. We fabricate an observable which suppresses these differences and which exhibits a simple N_f dependence that is satisfied by all existing continuum and lattice results in the large mass limit. This predicts the critical quark masses for increasing N_f —provided confinement is not lost—in all these approaches.

Let us first consider the case of a vanishing quark chemical potential $\mu = 0$ and N_f degenerate heavy quark flavors of mass M for simplicity. Descriptions of the QCD dynamics where quarks are included at the one-loop level yield the potential

$$\beta^4 V(\ell, \beta, M) = v_{\text{glue}}(\ell, \beta) - 2N_f f(\beta M) \ell, \quad (1)$$

with $f(x) = (3x^2/\pi^2)K_2(x)$, where $K_2(x)$ is the modified Bessel function of the second kind and β^{-1} is the temperature. The Polyakov loop ℓ is related to the free energy F_q of a static quark in the thermal bath of gluons as $\ell \propto \exp(-\beta F_q)$ and vanishes identically in the confined phase, where $F_q = \infty$. Here, we assume that the potential v_{glue} is confining, that is, it admits a minimum at $\ell = 0$ at zero temperature.

For each value of N_f , the critical values for ℓ , β and M on the upper boundary line of the Columbia plot are determined by solving the system of equations $\partial_\ell V = \partial_\beta^2 V = \partial_M^2 V = 0$, that is,

$$\partial_\ell v_{\text{glue}} = 2N_f f(\beta M), \quad (2)$$

$$\partial_\ell^2 v_{\text{glue}} = \partial_\ell^3 v_{\text{glue}} = 0. \quad (3)$$

The critical values for ℓ and β are determined from the two equations in (3), which only involve v_{glue} , and are, thus, completely blind to the quark content of the theory [More precisely, corrections to this statement are suppressed by $\exp(-\beta M)$]. This explains the fact that the critical temperature β_c^{-1} is essentially constant along the critical line in the Columbia plot [12,13,18]. The critical value $(\beta M)_c \equiv R_{N_f}$ can be determined from Eq. (2) for each value of N_f . Since the left-hand side does not depend on N_f , the flavor dependence of R_{N_f} is determined by the relation [18]

$$N_f f(R_{N_f}) = N'_f f(R_{N'_f}). \quad (4)$$

We deduce, in particular, that, even though the critical values ℓ_c , β_c and R_{N_f} depend on v_{glue} , Eq. (4) is model independent at one-loop order.

The above discussion easily generalizes to the case of nondegenerate quark masses, where one concludes that the equation determining the critical surface in the space of quark masses is universal, i.e., independent of v_{glue} . For instance, the critical line in the plane $(M_u = M_d, M_s)$ of the Columbia plot for $2 + 1$ (heavy) flavors is determined by

$$2f(\beta M_u) + f(\beta M_s) = 3f(R_3), \quad (5)$$

where only the number on the right-hand side, which determines the *location* of the critical line, depends on v_{glue} , through Eq. (2). We can use, alternatively, $3f(R_3) = 2f(R_2) = f(R_1)$. This trivially generalizes to more flavors.

The same strategy applies to the case of nonzero quark chemical potential $\mu = \mu_B/3$. The effective potential now depends separately on the Polyakov loops ℓ and $\bar{\ell}$ corresponding to quarks and antiquarks, respectively, and reads

$$\beta^4 V = v_{\text{glue}}(\ell, \bar{\ell}, \beta) - N_f f(\beta M)(e^{-\beta\mu} \ell + e^{\beta\mu} \bar{\ell}). \quad (6)$$

For given values of N_f and μ , the critical point $(\ell_c, \bar{\ell}_c, \beta_c, M_c)$ is determined by the set of equations¹

$$\partial_\ell V = \partial_{\bar{\ell}} V = 0, \quad (7)$$

$$\partial_\ell^2 V \partial_{\bar{\ell}}^2 V - (\partial_\ell \partial_{\bar{\ell}} V)^2 = (a \partial_\ell - b \partial_{\bar{\ell}})^3 V = 0, \quad (8)$$

with $a = \partial_\ell^2 V|_c$ and $b = \partial_\ell \partial_{\bar{\ell}} V|_c$. The first two equations rewrite

$$N_f f(\beta M) = e^{\beta\mu} \partial_\ell v_{\text{glue}} = e^{-\beta\mu} \partial_{\bar{\ell}} v_{\text{glue}}. \quad (9)$$

