Detailed spectroscopy of doubly magic ¹³²Sn

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The structure of the doubly magic ${}^{132}_{132}$ Sn₈₂ has been investigated at the ISOLDE facility at CERN, populated both by the β^- decay of 132 In and β^- -delayed neutron emission of 133 In. The level scheme of 132 Sn is greatly expanded with the addition of 68 γ transitions and 17 levels observed for the first time in the β decay. The information on the excited structure is completed by new γ transitions and states populated in the β -*n* decay of 133 In. Improved delayed neutron emission probabilities are obtained both for 132 In and 133 In. Level lifetimes are measured via the advanced time-delayed $\beta\gamma\gamma$ (t) fast-timing method. An interpretation of the level structure is given based on the experimental findings and the particle-hole configurations arising from core excitations both from the N = 82 and Z = 50 shells, leading to positive- and negative-parity particle-hole multiplets. The experimental information provides new data to challenge the theoretical description of 132 Sn.

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I. INTRODUCTION

The ¹³²Sn nucleus is one of the bastions of our understanding of nuclear structure in the framework of the nuclear shell model. With 50 protons and 82 neutrons, it is one of the most exotic doubly magic nuclei within reach of current experimental facilities. One of the signatures of its doubly magic nature is the high lying first-excited state at 4041.6 keV [1–3]. This value, once scaled by a factor of $A^{1/3}$ to account for the size of the nucleus, is large in comparison to other doubly magic nuclei such as ²⁰⁸Pb and ¹⁶O, which points to a strong double shell closure. The ¹³²Sn doubly magic structure is also manifested by the almost pure single-particle nature of the levels in ¹³³Sn. This nature was probed by a transfer reaction in inverse kinematics [4] yielding very large spectroscopic factors.

The region of the nuclear chart around ¹³²Sn plays an important role in the astrophysical rapid neutron-capture process (r-process), which impacts elemental abundances in the solar system. Recently, the identification of the nucleosynthesis site for neutron-rich nuclei around N = 82 has been reported [5,6] associated to a "kilonova" [7], observed by multimessenger astronomy. The robustness of the N = 82 neutron shell is one of the important parameters when modeling r-process nucleosynthesis and describing light curves arising from compact object mergers. The shell structure in this region is also necessary to understand the role of fission in the r-process [8].

From the point of view of nuclear structure, the nuclei with a valence particle or hole around ¹³²Sn are relevant for investigating single-particle states and transition probabilities. They provide observables that are the main ingredients in state-ofthe-art large-scale shell-model calculations to understand the nuclear structure in the region. The single-particle states in the region are represented in Fig. 1 following the procedure described in Ref. [9] and employing binding energies from Ref. [10] and the excitation spectra from ¹³¹Sn, ¹³³Sn, ¹³³Sb, and ¹³¹In. In particular, the neutron single-particle orbits above the N = 82 shell gap have been taken from low-lying states in ¹³³Sn: the $\nu f_{7/2}$ ground state and the $\nu p_{3/2}$, $\nu p_{1/2}$, $vh_{9/2}$, and $vf_{5/2}$ states at 854-, 1367-, 1561-, and 2005-keV excitation energy [4,11–16]. The $v_{i_{13/2}}$ single-particle state has not been experimentally identified to date [17]. These single-particle states are not only relevant for ¹³²Sn but also for neutron-rich nuclei in its vicinity.

Experimental data on ¹³²Sn is essential for the shell-model description of the exotic nuclear region around N = 82 and to

provide insight into particle-hole couplings for both protons and neutrons. Most of the excited levels in ¹³²Sn correspond to particle-hole (p-h) configurations where a proton or a neutron is promoted across the closed shell. The coupling of singleparticle and single-hole configurations (Fig. 1) leads to multiplets of excited states with an expected low admixture of other configurations. The particle-hole residual interaction makes the level energies within a multiplet nondegenerate. The identification of these multiplets provides information on the nuclear two-body matrix elements to first order. Experimentally measured transition rates between states within a multiplet, and also between states of different multiplets, give important knowledge of the underlying single-particle structure.

The investigation of the doubly magic ¹³²Sn is thus essential for theoretical models aiming at the understanding neutron-rich nuclei in the region. The development of these models is furthermore needed for the description of r-process nuclei that are at present experimentally out of reach.

The excited structure of ¹³²Sn has been experimentally investigated since the 1970s. β -decay experiments were carried out at OSIRIS [1,18–20] and ISOLDE [2,21], and fission experiments were performed at the JOSEF facility [22,23] and the Argonne National Laboratory [24].

The most complete β -decay experiment was performed by Fogelberg *et al.* [18–20] at the OSIRIS facility in the 1990s, where the level scheme of ¹³²Sn was expanded to 21 excited levels, including negative- and positive-parity states up to the neutron separation energy. Proton particle-hole states were identified for the first time, and the 4352-keV $J^{\pi} = 3^{-}$ state was confirmed to have an octupole vibrational character. Lifetime measurements of the excited states down to the ps range were performed, and spin and parity assignments were made for the levels below 5 MeV.

Despite all the detailed studies on ¹³²Sn attained through the β -decay and fission experiments, many of the expected particle-hole multiplet states remain without experimental identification. β decay is the ideal tool to investigate the excited structure of ¹³²Sn, both directly from ¹³²In (7⁻) g.s. and via β -delayed neutron emission from the ¹³³In (9/2⁺) g.s. and the (1/2⁻) 330-keV β -decaying isomer. This is due to the large energy window available for the decay, of $Q_{\beta}(^{132}In)$ = 14140(60) keV and $Q_{\beta n}(^{133}In) = 11010(200)$ keV (from systematics) [10], respectively, and due to the high spin of the parent nuclei that makes it possible to feed many states in ¹³²Sn.



FIG. 1. Experimental single-particle and single-hole energies for neutrons (ν) and protons (π) in the doubly magic nucleus ¹³²Sn. Following Ref. [9], the energy origin is set in the center of the shell gap (λ_F) in order to remove Coulomb energy differences ΔE_C . Binding energies are taken from Ref. [10]. The absolute singleparticle energies are given in MeV.

In this work, we focus on the investigation of the excited structure of ¹³²Sn populated in β and β -*n* decay. Taking advantage of the enhanced yield and selectivity achieved at the ISOLDE facility at CERN, we have identified some of the missing particle-hole multiplet states. In addition, lifetimes of excited states in ¹³²Sn have been measured using fast-timing techniques. The results from the β -decay study of the ¹³³In isomers have been partially covered in Ref. [16]. Details on the experimental method used in the present work are provided in Sec. II. The experimental results are presented in Sec. III and discussed in Sec. IV. Conclusions are drawn in Sec. V.

II. EXPERIMENTAL DETAILS

The experiment was carried out at the ISOLDE facility at CERN. It was performed in two separate data-collection campaigns in 2016 and 2018, where the excited structure in ¹³²Sn was populated in the β decay of ¹³²In and in the β -n decay of the ¹³³In $(9/2^+)$ and $(1/2^-)$ states. The ¹³²In and ¹³³In isotopes were produced by the bombardment of a UC_r target equipped with a neutron converter by 1.4-GeV protons from the CERN PS-Booster (PSB). The indium ions thermally diffused out of the target and were ionized using the ISOLDE resonance ionization laser ion source (RILIS) [25]. The use of RILIS granted isomeric selectivity, by taking advantage of the difference in the hyperfine splitting of the isomer and ground state. More details on the isomer selection can be found in Ref. [26]. Following the ionization, indium ions were extracted and accelerated by a 40-kV potential difference, mass analyzed [27], and implanted on an aluminized mylar tape located at the center of our detector setup at the ISOLDE Decay Station (IDS) [28]. The ions reached the IDS following the time structure of the PSB supercycle whereby proton pulses were grouped into sets of 34 or 35 pulses, out of which around half of them are delivered to the ISOLDE target-unit separated in time by multiples of 1.2 s. The beam was collected on the tape for a fixed time varying from 200 to 400 ms after the impact of each proton pulse. Once every supercycle, the tape was moved in order to reduce the activity of long-lived daughter nuclides. The average beam intensity at the experimental station was of the order of 4×10^4 and 2×10^3 ions per second for ¹³²In and ¹³³In, respectively. Data were collected for 20 h for each mass.

The IDS setup consists of a set of detectors aimed at measuring the β and γ radiation emitted after the β decay of the implanted isotopes. They are arranged in close geometry surrounding the implantation point. The setup can be divided in two branches. The first branch is composed of four clover-type HPGe detectors for γ -ray spectroscopy, with a combined full-energy peak efficiency of 4% at 1173 keV. The second branch is aimed at lifetime measurement of excited states using the advanced time-delayed $\beta \gamma \gamma(t)$ (fast timing) technique [29–31]. It consists of two LaBr₃(Ce) crystals with the shape of truncated cones [32] coupled to fast photomultiplier tubes (PMTs) [33], with 1% of total efficiency at 1 MeV each, and an ultrafast 3-mm-thick NE111A plastic scintillator used as a β detector, with a $\approx 20\%$ efficiency. The energy and fast-timing signals are taken from the PMT dynode and anode outputs, respectively. The timing signals are processed by analog constant fraction discriminators and introduced in pairs in time-to-amplitude converter (TAC) modules that provide the time difference between them. In this experiment, time differences between the β and the two LaBr₃(Ce) detectors as well as between the two LaBr₃(Ce) detectors were recorded. More details on the setup are provided in Refs. [31,34].

All the signals from both branches were read and digitized by the Nutaq digital data acquisition system [35]. Logic signals, such as the time of arrival of the proton pulse on target and the tape movement, were also digitized. Data were collected in a triggerless mode. Events were built during the offline analysis where they were sorted in coincidence windows and correlated with the proton arrival time. At this stage, the energy calibration for each detector was applied, as well as add-back corrections for the clover detectors. Because of the large energy of the ¹³²Sn γ rays, a precise efficiency calibration is needed in a wide energy range. Therefore, ¹⁵²Eu, ¹³⁸Cs, ¹⁴⁰Ba, and ¹³³Ba radioactive sources were used to build the energy calibration. The calibration was extended up to 7.6 MeV by including high-energy γ rays originating from the capture of thermal neutrons produced at the ISOLDE target station, mainly in iron (IDS frame) and germanium (HPGe detectors).

For the timing measurements, the calibration of the LaBr₃(Ce) time response for full-energy peaks (FEP) as a function of energy, the FEP walk curve, is required. It was built for each LaBr₃(Ce) detector using $\beta\gamma$ (t) and $\gamma\gamma$ (t) coincidences with ¹⁴⁰Ba / ¹⁴⁰La and ¹⁵²Eu γ -ray sources, ¹³⁸Cs and ⁸⁸Rb on-line sources and by including several transitions in ¹³²Sb as an internal calibration source. In this way, we obtained FEP time response curves for each LaBr₃(Ce) detector in the energy range 100 keV to 2.6 MeV, with an average one- σ error of 3 ps. A similar procedure was implemented to build the Compton walk curve in order to take care of the corrections due to Compton events.



FIG. 2. Singles γ -ray energy spectrum recorded by the HPGe detectors following the ¹³²In decay. This histogram was built using the events measured during the 30- to 530-ms time interval after proton pulse. The strongest peaks observed in the spectra are labeled with their energies in keV. The SE and DE labels indicates single-escape and double-escape peaks. The inset is an enlargement of the 2400- to 4450-keV region.

III. EXPERIMENTAL RESULTS

The excited structure of ¹³²Sn was populated through the β decay of ¹³²In (7⁻), and from the β -*n* decay of the ¹³³In (9/2⁺) g.s. and the (1/2⁻) isomer. The large differences in the spin and parity of the parent nuclei result in distinct feeding patterns for each decay, which provides information on the spin and parity of the levels fed.

Owing to the large difference in the β -decay half-lives of ¹³²In and ¹³²Sn, of 200(2) ms and 39.7(8) s [3], respectively, the time distribution relative to the arrival of the proton on target makes it possible to identify whether a γ ray has been emitted during the β decay of ¹³²In or from the daughters. A similar situation occurs for the β decay of ¹³³In. Apart from the time distribution, the identification of the γ rays belonging to ¹³²Sn is based on γ - γ coincidences with previously known transitions.

A. β decay of ¹³²In

The Q_{β} in ¹³²In is 14140(60) keV, while the neutron separation energy in ¹³²Sn is 7353(4) keV [10]. Hence, the feeding of excited states up to \approx 7 MeV is possible in this decay and high-energy γ rays may be observed. The excited structure populated in the ¹³²In β decay is very complex. The high spin of the parent, (7⁻) [36], favors the population of high-spin (6–8) excited states in the energy range from 4 to 7 MeV. Those levels can only de-excite to the ground state by means of γ -ray cascades of three or more transitions. As discussed before, due to the doubly magic nature of ¹³²Sn, the first excited state appears at a very high energy, 4041 keV. Therefore, it is not expected to find new levels in this decay that can de-excite directly to the g.s. with an energy below 4 MeV.

The energy spectra recorded by the HPGe clover detectors, setting a time window of 30–530 ms after proton impact, are depicted in Fig. 2. This condition was imposed in order to reduce the contribution of the different contaminants. The

contribution of neutron-induced background coming from the target is suppressed by removing the first 30 ms of the time window. An upper limit of the time window at 530 ms was chosen to reduce the contribution of the long-lived daughters, while keeping most of the statistics.

1. Half-life of ¹³²In ground state

The half-life of ¹³²In was measured by fitting the time distribution of the 10 strongest γ rays (labeled in Fig. 2 except for the 4416 keV). Since the activity at the experimental station is pulsed by the proton beam structure and the release from the target, the time distribution is fitted to an exponential decay function with a constant background after the end of the implantation. The background contribution was estimated by analyzing the time range from 2400 to 3600 ms after proton impact. Because of the high count rates, dead-time effects are sizable, mainly during implantation, but also at the beginning of the decay. In each HPGe crystal, an average count rate of 3×10^3 counts per seconds (cps) was observed; however, during the implantation time the count rate could rise up to 1.5×10^4 cps. To account for this effect, the beginning of the fit range was shifted by a few half-lives toward higher times and a χ^2 fit test was performed to verify that the expected exponential decay behavior was recovered. The lifetime measurement was performed independently for each of the two data sets of ¹³²In decay measured in the two experimental campaigns. The analysis made use of single events recorded in the HPGe detectors. The contribution of the Compton background under full-energy peaks was subtracted. This investigation furnishes 20 independent values for the ¹³²In. 10 from each data set, which are all statistically compatible with each other. The final value of the ¹³²In half-life was adopted as the weighted average of these measurements yielding $T_{1/2} = 202.2(2)$ ms. The statistical uncertainty of the weighted average is calculated and increased by multiplying by the χ^2 obtained. No systematic error is included. This half-life is in agreement with, but more precise than, the value reported in the latest evaluation, $T_{1/2} = 200(2)$ ms [3]. In Fig. 3, the decay curves for four of the γ rays under consideration, from the 2016 data set, are shown.

2. Identification of new y rays in ¹³²Sn

The analysis of γ - γ coincidences was done using the full statistics independently for the two data sets from each campaign. The assignments were cross checked by requiring coincidences with the β detector and/or a time range since proton impact from 30 to 530 ms. Figure 4 shows the γ rays in coincidence with the $6^+ \rightarrow 4^+$ 299.3-keV transition in ¹³²Sn. The spectrum illustrates the amount of statistics and the quality of the γ -ray coincidence spectra.

The level scheme of 132 Sn has been greatly expanded with the addition of 57 new γ transitions and 11 new levels, observed following the direct 132 In β decay. The level scheme is shown in Fig. 5. A list of the γ rays is provided in Table I.

The states located at 5766 and 5446 keV were previously observed in the β -delayed neutron emission of ¹³³In [16]. The assignment is confirmed in this work with the uncovering of new cascades in the ¹³²In decay involving both levels.



FIG. 3. Decay curves of the 375-, 4042-, 2268- and 4352-keV γ rays recorded in singles in the HPGe detectors. The region considered for the fit goes from 700 ms, marked with a dark-blue dashed line, up to 2400 ms. This region has been adjusted in order to minimize dead-time effects.

A new level is found at 5754 keV defined by the 1457to 1038-keV γ cascade. This sequence had already been observed by Fogelberg *et al.* [18]; however, the order of the γ rays they proposed was inverted, giving rise to an excited level at 6173 keV with suggested (6⁺) spin parity. This level has been ruled out in our analysis due to the finding of another γ ray that de-excites the 5754-keV state, confirmed by γ - γ coincidences.

The 5280-keV level was already reported in ²⁴⁸Cm fission studies [24], and tentatively identified as the (9⁺) state that arises from the particle-hole $\nu f_{7/2}h_{11/2}^{-1}$ configuration. That level is confirmed in this work by the observation of the de-exciting 431.8-keV transition in delayed coincidence with the 132-keV γ -ray that de-excites the 8⁺ 4848-keV level.

The direct β feeding to states in ¹³²Sn was determined from the balance between feeding and de-exciting γ rays to each level. The intensities of the γ rays were obtained from the measured HPGe singles with neither coincidence nor condition on the time from the impact of protons on target. Theoretical internal conversion coefficients have been taken from Ref. [37] if required. The β feeding to the states should be understood as upper limits and the log*ft* values as lower limits due to possible missing transitions.

3. β -delayed neutron branches in ¹³²In

The β -delayed one neutron emission of ¹³²In has been confirmed by the observation of γ rays belonging to the excited structure of ¹³¹Sn. Two transitions have been identified in this decay, specifically, at 2435.0(3) and 4273.6(5) keV, with absolute intensities of 0.11(1)% and 0.04(1)%, respectively. The P_n value has been obtained from the analysis of the γ -ray intensities of the β and β -*n* branches, following the β decay of the ¹³²Sn and ¹³¹Sn daughters. For the ¹³²Sn \rightarrow ¹³²Sb decay branch, the intensities of the five most intense γ rays were considered. The absolute intensities for those transitions were adopted from Ref. [38]. Previous measurements of the 131 Sn \rightarrow 131 Sb decay [39] were not able to disentangle the decay of the ¹³¹In isomers. Besides, in our analysis we observed that the intensity of the γ rays emitted in this decay mainly originate from the population of levels with high spin (11/2,13/2, 15/2). This indicates that the ¹³²In isotopes that decay by β -n mostly feed the 11/2⁻ isomer in ¹³¹Sn directly, which is strongly favored against the $3/2^+$ g.s. due to the angular momentum difference.