As in the previous case, the last two equations in (8), involving two or more ℓ and $\bar{\ell}$ derivatives, only concern v_{glue} and define two functions $\ell(\beta)$ and $\bar{\ell}(\beta)$ independent of both N_f and μ . Together with these, the ratio of the two Eqs. (9),

$$e^{-2\beta\mu} = \partial_\ell v_{\text{glue}} / \partial_{\bar{\ell}} v_{\text{glue}}, \quad (10)$$

determines an N_f -independent value for $\beta_c(\mu)$ —or, more directly, $\mu_c(\beta)$ —and in turn N_f -independent critical values $\ell_c(\mu) = \ell(\beta_c(\mu))$ and $\bar{\ell}_c(\mu) = \bar{\ell}(\beta_c(\mu))$. As before, the only source of flavor dependence comes from the prefactor of the function f in Eq. (9). Taking the ratio of any of these for two different values of N_f , we conclude that Eq. (4) still holds, for any value of μ .

Again, this can be generalized to the case of non-degenerate quark masses and we conclude, following the same lines, that the critical values $\ell_c(\mu)$, $\bar{\ell}_c(\mu)$, and $\beta_c(\mu)$ are constant along the whole critical surface and that the flavor dependence of the latter is insensitive to v_{glue} and μ . For instance, in the $2+1$ flavor case, the critical line is defined by Eq. (5). Only the actual *location* of the critical line depends on v_{glue} and μ , through the determination of R_3 in Eq. (5). This is demonstrated in Fig. 1.

Finally, Eq. (9) gives the μ dependence of R_{N_f} in terms of the functions $\beta_c(\mu)$, $\ell_c(\mu)$ and $\bar{\ell}_c(\mu)$, defined above. We also emphasize that the above discussion is valid for both real and imaginary chemical potential. In this respect, it is interesting to mention that the phase diagram at imaginary chemical potential features a tricritical point, which results in a particular scaling of both β_c and R_{N_f} when approaching $\beta\mu = i\pi/3$ [24]. The latter can be analytically continued to real μ and is actually well reproduced by lattice data and by various continuum approaches. The existence of a tricritical point is intimately related to the Roberge-Weiss symmetry of the potential for $\beta\mu = i\pi/3$, which reads $V(\ell, \bar{\ell}) = V(e^{i2\pi/3}\bar{\ell}, e^{-i2\pi/3}\ell)$. To see this, it is convenient to change to the real variables x and y defined by $\ell = e^{i\pi/3}(x - iy)$ and $\bar{\ell} = e^{-i\pi/3}(x + iy)$, in terms of which the Roberge-Weiss

¹For $\mu \in \mathbb{R}$, the physical values of ℓ and $\bar{\ell}$ are real. Therefore, it is enough to consider $V(\ell, \bar{\ell})$ with real and independent variables. For $\mu \in i\mathbb{R}$, one can conveniently work instead with $\bar{\ell} = \ell^*$ [23].

FIG. 1. Top right corner of the Columbia plot. The squares represent the $N_f = 3$ model-dependent initial values for R_{N_f} , with $\beta\mu \approx 0.2n$ and $n \in \mathbb{N}$, here obtained from GZ1. The curves are determined uniquely from Eq. (5) and lie on top of those obtained from the numerical solution of the model.

symmetry rewrites $y \rightarrow -y$. Defining $x(y)$ from the condition $\partial_x V = 0$ and evaluating the potential along this line, one obtains a reduced potential $V_r(y)$ with $\mathbb{Z}_2$ symmetry $y \rightarrow -y$. The tricritical point corresponds to the cancellation of both the second and the fourth derivatives of $V_r(y)$ at $y = 0$. Below, we determine the tricritical point both by following the boundary line of the Columbia plot as $\beta\mu$ approaches $i\pi/3$ or directly from the reduced potential at $\beta\mu = i\pi/3$.

It is interesting to test the above considerations on various one-loop approaches available in the literature. These include the matrix model of Ref. [18], the CF model at one-loop order [15], as well as the GZ-type model of Refs. [20,21]. In this latter case, no results are available for the Columbia plot. We produce them here after briefly reviewing the approach.