The total intensity from ${}^{131}\text{Sn} \rightarrow {}^{131}\text{Sb}$ decay was calculated from the analysis of the γ rays from ${}^{131}\text{Sb}$ observed in this data set. An absolute intensity of 69(7)% has been estimated for the most intense transition of 1226 keV. This value was obtained by making two assumptions: first that ${}^{132}\text{In} \beta$ -*n* decay mainly populates the $(11/2^-)$ isomer, which is consistent with our observations, and second that no direct intensity was lost due to direct population of ${}^{131}\text{Sn}$ to the ${}^{131}\text{Sb}$ g.s. This is to be expected in order to be consistent with the first assumption due to the large spin difference $(11/2^- \rightarrow 7/2^+ \text{ transition})$. The 7% uncertainty in the value takes into account these assumptions.

Finally, the number of decays calculated for each tin isotope was corrected to account for the movement of the tape at



FIG. 4. Compton-subtracted $\gamma \cdot \gamma$ energy spectrum gated on the 6⁺ \rightarrow 4⁺ 299.3-keV γ transition in ¹³²Sn. The previously known γ rays are labeled with their energies in black. New transitions identified in this work are labeled in red with an asterisk. The negative peaks in the spectrum arise from background subtraction, due to Compton scattering between two HPGe clover detectors.



FIG. 5. Level scheme of ¹³²Sn observed following the β decay of ¹³²In. Note that the energy gap from the g.s. to the 2⁺₁ state is not to scale. The positive-parity states are shown on the left-hand side and the negative-parity ones on the right-hand side. The high-lying 7⁻ and 6⁻ states feed states of both parities. Levels and transitions previously observed in this decay are colored in black, while those observed for the first time are highlighted in red. Levels previously known from ²⁴⁸Cm fission or from ¹³³In β -*n* decay and observed here in the β decay of ¹³²In are colored in blue.

TABLE I. List of γ rays observed in the β decay of ¹³²In to ¹³²Sn, including transition energies and intensities. The initial and final levels for each connecting transition are also given.

E_i	J_i^{Π}	E_{f}	J_f^Π	E_{γ}	I_{γ}^{a}
(keV)		(keV)	5	(keV)	
4041.6(3)	2^{+}	0	0^+	4041.6(3)	100(11)
4351.6(3)	3-	0	0^+	4351.5(3)	43(5)
. ,		4041.6(3)	2^{+}	310.5(3)	4.2(3)
4416.6(3)	4^{+}	0	0^+	4416.7(3)	16(2)
		4041.6(3)	2^{+}	374.9(3)	100
		4351.6(3)	3-	64.4(3)	1.29(9)
4715.9(4)	6^+	4416.6(3)	4^{+}	299.3(3)	82(6)
4830.5(4)	4^{-}	4351.6(3)	3-	478.9(3)	45(3)
		4416.6(3)	4^{+}	414.5(3)	0.79(6)
4848.3(5)	8^+	4715.9(4)	6^{+}	132.4(3)	26(2)
4885.7(5)	5^{+}	4416.6(3)	4^{+}	469.1(5)	2.5(2)
		4715.9(4)	6^+	169.5(4)	$0.12(5)^{b}$
4918.8(5)	7^{+}	4715.9(4)	6^{+}	202.9(3)	8.0(6)
		4848.3(5)	8^+	70.9(4)	1.2(2) ^b
4942.4(4)	5-	4351.6(3)	3-	590.4(3)	1.07(8)
		4416.6(3)	4+	525.9(3)	33(2)
		4715.9(4)	6^+	226.5(3)	0.67(5)
10.10.0(5)	(2-)	4830.5(4)	4	111.3(3)	2.8(2)
4949.0(5)	(3-)	4830.5(4)	4-	117.9(5)	$0.012(4)^{\circ}$
		4331.0(3)	$\frac{3}{2^+}$	397.4(0) 908 2(4)	$0.11(3)^{\circ}$
5280 0(6))	(0^{\pm})	4949 2(5)	2 0+	421.8(4)	$0.63(6)^{b}$
5200.0(0))	(9^{-1})	4040.3(3)	0 2-	431.0(4)	0.03(0)
5587.5(5)	(4)	4331.0(3) 4830.5(4)	3 4-	1030.0(3) 557 1(4)	1.29(11) 0.13(2)
		4830.3(4) 4942.4(4)	4 5-	4446(4)	0.13(2) 0.23(3)
		4949.0(5)	(3^{-})	437.2(4)	0.23(2)
5398.9(5)	(6^{+})	4715.9(4)	6+	683.0(3)	3.9(3)
5446 4(5)	(4^+)	4416 6(3)	4^+	1029 8(4)	0.26(3)
5478 4(6)	(1^{+})	4848 3(5)	8+	630 2(3)	4 6(3)
5628 0(2)	(0^{+})	47150(4)	6+	012 1(3)	+.0(3)
5028.9(5)	(r)	4848 3(5)	8+	780 6(3)	5.0(4)
		4918.8(5)	7+	710.1(3)	2.0(2)
		5398.9(5)	(6^{+})	229.8(3)	0.65(5)
		5478.4(6)	(8^+)	150.3(3)	$0.29(3)^{b}$
5697.7(3)	(5+)	4416.6(3)	4+	1280.7(3)	0.134(13)
		4715.9(4)	6^+	982.2(5)	$0.08(2)^{b}$
		4885.7(5)	5^{+}	812.4(6)	$0.05(2)^{b}$
5753.9(4)	(6^+)	4715.9(4)	6^{+}	1038.2(3)	1.8(2)
		5398.9(5)	(6^{+})	354.3(3)	0.58(4)
5766.3(3)	(5+)	4416.6(3)	4+	1349.6(3)	0.27(2)
		4715.9(4)	6^+	1050.3(4)	0.122(10)
		4885.7(5)	5-	881.7(3)	0.114(14)
(000, 2 (4))	(7+)	4942.4(4)	5	823.2(7)	0.068(3)
0008.2(4)	(/+)	4/13.9(4)	0 ⁺	1292.2(5)	$0.042(7)^{\circ}$
		4040.3(3) 4918 8(5)	0' 7+	100.1(3) 1080.1(4)	0.103(13) 0.15(2)
		5398.9(5)	(6^{+})	609.4(4)	0.37(5)
6235 5(3)	(7^{+})	4715 9(4)	6+	1519 6(3)	$0.54(5)^{b}$
5255.5(5)	(r)	4918.8(5)	7 ⁺	1317.1(3)	0.31(3)
		5398.9(5)	(6+)	836.3(4)	0.64(6)
		5753.9(4)	(6^+)	481.8(3)	0.53(6)

TABLE I. (Continued.)								
E:	J^{Π}	Er	J^{Π}_{c}	E.,	Lua			
(keV)	U ₁	(keV)	• _f	(keV)	- γ			
6206 6(5)	(5-)	4820 5(4)	4-	1466 1(2)	0.120(15)			
(424.2(2))	(5)	4030.3(4)	4	1710.2(4)	0.120(13)			
6434.2(3)	(5))	4/15.9(4)	0' 5+	1/18.3(4) 1548.5(4)	0.091(10) 0.14(2)			
		4005.7(5) 5446 4(5)	(4^+)	987.7(3)	0.14(2) 0.14(4) ^b			
6476 3(4)	(5-)	4830 5(4)	Δ ⁻	1645 6(3)	0.11(1) 0.40(7)			
0470.3(4)	(5)	4942.4(4)	4 5-	1534 8(5)	0.40(7) 0.085(9)			
6492 8(3)	$(6, 7^+)$	5398 9(5)	(6^+)	1093 9(3)	0.73(5)			
6526 2(5)	(6, 7)	5628 9(3)	(7^+)	897 3(3)	0.73(3) 0.32(4)			
6508 5(5)	(0-0)	4042 A(4)	5-	1656 1(3)	4.0(3)			
0398.3(3)	(0)	4942.4(4) 5398.9(5)	(6^+)	1030.1(3) 1199.6(5)	4.0(3) 0.036(10) ^b			
6630 6(4)	(6^{+})	4715 0(4)	(0 ⁻)	1014.6(3)	2.5(2)			
0030.0(4)	(0^{+})	4/13.9(4)	5+	1914.0(3) 1745.1(5)	2.3(2)			
		4018 8(5)	5 7+	1743.1(3) 1711 6(3)	0.23(3) 0.24(2)			
		5398.9(5)	(6^+)	1/11.0(3) 1231.9(4)	0.24(2) $0.27(3)^{b}$			
6700 7(4)	(6^{-})	4018 8(5)	7+	1701.0(3)	0.42(4)			
0709.7(4)	(0)	4942.4(4)	5-	1767.2(3)	$3.2(3)^{b}$			
6733 4(4)	(5^{+})	<i>1/</i> 16 6(3)	۵ 4+	2317 1(4)	0.008(10)			
0755.4(4)	(5)	48857(5)	+ 5+	1847 5(3)	0.098(10) $0.12(2)^{b}$			
6005 0(4)	(7+)	4010 0(5)	7+	1077 1(2)	0.12(2)			
0893.8(4)	(T^{*})	4918.8(<i>3</i>) 5398.9(5)	(6^+)	1977.1(3)	0.31(3) 0.37(3)			
6007 1(2)	(7+)	47150(4)	(0) 4+	170.0(3)	0.37(3)			
0997.1(3)	(T^{*})	4/13.9(4)	$\frac{0}{7^+}$	2201.0(3) 2078 3(3)	0.33(3) 0.22(2)			
		54784(6)	(8^+)	2078.3(3) 1519 2(5)	0.22(2) 0.14(2) ^b			
		5628.9(3)	(7^+)	1319.2(3) 1368.2(5)	0.14(2) $0.43(5)^{b}$			
7210 8(3)	6-	4830 5(4)	<u>4</u> -	2380.0(3)	38(3)			
7210.0(3)	0	48857(5)	 5+	2300.0(3) 2325 5(3)	0.85(6)			
		4918 8(5)	5 7+	2323.3(3) 2292.2(3)	1.04(10)			
		4942.4(4)	, 5-	2292.2(3) 2268.7(3)	27(2)			
		5387.3(3)	(4 ⁻)	1823.2(3)	1.41(10)			
		5398.9(5)	(6+)	1812.6(6)	0.12(1)			
		5628.9(3)	(7^{+})	1582.1(3)	1.16(9)			
		5697.7(3)	(5 ⁺)	1513.8(3)	0.34(3)			
		5753.9(4)	(6^{+})	1456.9(3)	1.44(11)			
		5766.3(3)	(5 ⁺)	1445.1(3)	0.49(4)			
		6008.2(4)	(7+)	1202.4(6)	0.024(7) ^b			
		6235.5(3)	(7^{+})	975.6(3)	1.4(2) ^b			
		6296.6(5)	(5-)	913.9(4)	0.121(14) ^b			
		6434.2(3)	(5 ⁺)	777.4(3)	$0.15(2)^{\circ}$			
		64/6.3(4)	(5)	(133.5(3))	0.38(3)			
		67007(4)	(0) (6^{-})	5012.0(3)	0.42(3) 1.7(4)			
		66306(4)	(0^{+})	580.8(5)	$0.09(2)^{b}$			
7244 0(2)	7-	4715 0(4)	(0 ⁺)	2507.0(3)	1.47(10)			
7244.0(5)	/	4/13.9(4)	8+	2327.9(3) 2305 $4(3)$	1.47(10) 2 3(2)			
		4947 4(4)	5-	2393.4(3) 2301 3(3)	2.3(2) 2.0(2)			
		53989(5)	(6^+)	1845 3(3)	0.46(3)			
		5478.4(6)	(8^+)	1766.2(3)	3.2(3) ^b			
		5753.9(4)	(6 ⁺)	1489.4(4)	0.084(11)			
		6235.5(3)	(7 ⁺)	1008.1(5)	0.11(2)			
		6492.8(3)	$(6, 7^+)$	751.3(3)	0.124(12)			

^aRelative γ intensities normalized to 100 units for the 4⁺ \rightarrow 2⁺ 375-keV transition. For intensity per 100 decays of the parent, multiply by 0.56(4).

^bIntensity from γ - γ coincidences.

the end of each supercycle, considering the different half-lives of each isotope and for dead time effects. From this analysis, a $P_n = 12(2)\%$ value was found for the ¹³²In β -*n* decay, which is notably higher than the 6.8(14)% in Ref. [40] but in good agreement with the 10.7(33)% from Ref. [41].

Given the two-neutron separation energy in the ¹³²Sn $S_{2n}(^{132}Sn) = 12557.0(27)$ keV [10], there is a 1583-keV energy window, within $Q_{\beta}(^{132}In)$, that makes the decay via a β -delayed two-neutron branch possible. We have searched for γ rays belonging to the A = 130 mass chain. Nevertheless, no evidence has been found that would point to the existence of a β -2n decay branch in ¹³²In. This is consistent with expectations, since the only levels in ¹³⁰Sn that could be populated are the 0⁺ g.s. and 2⁺ at 1221 keV [42]. Assuming a (7⁻) spin-parity assignment for the ¹³²In g.s. [36], this decay will be highly suppressed.

B. β -delayed neutron decay of ¹³³In

The large $Q_{\beta} = 13.4(2)$ MeV value along with the low neutron separation energy in ¹³³Sn, $S_n = 2.399(3)$ MeV [10], favor the ¹³³In decay via β -delayed neutron emission to ¹³²Sn. This gives rise to the large P_n values for both ¹³³In β -decaying isomers [16]. The lower spin of the ¹³³In (9/2⁺) ground state and (1/2⁻) isomer, in comparison with ¹³²In (7⁻), is expected to favor the population of low spin p-h excited states that are not fed in the β decay of ¹³²In due to the large spin of the parent (7⁻). The population of ¹³²Sn excited levels in the β decay of ¹³³In was already reported in Ref. [16], where the β decay of ¹³³In was investigated focusing on the excited structure of ¹³³Sn. In the present work, we concentrate on results of the β -*n* decay of ¹³³In to ¹³²Sn, discuss excited states in ¹³²Sn, and report new transitions following the β -*n* decay branch of ¹³³In.

1. Feeding of excited states in ¹³²Sn

 γ rays emitted after the β decay of ¹³³In can be clearly distinguished from the background by their time distribution following the impact of protons on target. Nevertheless, the decay curve does not allow the separation of the transitions that belong to ¹³²Sn from those of ¹³³Sn or from the background induced by β -delayed neutrons from ¹³³In β -*n* decay.

The identification of new γ rays that belong to 132 Sn is based on γ - γ coincidences. γ rays with energies below 4 MeV are always a part of a cascade since they cannot directly feed the g.s. The analysis allows to identify several levels and γ rays in 132 Sn that are not observed in the 132 In decay; see Fig. 6. Among them, we confirm the states at 4965, 5131, 5431, and 5790 keV.

The low spin of the states to which they can de-excite suggests a small spin value (2–4) for these levels, which makes them good candidates for the remaining particle-hole states with low spin expected in this energy range. In Fig. 7, the level scheme of ¹³²Sn in the β -*n* decay of ¹³³In is depicted. The direct feeding to each level ($I_{\beta-n}$) is measured by analyzing the γ -ray intensities calculated separately for each isomer. The indium beams for each isomer were separated, taking advantage of the isomer selectivity provided by RILIS. However, the separation was not complete, and the ^{133m}In



FIG. 6. $\gamma \cdot \gamma$ spectrum observed in the β decay of ¹³³In, gated on the 4352-keV transition in ¹³²Sn. The contribution from Compton events beneath the 4352-keV peak has been subtracted. Newly observed γ transitions are labeled in red with an asterisk.

beam contained a contribution of $\approx 30\%$ of 133g In [16]. The amount of 133m In in the 133g In beam is less than 5%. The total feeding has been calculated using the intensities of the γ rays emitted by the daughters. The observed states in 132 Sn following the β -*n* decay of the 133 In (9/2⁺) g.s. and (1/2⁻) isomeric state are listed in Table II.

2. High-energy y rays

Another interesting feature observed in the β decay of ¹³³In is the presence of several γ rays at very high energies, above 5 MeV, with a time behavior compatible with the decay of ^{133g,m}In. The existence of those γ rays was already reported in Ref. [16], where the 6088-keV transition was assigned to ¹³³Sn. Some other γ rays were discussed in Ref. [16] as being emitted in the decay of ¹³³In; however, the lack of γ - γ coincidences does not allow us to identify the daughter tin isotopes they belong to.

The high-energy γ lines observed in the ^{133g,m}In decays are shown in Fig. 8. As it can be seen, the observed peaks differ notably depending on the selected β -decaying indium state. In the decay of the ^{133g}In (9/2⁺) g.s. there are two predominant γ rays, the one at 6088 keV mentioned above and another one at 6019 keV. Although the 6019-keV peak has the same energy as a transition in ⁵⁷Fe produced by the neutron background, as discussed in Ref. [16], its intensity is only a small fraction of the total γ -ray intensity from the excited 7647-keV level in ⁵⁷Fe, while the other, more intense transitions, are not observed. Therefore, the 6019-keV transition is likely to be emitted following the β decay of ¹³³In and predominantly from the (9/2⁺) g.s.

In the decay of the ^{133m}In (1/2⁻), the 6088- and 6019-keV transitions are suppressed, but several other peaks, which are absent in the decay of the ^{133g}In, can be identified. Those peaks appear at the energies of 5440, 5712, 5770, 5952, and 6067 keV. Two more tentative peaks, at the detection limit of the HPGe detectors, are seen at 6220 and 6463 keV. Some of these γ lines may be compatible with escape peaks from other γ rays (for instance, single and double escape peaks from 6463 keV), but it is not possible to make a consistent identification for all of the energies. It is interesting to ob-



FIG. 7. Level scheme of ¹³²Sn observed following the β -*n* decay of the ¹³³In (9/2⁺) ground state and (1/2⁻) isomer. Note that the energy gap from the g.s. to the 2⁺₁ state is not to scale. The positive-parity states are on the left-hand side and the negative-parity states are to the right. The isomer observed feeding to levels in ¹³²Sn is provided separately for each decay. Note contributions coming from beam impurity cannot be excluded in the (1/2⁻) decay. Levels and transitions observed for the first time in the β decay of ¹³³In are highlighted in red.

TABLE II. List of observed states in ¹³²Sn following the β -*n* decay of the ¹³³In (9/2⁺) g.s. (>95% pure), labeled ^{133g}In, and the beam with enhanced content of the (1/2⁻) isomeric state, with a contamination of \approx 30% of ^{133g}In, labeled ^{133m}In.