The model for the glue potential proposed in Refs. [20,21] is inspired from the GZ quantization in the vacuum, where the restriction of the path integral to the first Gribov region is implemented by means of a suitably adjusted Gribov parameter. The extension of this approach to finite temperature proposed in [20,21] yields a glue potential in the form $v_{\text{glue}}(\ell, \bar{\ell}, \beta) = \beta^4 W(\ell, \bar{\ell}, \beta, \{\gamma_\kappa\})$, where the Gribov parameters γ_κ can be, *a priori*, different for each color mode κ and are functions of ℓ , $\bar{\ell}$, and T , determined from the gap equations $\partial_{\gamma_\kappa} W = 0$. The function W has been computed to one-loop order in these references, where it was expressed in terms of a background gauge field $\beta \bar{A}_\mu(x) = \delta_{\mu 0} r_j t^j$, with t^j the generators of the Cartan subalgebra of the gauge group. For $SU(3)$, these are the two diagonal Gell-Mann matrices $\lambda^{(3)}/2$ and $\lambda^{(8)}/2$. At this order of approximation, the background field is related to the Polyakov loops as

$$\ell(r) = \bar{\ell}(-r) = \frac{1}{3} \left[e^{-i\frac{r_3}{\sqrt{3}}} + 2e^{i\frac{r_3}{2\sqrt{3}}} \cos(r_3/2) \right]. \quad (11)$$

The color modes κ correspond either to one of the Cartan directions j or to any of the roots α of the gauge algebra. In Ref. [21], three scenarios for the color dependence of the Gribov parameters have been proposed, all compatible with the symmetries of the problem:

GZ1: $\gamma_\kappa = \gamma, \forall \kappa$.

GZ2: $\gamma_\kappa = \gamma_1$ if $\kappa = j$ and $\gamma_\alpha = \gamma_2, \forall \alpha$.

GZ3: $\gamma_\kappa = \gamma_1$ if $\kappa = j$ and $\gamma_\alpha = \gamma_{-\alpha}$.

We stress that, when computing the derivatives of the glue potential in Eqs. (7) and (8), one needs to take into account the ℓ and $\bar{\ell}$ dependence of the Gribov parameters. Taking derivatives of the gap equation $\partial_\gamma W = 0$, one gets, for example in the case GZ1, $\partial_\ell \gamma = -\partial_{\ell,\gamma}^2 W / \partial_{\gamma,\gamma}^2 W$ and similarly for other derivatives.

We compute the values of R_{N_f} for various N_f in each scenario and compare them to lattice results. At the order of approximation considered here, these quantities do not depend on the value of the Gribov parameter at zero temperature and are, therefore, a stringent test for the various scenarios. Our results are gathered in Table I and compared to other approaches. We observe that, among the various one-loop approaches considered here, the degenerate GZ approach (GZ1) gives the best results as compared to the lattice values. Neglecting the background dependence of the γ_κ 's yields the values referred to as GZ0. We also note that the nondegenerate case (GZ3) is completely discarded: For $N_f = 1$, we find a first order phase transition irrespectively of the value of the quark mass and the values for R_2 and R_3 are way too small.

One easily checks that the universal equation (4) is accurately satisfied, given the precision, for all one-loop results in Table I. In contrast, the lattice values do not satisfy the scaling (4) well. As we discuss below, they follow a somewhat different scaling, where the function $f(x)$ is replaced by a simple exponential.

In Table I, we also quote the results from two calculations beyond one-loop order, namely, the two-loop perturbative calculation in the CF model of Ref. [16] and the DSE results of Ref. [14]. In this case, the direct

TABLE I. R_{N_f} for $N_f = 1, 2$, and 3 degenerate quark flavors, as computed in various approaches. CF1 and CF2 refer to the one- and two-loop results within the CF model. The last two lines of the table gather results beyond one-loop order.