$\overline{E_i}$ (keV)	J_i^{Π}	E_f (keV)	J_f^Π	E_{γ} (keV)	$I_{\rm rel}^{\rm c}$ ^{133g} In	$I_{\rm rel}^{\rm d}$
4041 6(2)	2+	0	0+	4041 6(2)	100	100
4041.0(3)	2-	0	0+	4041.0(3)	54(8)	70(11)
4331.0(3)	3	0	$\frac{0}{2^+}$	4351.5(3)	54(8) 7 0(9)	12(2)
4416 6(3)	4+	0	2 0+	<i>AA</i> 16 <i>7</i> (3)	13(2)	0(2)
4410.0(3)	4	4041 6(3)	2^+	374 9(3)	74(9)	9(2) 39(6)
		4351.6(3)	2- 3-	64.4(3)	0.96(11) ^b	$0.51(7)^{b}$
4715.9(4)	6+	4416.6(3)	4+	299.3(3)	31(4)	13(2)
4830.5(4)	4-	4351.6(3)	3-	478.9(3)	18(2)	18(2)
		4416.6(3)	4+	414.5(3)	0.9(5)	0.21(8) ^a
4848.3(5)	8+	4715.9(4)	6+	132.4(3)	4.0(6)	<2ª
4885.7(5)	5^{+}	4416.6(3)	4^{+}	469.1(5)	11.1(14)	7(2)
		4715.9(4)	6^+	169.5(4)	1.5(7) ^a	<1.6 ^a
4918.8(5)	7^{+}	4715.9(4)	6^+	202.9(3)	5.4(8)	3(2)
		4848.3(5)	8^+	70.9(4)	0.8(1) ^b	0.4(2) ^b
4942.4(4)	5^{-}	4351.6(3)	3-	590.4(3)	$0.7(6)^{a}$	0.22(3) ^b
		4416.6(3)	4^{+}	525.9(3)	10.1(14)	6.6(10)
		4715.9(4)	6+	226.5(3)	0.21(3) ^b	0.14(2) ^b
		4830.5(4)	4-	111.3(3)	1.0(3)	0.56(9) ^b
4949.0(5)	(3 ⁻)	4830.5(4)	4-	117.9(5)	1.4(4)	1.0(7)
		4351.6(3)	3^{-}	597.4(6)	$8(2)^{a}$	12(4) ^a
10(5.2(7))	(2+)	4041.0(3)	Z '	908.2(4)	1.5(5)	<8
4965.3(7)	(31)	4416.6(3)	4' 2-	549.0(4) 613 5(5)	1.0(6)	$1.9(8)^{a}$
		4041.6(3)	2^{+}	923.8(7)	2.4(5)	3.2(12)
5131.2(6)	(2^{-})	4351 6(3)	- 3-	779 2(4)	23(4)	14(3)
5151.2(0)	(2)	0	0^{+}	5131.9(8)	1.1(5)	4(3)
5387.3(3)	(4 ⁻)	4351.6(3)	3-	1036.0(3)	3.9(5)	3.9(12)
		4830.5(4)	4-	557.1(4)	0.39(6) ^b	0.39(13) ^b
		4942.4(4)	5-	444.6(4)	0.71(14) ^b	0.7(2) ^b
		4949.0(5)	(3-)	437.2(4)	0.7(2) ^b	0.7(2) ^b
5398.9(5)	(6+)	4715.9(4)	6+	683.0(3)	4.7(7)	2.2(19)
5431.4(7)	(3)	4041.6(3)	2^{+}	1390.3(14)	2.0(7)	4.8(8)
		4351.6(3)	3-	1078.9(7)	$2.4(8)^{a}$	4(2)
		4416.6(3)	4+	1015.4(10)	2.8(7) ^a	1.1(8) ^a
5446.4(5)	(4+)	4416.6(3)	4+	1029.8(4)	4.6(6)	2.9(12)
5478.4(6)	(8+)	4848.3(5)	8+	630.2(3)	3.2(7)	3.2(13)
5628.9(3)	(7^{+})	4715.9(4)	6^+	913.1(3)	1.9(3)	<1ª
		4848.3(5)	8^+ 7+	780.6(3)	$0.79(13)^{\circ}$	$< 0.3^{\circ}$
		4918.8(3) 5398 9(5)	(6^+)	710.1(5)	$0.31(3)^{\circ}$ 0.10(2) ^b	<0.2 ^a
		5478.4(6)	(8^+)	150.3(3)	0.10(2) $0.047(8)^{b}$	< 0.03 ^b
5697 7(3)	(5^{+})	4416 6(3)	4+	1280.7(2)	0.8(3)	2.1(17) ^b
		4715.9(4)	6^{+}	982.2(3)	0.8(4)	$1.3(9)^{a}$
		4885.7(5)	5^{+}	812.4(6)	0.5(4) ^b	0.7(7) ^b
5753.9(4)	(6+)	4715.9(4)	6+	1038.2(3)	$2.0(6)^{a}$	$0.8(7)^{a}$
		5398.9(5)	(6^{+})	354.3(3)	$0.6(2)^{\circ}$	$0.3(2)^{\circ}$

TABLE II. (Continued.)

$\frac{E_i}{(\text{keV})}$	J_i^{Π}	E_f (keV)	J_f^Π	E_{γ} (keV)	$I_{\rm rel}^{\rm c}$ ^{133g} In	$I_{\rm rel}^{\rm d}$ ^{133m} In
5766.2(3)	(5+)	4416.6(3)	4+ 6+	1349.6(3) 1050 3(4)	1.4(10)	$2.3(15)^{a}$
		4885.7(5) 4042.4(4)	5+ 5-	881.7(3)	0.9(4) 0.9(3)	0.40(7) 0.24(6) $0.26(4)^{a}$
5790.4(6)	(4+)	4942.4(4) 4416.6(3)	5 4+	823.2(7) 1373.9(4)	$0.4(2)^{2}$ 2.7(3)	$0.26(4)^{a}$ $3.3(13)^{a}$
6296.6(5)	(5-)	4351.6(3) 4830.5(4)	3- 4-	1438.5(4) 1466.1(3)	0.8(3) 1.9(11) ^a	1.0(6) <0.5 ^a
6476.3(4)	(5 ⁻)	4830.5(4) 4942.4(4)	4- 5-	1645.6(3) 1534.8(5)	1.6(10) ^a 0.3(2) ^b	$<\!\!0.5^{a} \\ <\!\!0.1^{b}$

^aIntensity obtained from γ - γ coincidences.

^bNot observed in this decay, intensity calculated from ¹³²In decay data.

^eRelative γ intensities normalized to 100 units for the 4042-keV transition. For intensity per 100 decays multiply by 0.049(5).

^dRelative γ intensities normalized to 100 units for the 4042-keV transition. For intensity per 100 decays multiply by 0.043(5).

serve transitions having this energy from the decay of the $(1/2^{-})$ isomer, as there are unidentified members of particlehole multiplets in ¹³²Sn, such as $\nu p_{3/2} d_{3/2}^{-1}$, $\pi g_{7/2} g_{9/2}^{-1}$, and $\nu p_{3/2} s_{1/2}^{-1}$, that can give rise to low spin levels. It is very unlikely to populate them in the decay of ¹³²In with (7⁻). However, the feeding of such levels would be strongly favored in the β -*n* decay of the (1/2⁻) state in ^{133m}In. All of this points toward these transitions likely originating from the de-excitation of such p-h multiplet states.

It is worth mentioning that a 5131-keV peak can be seen in both the ^{133g}In and ^{133m}In decays. This γ ray has been firmly identified to belong to ¹³²Sn since its energy perfectly matches the de-excitation of the new 5131-keV level proposed in this work. In addition, the existence of a transition to the 0⁺ g.s.



FIG. 8. β -gated γ -ray spectra from the β decay of ¹³³In isomers highlighting the energy range above 5 MeV. Only the events recorded in the time window from 10 to 600 ms since the arrival of the proton pulse are used.

TABLE III. γ rays observed in the ¹³³In decay that could not be assigned to any specific decay branch. Intensities are given relative to the 4042-keV γ -ray intensity. The label ^{133g}In refers to the ¹³³In (9/2⁺) g.s., with an estimated purity above 95%, while the label ^{133m}In is used for the beam with enhanced content of the (1/2⁻) isomeric state, with a contamination of \approx 30% of ^{133g}In.

$\overline{E_{\gamma}}$ (keV)	$I_{\rm rel}^{a}$ ^{133g} In (9/2 ⁺)	$I_{\rm rel}^{b}$ ^{133m} In (1/2 ⁻)
1116(2)	2.5(4)	4.6(8)
1529.7(7)		2.6(7)
1649.9(4)		7(1)
4110.8(3)	8(1)	8(2)
5439.6(4) ^d		4(2)
5711.6(9) ^e		3.7(12) ^c
5770(1)		3.8(12) ^c
5952.5(6) ^d		6(2) ^c
6018(2)	4.7(9)	6(2) ^c
6067(2)		3.9(13) ^c
6220(2)		2.6(10) ^c
6463(3)		2.0(9) ^c

^aFor I_{abs} multiply by 0.049(5).

^bFor I_{abs} multiply by 0.043(5).

^cIntensity obtained from β -gated spectrum.

^dEnergy compatible with the escape peaks from the tentative 6463keV γ ray.

^eEnergy compatible with the single escape peak from the tentative 6220-keV γ ray.

supports the tentative assignment of this level to the 2^- state of the $v f_{7/2} d_{3/2}^{-1}$ multiplet.

For the sake of completeness, the γ rays observed in the ¹³³In decay that have not been assigned to any decay branch are listed in Table III.