$\mu = 0$	R_1	R_2	R_3	R_2/R_1	R_3/R_2	Y_3
Lattice [13]	7.23	7.92	8.33	1.10	1.05	1.59
GZ1	7.09	7.92	8.40	1.12	1.06	1.58
GZ2	9.45	10.25	10.72	1.08	1.05	1.58
GZ3	...	1.33	2.12	...	1.59	...
GZ0	4.66	5.56	6.07	1.20	1.09	1.59
Matrix [18]	8.04	8.85	9.33	1.10	1.05	1.59
CF1 [15]	6.74	7.59	8.07	1.12	1.06	1.58
CF2 [16]	7.53	8.40	8.90	1.11	1.06	1.57
DSE [14]	1.42	1.83	2.04	1.29	1.11	1.51

comparison of critical masses is complicated by nontrivial mass renormalization beyond leading order. As argued in Ref. [16], this can be partially absorbed in the ratios $R_{N_f}/R_{N'_f}$. In particular, these ratios for DSE agree well with the other continuum approaches despite the low values of R_{N_f} . Note that the same argumentation does not save the scenario GZ3, first, because there is no reason to expect such mass renormalization effect at one-loop order and, second, because the ratio R_3/R_2 is bad anyway as compared to all other continuum approaches.

In the same vein, as discussed in Ref. [16], the lattice also brings additive mass renormalizations because it explicitly breaks chiral symmetry. Such effects are suppressed by taking ratios of differences, e.g.,

$$Y_{N_f} = \frac{R_{N_f} - R_1}{R_2 - R_1}. \quad (12)$$

In Table I, we quote the results for Y_3 , which is surprisingly stable for all the approaches (continuum and lattice). As far as continuum models of the form (1) are concerned, this is a simple consequence of the scaling law (4) and the large values of R_{N_f} . Using the asymptotic expansion of the Bessel function, one easily checks that

$$Y_{N_f} \approx \frac{\ln N_f}{\ln 2}, \quad (13)$$

up to relative corrections of $\mathcal{O}(R_1^{-2})$. This yields $Y_3 \approx 1.58$, in excellent agreement with our results in Table I.

It is remarkable that the results for Y_3 for all approaches beyond one-loop agree well with the prediction (13). We can understand the lattice value from the N_f scaling observed in Ref. [13]

$$N_f e^{-R_{N_f}} \cosh(\beta_c \mu) \approx 0.00075, \quad (14)$$

valid for all values of μ . This yields the scaling law $\exp(R_{N'_f} - R_{N_f}) = N'_f/N_f$, from which one immediately obtains Eq. (13) using the fact that the lattice value of β_c is found insensitive to N_f . Similarly, at leading order in the

TABLE II. R_{N_f} at $\beta\mu = i\pi/3$, for $N_f = 1, 2$ and 3 degenerate quark flavors, as computed in various approaches.

$\beta\mu = i\pi/3$	R_1	R_2	R_3	R_2/R_1	R_3/R_2	Y_3
Lattice [13]	5.56	6.25	6.66	1.12	1.07	1.59
GZ1	5.02	5.91	6.42	1.18	1.09	1.57
GZ2	7.51	8.34	8.82	1.11	1.06	1.58
Matrix [19]	5.00	5.90	6.40	1.18	1.08	1.56
CF1 [15]	4.72	5.63	6.14	1.19	1.09	1.57
CF2 [16]	5.47	6.41	6.94	1.17	1.08	1.57
DSE [14]	0.41	0.85	1.11	2.07	1.31	1.59

hopping (i.e., large quark mass) expansion, the lattice results satisfy the law (5) with $f(x) \rightarrow e^{-x}$ [12].

We conclude that the scaling law (13) is quite robust and universal (independent of the actual gluon dynamics) and can thus be used to predict the values of R_{N_f} for $N_f \geq 3$, given R_2 and R_1 in the various approaches. We have checked that these predictions describe well the actual results in the one-loop models GZ1, GZ2, and CF1, as expected. We have also verified that the same holds for the two-loop values of R_{N_f} in CF2.

The results for an imaginary chemical potential, and more precisely along the tricritical line at $\beta\mu = i\pi/3$, are gathered in Table II. We verify that the law (4) and its consequences as described above are well verified by the values of R_{N_f} for one-loop models. Again, the GZ1

scenario seems to be giving the best values to date, although they are in this case pretty close to the ones from the matrix model of Ref. [19].

As anticipated, the values of Y_3 from all approaches agree well with the prediction (13). This is to be expected from the above discussion for both one-loop models and Lattice results. The DSE value is strikingly good despite the low values of R_{N_f} and the not so good values of the ratios $R_{N_f}/R_{N'_f}$. This supports the conjecture of the universal character of Y_{N_f} .

ACKNOWLEDGMENTS

We thank Daniel Kroff for related work on the Gribov-Zwanziger model.

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