3. β -delayed neutron emission from ¹³³In

We have used the same procedure described above for ¹³²In to determine the β -delayed neutron-emission probabilities from the ¹³³In $(9/2^+)$ ground state and $(1/2^-)$ isomer. The most intense γ rays have been considered in the analysis. For 133 Sn \rightarrow 133 Sb decay, the absolute intensity of 12(2)% for the 962-keV transition was adopted from Ref. [43], while for the 132 Sn \rightarrow 132 Sb an absolute intensity of 48.8(12)% for the 340-keV transition was taken from Ref. [38]. The relative decay activity of the tin daughter nuclei was corrected for the tape movement. In particular, the supercycle structure of the proton beam has to be considered for the evaluation of the unobserved activity. Our analysis yields $P_n = 90(3)\%$ for the decay of the ¹³³In 9/2⁺ g.s., and $P_n = 93(3)\%$ for the decay of the $(1/2^{-})$ isomer. The results differ from those previously reported by us in Ref. [16], which were obtained from the same dataset but where the supercycle structure was not fully taken into account. The re-evaluated results are in agreement with the $P_n = 85(10)\%$ value in Ref. [11].

C. Lifetime measurements

Lifetimes of excited levels in ¹³²Sn have been investigated by means of the advanced time-delayed $\beta \gamma \gamma(t)$ fast-timing



FIG. 9. Time delay spectra between the β and each of the two LaBr₃(Ce) detectors for $\beta \gamma \gamma(t)$ events. These distribution are built by selecting the events when the 526-keV transition in the HPGe detectors and the 375-keV transition in the LaBr₃(Ce) detector. The lifetime is obtained by a χ^2 fit of the whole time distribution to a exponential decay convoluted with a Gaussian function plus a constant background to account for the random background.

method [29–31]. The lifetimes were mainly obtained from the time differences between the fast β and LaBr₃(Ce) detectors. A coincidence condition on the HPGe detectors is applied. The HPGe detectors do not participate in the timing information but are essential in this complex level scheme due to their energy resolution to obtain the required γ -ray selectivity.

The use of two different LaBr₃(Ce) detectors gives us the possibility to obtain two independent measurements for the same lifetime, one per β -LaBr₃(Ce) combination. In addition, $\gamma\gamma(t)$ time differences between the two LaBr₃(Ce) detectors are used when possible. To illustrate the analysis and the results here obtained, we discuss the half-life of the 4416-keV 4⁺ and 4831-keV 4⁻ levels, depicted in Figs. 9 and 10 respectively.

To measure the 4416-keV 4⁺ level half-life using $\beta \gamma \gamma(t)$ events, a time distribution was generated by selecting the 526- and 375-keV transitions in the HPGe and LaBr₃(Ce) detectors respectively. Corrections were included to account for the contribution of Compton background. The 4416-keV 4⁺ state lifetime is free from the influence of other long-lives states and shows up as an exponential tail which can be fitted to measure the half-life. The analysis was done separately for each of the two LaBr₃(Ce) as well as for each of the two available data sets. In the case of $\gamma \gamma(t)$ events, the 299and 375-keV transitions are selected. Here, no extra gate in the HPGe energies is needed, thanks to the large peak to background ratio. The lifetime is measured from time difference distributions with the direct and reversed energy selection on the LaBr₃(Ce) detectors, giving two independent measurements for each of the two data sets. Using the two experimental data sets, our analysis yields eight independent measurements for the half-life, four from $\beta \gamma(t)$ events and another four from $\gamma \gamma(t)$, all of them consistent with each other. The final value is obtained from the weighted average from these measurements, yielding a final value of 3.99(2) ns, which is in good agreement with the 3.95(13) ns reported by Fogelberg et al. [19].



FIG. 10. Time-delayed $\beta\gamma\gamma$ (t) spectra used to measure the lifetime of the 4830-keV 4⁻ excited level. The blue spectra depicts the prompt time distribution used as reference, which is obtained by gating on the 479- and 2380-keV transitions in the HPGe and the LaBr₃(Ce) detectors respectively. The red one corresponds to events obtained after reversing the gates, the 2380-keV one is applied to the HPGe, and the 479-keV one is for the LaBr₃(Ce). The shift measured between the centroid position of each distribution ΔC is caused by the lifetime of the level, but also due the time walk Δ FEP between both energies. The lifetime τ is obtained by subtracting to the centroid shift the contribution due to the FEP time response.

Shorter lifetimes were measured using the centroid shift method. In Fig. 10, the analysis to extract the lifetime of the 4830-keV 4⁻ level is is illustrated for $\beta\gamma\gamma$ (t) events for one of the LaBr₃(Ce) detectors. In this case, the mean life is derived from the centroid shift of the time distribution with respect to a prompt cascade, corrected by the FEP time response calibration.

The analysis has been repeated for both LaBr₃(Ce) detectors and both data sets, and also using the $\gamma \gamma$ (t) method, yielding six independent values for the 4830-keV 4⁻ level mean life. The weighted average of $T_{1/2} = 27(2)$ ps is adopted as the final result. The half-life is in very good agreement with the 26(5) ps reported by Fogelberg *et al.* [19]. It should be noted that the uncertainties in Ref. [18] are too small to be compatible with a fast-timing measurement; the values within brackets in Ref. [19] are actually the errors in ps [44], so the uncertainties from Ref. [19] are adopted.

The lifetime of the 4848-keV 8⁺ level is beyond the fasttiming time range, but it can be investigated using $\beta\gamma$ (t) coincidences between the plastic scintillator and the HPGe detectors. Three β -HPGe(t) time differences spectra were obtained by selecting the 132-, 299- and 375-keV γ rays, respectively. The half-life was measured by fitting the delayed slope of the spectra in a long time range of $\approx 30 \,\mu$ s. The contribution of random coincidences to the time spectra in this range had to be carefully taken into account. Our analysis yields $T_{1/2} = 2.108(14) \,\mu$ s for the 4848-keV level in agreement with the value of 2.080(17) μ s reported in the latest evaluation [3].

The analysis procedures were extended to the other observed levels, provided sufficient statistics were available. The data sets from the two experimental runs have been combined for the analysis. The lifetimes of seven different states were measured. In addition, upper limits for additional seven levels were obtained. The results obtained in this work for level lifetimes in ¹³²Sn are compiled in Tables IV and compared to the previous β -decay studies.

The overall agreement is quite good, with the exception of the 4919-keV 7⁺ level whose half-life is 104(4) ps, much higher than the value of 62(7) ps reported earlier [18], which was measured using BaF₂ scintillator detectors. Since this level can only be measured by analyzing the time distribution of the 203-keV γ -ray, where the contribution of Compton background is very important, the difference may stem from time corrections in this difficult energy range.

The reduced transition probabilities for de-exciting γ transitions in ¹³²Sn have been determined using the measured lifetimes, branching ratios, and energies and using theoretical internal conversion coefficients [37]. The most likely spinparity assignments are employed (see Sec. IV). The transition rates are calculated assuming a pure multipolarity character of the transitions.

IV. DISCUSSION

All new levels in ¹³²Sn observed in this investigation are candidates for the remaining unidentified states within the particle-hole multiplets. In Fig. 11, the energies for the 24 particle-hole multiplets in ¹³²Sn expected to appear below the neutron separation energy are represented. The energies and the splitting of the different levels for the same multiplet are estimated by taking into account the single particle energies from neighboring nuclei, and the analogous particle-hole states in ²⁰⁸Pb, taken from Refs. [19,46,47], where a $A^{-1/3}$ scale is introduced to take into account the nuclear potential depth. These empirical calculations provide guidance for the location of the p-h states, which allows to propose spin-parity assignments to the new levels found in this work.

The other piece of information is provided by the vast number of new transitions which connect the new states to known levels. By assuming that the transitions are predominantly of dipole character (mainly of M1 multipolarity) and using the electromagnetic selection rules, it is possible to make tentative spin-parity assignments of the newly identified levels. The transition rates obtained from the measured lifetimes and lifetime limits of the new levels also provide constraints. Together with the information from the systematics of p-h states, tentative configurations for the new levels are proposed. In the level schemes presented above, the tentative spin and parity assignments are already shown.

A. Low-energy neutron particle-hole states

The unique identification of every observed state in ¹³²Sn with a specific state from a given p-h multiplet is a very complex task. In previous β -decay studies [2,18], the tentative assignment of several states was done by considering the analogies between the ¹³²In $[(\pi g_{9/2})^{-1}\nu f_{7/2}]$ decay and its two neighbors ¹³¹In $[\pi g_{9/2}^{-1}]$ and ¹³³Sn $[\nu f_{7/2}]$ decays. The 6⁻ and 7⁻ levels observed above 7 MeV, attributed to the $\nu f_{7/2}g_{7/2}^{-1}$ configuration, receive the main fraction of

TABLE IV. Half-lives and reduced transition probabilities of the transitions in ¹³²Sn. The $B(X\lambda)$ values have been derived from the lifetimes and branching ratios obtained from ¹³²In decay in this work I, as well as the theoretical internal conversion coefficients, calculated using Bricc [37]. Transition rates have been calculated assuming a pure multipolarity character of the transitions, using the assignments from Ref. [18]. For those levels where no previous assignment had been made, the $B(X\lambda)$ values corresponding to the most likely multipolarities are presented.

$\overline{E_i}$ (keV)	Config _i	J_i^{Π}	$T_{1/2}$	<i>T</i> _{1/2} (literature)	E_f (keV)	Config_f	J_f^Π	E_{γ} (keV)	Xλ	$B(X\lambda)$ (W.u.)
4351.6	Octupole vibration	3-	<5 ps	<5 ps [18] 3.4(⁺²⁰) ps [45] ^b	0 4041.6	g.s. $v f_{7/2} h_{11/2}^{-1}$	$0^+ 2^+$	4351.5 310.5	E3 ^c E1 ^c	>7.1 $>1.2 \times 10^{-4}$
4416.6	$v f_{7/2} h_{11/2}^{-1}$	4+	3.99(2) ns	3.95(13) ns [18]	0 4041.6 4351.6	g.s. $v f_{7/2} h_{11/2}^{-1}$ Octupole vibration	$0^+ 2^+ 3^-$	4416.7 374.9 64.4	E4 E2 ^c E1	$7.7(4) \\ 0.40(2) \\ 2.57(13) \times 10^{-6}$
4715.9	$v f_{7/2} h_{11/2}^{-1}$	6^{+}	21.3(4) ns	20.1(5) ns [18]	4416.6	$v f_{7/2} h_{11/2}^{-1}$	4^{+}	299.3	E2 ^c	0.268(6)
4830.5	$v f_{7/2} d_{3/2}^{-1}$	4-	27(2) ps	26(5) ps [18] ^a	4351.6 4416.6	Octupole vibration $v f_{7/2} h_{11/2}^{-1}$	3- 4+	478.9 414.5	M1° E1	$7.3(5) \times 10^{-3}$ $2.3(3) \times 10^{-6}$
4848.3	$\nu f_{7/2} h_{11/2}^{-1}$	8^+	$2.108(14) \ \mu s$	2.080(17) µs [3]	4715.9	$v f_{7/2} h_{11/2}^{-1}$	6^{+}	132.4	E2 ^c	0.1039(14)
4885.7	$\nu f_{7/2} h_{11/2}^{-1}$	5+	<30 ps	<40 ps [18]	4416.6	$v f_{7/2} h_{11/2}^{-1}$	4+	469.1	M1 E2	$>6.5 \times 10^{-3}$ >19
					4715.9	$ u f_{7/2} h_{11/2}^{-1}$	6+	169.5	M1 E2	$>4.6 \times 10^{-3}$ >94
4918.8	$v f_{7/2} h_{11/2}^{-1}$	7+	104(4) ps	62(7) ps [18] ^a	4715.9 4848.3	$rac{ u f_{7/2} h_{11/2}^{-1}}{ u f_{7/2} h_{11/2}^{-1}}$	${6^+ \over 8^+}$	202.9 70.9	M1 M1	$\begin{array}{c} 1.74(9) \times 10^{-2} \\ 6.0(7) \times 10^{-2} \end{array}$
4942.4	$\nu f_{7/2} d_{3/2}^{-1}$	5-	23(2) ps	17(5) ps [18] ^a	4351.6	Octupole vibration	3-	590.4	E2	0.24(3)
					4416.6	$\nu f_{7/2} h_{11/2}^{-1}$	4+	525.9	E1 ^c	$6.7(7) \times 10^{-5}$
					4715.9	$\nu f_{7/2} h_{11/2}^{-1}$	6+	226.5	E1	$1.7(2) \times 10^{-5}$
					4830.5	$v p_{3/2} h_{11/2}$	4-	111.3	MI	$5.2(7) \times 10^{-2}$
5387.3	$(\nu f_{7/2} s_{1/2}^{-1})$	(4 ⁻)	<17 ps		4351.6	Octupole vibration	3-	1036.0	M1	$>0.8 \times 10^{-3}$
					4830.5	$\nu f_{7/2} d_{3/2}^{-1}$	4-	557.1	E2 M1 F2	>0.5 >4.5 × 10 ⁻⁴ >0.9
					4942.4	$\nu f_{7/2} d_{3/2}^{-1}$	5-	444.6	M1 E2	$>1.5 \times 10^{-3}$ >5.1
					4949.0	$v f_{7/2} d_{3/2}^{-1}$	(3-)	437.2	M1 E2	$>1.7 \times 10^{-3}$ >5.6
5398.9	$(\pi g_{7/2} g_{9/2}^{-1})$	(6+)	<17 ps		4715.9	$ u f_{7/2} h_{11/2}^{-1}$	6+	683.0	M1 E2	$>4.0 \times 10^{-3}$ >5.6
5478.4	$(\pi g_{7/2} g_{9/2}^{-1})$	(8+)	<14 ps		4848.3	$ u f_{7/2} h_{11/2}^{-1}$	8+	630.2	M1 E2	$>6.4 \times 10^{-3}$ >10
5628.9	$(\pi g_{7/2} g_{9/2}^{-1})$	(7+)	9(3) ps	13(4) ps [18] ^a	4715.9	$ \nu f_{7/2} h_{11/2}^{-1}$	6+	913.1	M1 E2	$2.0(^{+9}_{-5}) \times 10^{-3}$ $1.5(^{+7}_{-4})$
					4848.3	$\nu f_{7/2} h_{11/2}^{-1}$	8^+	780.6	M1	$1.3(^{+6}_{-3}) \times 10^{-3}$
					4918.8	$\nu f_{7/2} h_{11/2}^{-1}$	7+	710.1	E2 M1 F2	1.4(-3) $7(+3) \times 10^{-4}$ 0.9(+4)
					5398.9	$(\pi g_{7/2} g_{9/2}^{-1})$	(6+)	229.8	M1 E2	$6(^{+3}_{-2}) \times 10^{-3}$ $76(^{+34}_{-10})$
					5478.4	$(\pi g_{7/2}g_{9/2}^{-1})$	(8+)	150.3	M1 E2	$9(^{+4}_{-2}) \times 10^{-3} \\ 215(^{+95}_{-54})$
5753.9	$(vp_{3/2}h_{11/2}^{-1})$	(6+)	<20 ps		4715.9	$\nu f_{7/2} h_{11/2}^{-1}$	6+	1038.2	M1 E2	$>7.1 \times 10^{-4}$ >0.4
					5398.9	$(\pi g_{7/2} g_{9/2}^{-1})$	(6+)	354.3	M1 E2	$>5.5 \times 10^{-3}$ >28
6235.5		(7+)	<10 ps		4715.9	$ u f_{7/2} h_{11/2}^{-1}$	6+	1519.6	M1 E2	$>1.6 \times 10^{-4}$ >0.04

	IABLE IV. (Continuea.)									
E _i (keV)	Config _i	J_i^Π	<i>T</i> _{1/2}	<i>T</i> _{1/2} (literature)	E_f (keV)	Config_f	J_f^{Π}	E_{γ} (keV)	Χλ	<i>B</i> (<i>X</i> λ) (W.u.)
					4918.8	$\nu f_{7/2} h_{11/2}^{-1}$	7+	1317.1	M1 E2	$>1.4 \times 10^{-4}$ >0.05
					5398.9	$(\pi g_{7/2} g_{9/2}^{-1})$	(6+)	836.3	M1 E2	$>1.1 \times 10^{-3}$ >1.0
					5753.9	$(vp_{3/2}h_{11/2}^{-1})$	(6+)	481.8	M1 E2	$>4.8 \times 10^{-3}$ >13
6709.7		(7-)	<13 ps		4918.8	$\nu f_{7/2} h_{11/2}^{-1}$	7+ 5-	1791.0	E1	$>3.6 \times 10^{-7}$
					4942.4	$v f_{7/2} d_{3/2}$	5-	1/6/.2	E2	$>6 \times 10^{-2}$

^aThe uncertainties are taken from Ref. [19] since those in Ref. [18] contain several typographical errors [44].

^bCalculated from the B(E3) rate measured in Coulomb excitation [45].

^cAssigned multipolarity in Ref. [18].

the total β -feeding intensity. This strong transition would be equivalent to the Gamow-Teller transition in the ¹³¹In decay $\pi g_{9/2}^{-1} \rightarrow \nu g_{7/2}^{-1}$ [48]. If we keep the ¹³¹In decay analogy, the second strongest decay branch corresponds to the first-forbidden transition $\pi g_{9/2}^{-1} \rightarrow \nu h_{11/2}^{-1}$. In the ¹³²In decay, the equivalent transition would populate the $\nu f_{7/2} h_{11/2}^{-1}$ multiplet. Consequently, the positive-parity states that appear below 5 MeV are suggested to be members of this configuration. On the other hand, the strong 2435-keV γ transition in ¹³¹Sn that connects the single hole states $\nu g_{7/2}^{-1} \rightarrow \nu d_{3/2}^{-1}$ would be analogous to the 2380- and 2268-keV transitions in ¹³²Sn, which indicates that the 4⁻ and 5⁻ found below 5 MeV are indeed members of the $v f_{7/2} d_{3/2}^{-1}$ p-h multiplet.

In this way, there are two neutron p-h multiplets identified within this energy range. However, several of the expected levels from those configurations lack experimental identification. Specifically, the 3⁺ and 8⁺ levels from the $v f_{7/2} h_{11/2}^{-1}$ coupling, as well as the 2⁻ and 3⁻ levels from the $\nu f_{7/2} d_{3/2}^{-1}$ multiplet, which are expected to be found at excitation energies around 5 MeV, remain unseen. In a previous investigation from the ²⁴⁸Cm spontaneous fission [24], a level at 5280 keV was suggested to be the missing $v f_{7/2} h_{11/2}^{-1} 8^+$ level. On the contrary, in our work we observe the population of this level in the ¹³²In decay, which de-excites by a γ ray to the 4848-keV state. This level has a very large apparent $\log ft$ value, around 7.2, as it would be expected for a high spin such as 9^+ , which suggests its identification as the missing 9^+ level.

The remaining three levels found within that energy range are the 4949-, 4965- and 5131-keV states. They are directly populated in the β -n decay of 133g,m In, but not directly fed from the ¹³²In (7⁻) decay. The 4949-keV level is observed in the ¹³²In decay, but indirectly populated by a γ transition from the 5387 keV (4-) level without any noticeable direct β feeding. The β -n feeding from the $(1/2^{-})$ and $(9/2^{+})$ ¹³³In states points toward a low spin value for these three levels. Specifically, the 5131-keV state is populated more favorably in the β -n decay of the $(1/2^{-})$ isomer, which, along with the γ transition which connects that level with the g.s., suggests a lower spin for that level than for the other ones. This is an indication that the 5131-keV state is very likely the 2⁻ member of the $\nu f_{7/2} d_{3/2}^{-1}$ multiplet. The systematics

of the transitions that de-excite the 4949- and 4965-keV levels suggests angular momenta J = 3. Therefore one of them would correspond to the 3⁺ state from $\nu f_{7/2} h_{11/2}^{-1}$ and the other matches the 3⁻ from $\nu f_{7/2} p_{3/2}^{-1}$. There is no direct information to determine their parity, since both of them are linked to positive- and negative-parity levels. However, there are analogies between the 4949-keV and the 5⁻ 4942-keV levels. First, both are being populated from the 5387-keV state, interpreted as $\nu f_{7/2} s_{1/2}^{-1}$ (4⁻), with similar intensities. Second, both levels have a transition to the 4352-keV 3⁻ collective state and another one to the $\nu f_{7/2}d_{3/2}^{-1}$ 4⁻ level whose intensity ratio is about 10:1 in both cases. Those similarities strongly suggest that 4949-keV level is indeed the 3⁻ member from the $\nu f_{7/2} d_{3/2}^{-1}$ multiplet, and therefore the 4965 keV can only be the 3⁺ member of the $v f_{7/2} h_{11/2}^{-1}$ p-h configuration.

The new assignments are shown in Fig. 11.

B. Particle-hole states from 5 to 6 MeV

In the investigation by Fogelberg et al. [18,19], the 5399-keV (6⁺), 5478-keV (8⁺), and 5629-keV (7⁺) levels were identified as members of the proton p-h $\pi g_{7/2}g_{9/2}^{-1}$ multiplet. This assignment was supported by the intense feeding of the 5629 keV (7^+) state, which would be the equivalent to the strongest transition in the ¹³³Sn decay, $\nu f_{7/2} \rightarrow \pi g_{7/2}$. Within this region, we have found seven new levels with expected angular momenta from 4 to 8. In addition to the proton $\pi g_{7/2} g_{9/2}^{-1}$ p-h levels, states from the neutron $\nu p_{3/2} h_{11/2}^{-1}$ and $\nu f_{7/2} s_{1/2}^{-1}$ configurations are also expected. All the levels found from 5.3 to 6 MeV could be related to p-h levels from those multiplets. There is not much information apart from γ -ray intensities and the lifetimes and lifetime limits that point toward dominant M1 transitions. This, together with the possibility that the configurations are mixed, hinders a clearer assignment. Nevertheless, several conclusions about them can be drawn.

For the 5431-keV level, observed only in the ¹³³In decay, a J = 3 spin assignment can be assumed based on the γ transition systematics. Thus, this level can be either identified with the 3^+ state of the $\pi g_{7/2} g_{9/2}^{-1}$ or with the 3^- of the $v f_{7/2} s_{1/2}^{-1}$ configuration.



FIG. 11. Calculated energies for the different particle-hole multiplet states in ¹³²Sn, adopted from the work of J. Blomqvist [46,47]. The energies and energy splitting within a given multiplet are estimated by scaling the analogous particle-hole states in ²⁰⁸Pb and taking into account single-particle energies from neighboring nuclei. Previously identified levels are plotted with continuous lines. The experimental energies from our work are shown for the newly identified states. The levels whose energies appear between brackets correspond to tentative assignments.

At similar excitation, we expect two 4⁺ states belonging to the two positive-parity multiplets mentioned above. In our analysis, two levels have been found within this energy range with a tentative angular momenta J = 4. There is a level at 5446 keV (4⁺), populated indirectly by γ transitions in ¹³²In and directly in the β -*n* decay of ^{133g,m}In. This level is a good candidate to be a member of the proton $\pi g_{7/2}g_{9/2}^{-1}$ multiplet, but it can also be interpreted as the 4⁺ level from the neutron $\nu p_{3/2}h_{11/2}^{-1}$ configuration. At 5790 keV, another level was identified; this one can be only observed in the ¹³³In β -*n* decay, and its de-exciting transitions point toward a spin of (3,4). Therefore, this level can be identified either as the 4⁺ from the $\nu p_{3/2}h_{11/2}^{-1}$ particle-hole coupling expected in this region, or the 3⁺ from $\pi g_{7/2}g_{9/2}^{-1}$.

The (5⁺) levels at 5698 and 5766 keV, which are observed in this work in both the ¹³²In and ¹³³In decays, can be related to the 5⁺ states from the $\pi g_{7/2}g_{9/2}^{-1}$ and the $\nu p_{3/2}h_{11/2}^{-1}$ multiplets. The two remaining levels in this region are the 5754-keV (6⁺) and the 6008-keV (7⁺) ones, which we tentatively suggest as members of the $\nu p_{3/2}h_{11/2}^{-1}$ particle-hole configuration.

These tentative assignments are reflected in Fig. 11.

C. States from 6 to 7 MeV

Moving up to the next energy interval, the identification becomes even more complicated, due to all the possible ph multiplets that are expected in this region, and the likely admixture of configurations. Nevertheless, since most of these levels are populated only in the direct β decay of ¹³²In, they are constrained by the selective nature of β decay that favors, in this case, states with a large spin (6–8). Because there are not so many p-h multiplets at this energy that could give rise to levels with such a large spin (Fig. 11), we can draw some conclusions about them.

Regarding the negative-parity states, there are two highlying levels with most likely (6⁻) assignments observed only in the ¹³²In decay, at 6598 and 6709 keV. Only two neutron multiplets, the $vh_{9/2}d_{3/2}^{-1}$ and $vf_{7/2}d_{5/2}^{-1}$, have a negative-parity member with J = 6, and therefore these two levels can only be related to those. The remaining two negative-parity levels appearing at 6297 and 6476 keV are present in both the ¹³²In and ¹³³In β decays. The systematics of the transitions that de-excite and populate them suggest a (5⁻) spin parity and therefore they are likely to be members of the $vh_{9/2}d_{3/2}^{-1}$ and $vf_{7/2}d_{5/2}^{-1}$ multiplets as well.

On the positive-parity side, the situation is more involved due to the larger amount of multiplets predicted at these high energies. There are eight different states with an assumed positive parity. These were only observed in the direct β decay of ¹³²In, out of which five have been identified in this work for the first time. Relying on the systematics of the transitions between these levels, along with the selectivity of the β -decay population from the (7⁻) g.s. in ¹³²In, they can have angular momenta from 5 to 8. Four different positive parity p-h multiplets are predicted in this energy range, three of them expected to arise from neutron configurations $(\nu h_{9/2} h_{11/2}^{-1}, \nu f_{5/2} h_{11/2}^{-1})$, and $\nu p_{3/2} h_{11/2}^{-1}$, and nother one coming from the proton $\pi d_{5/2} g_{9/2}^{-1}$ coupling. Almost all of them can be give rise to $(5,6,8)^+$ states, which hampers their identification. Moreover, the states are probably mixed.

The only noticeable difference observed among the positive-parity levels is the larger feeding measured for the 6631-keV state, around 1% with a $\log ft$ of the order of 6.4 (Fig. 5). This enhanced population can be interpreted on the grounds of the equivalence mentioned before between the ¹³²In and ¹³³Sn decays. In ¹³³Sn, the β decay is dominated by the first forbidden $\nu f_{7/2} \rightarrow \pi g_{7/2}$ transition populating the g.s. in ¹³³Sb with 86% of the total β intensity and $\log ft \approx 5.5$ [49], which is similar to the population of the $\pi g_{7/2}g_{9/2}^{-1}$ multiplet in the ¹³²In decay. Moreover, the second strongest transition found in ¹³³Sn decay corresponds to the $v f_{7/2} \rightarrow \pi d_{5/2}$ transition, receiving 11% of the total feeding with $\log ft \approx 6.1$ [49]. This transition would be equivalent to the population of the proton $\pi d_{5/2} g_{9/2}^{-1}$ configuration in the ¹³²In β decay. Comparing the population of the 6631-keV level with the population of 5629-keV level, identified as the (7^+) state of the $\pi g_{7/2} g_{9/2}^{-1}$ multiplet, we can see that they keep the 8:1 β intensity ratio, and similar log ft values for the level at 5629 keV. Such a large population might be an indication of a predominant $\pi d_{5/2} g_{9/2}^{-1}$ configuration for the 6631-keV (6⁺) state.

V. CONCLUSIONS

Experimental information about the ¹³²Sn structure plays a crucial role in the shell-model interpretation of nuclei around N = 82, because it provides direct knowledge about the particle-hole couplings for both protons and neutrons. In this work, the properties of excited states in ¹³²Sn have been studied from the β decay of ¹³²In. By taking advantage of the isomer selectivity capabilities of the ISOLDE RILIS, independent investigations of the β decay of the ^{133g} In (9/2⁺) g.s. and the 133m In $(1/2^{-})$ isomer were performed as well. Thanks to both decay modes, the knowledge of the ¹³²Sn structure has been largely expanded in this work. A total of 17 new levels and 68 new γ -transitions have been added (including those already quoted in the previous publication [16] derived from the same experiment). A complete fast-timing investigation of the excited levels in ¹³²Sn has been performed as well, confirming and extending previous results.

An interpretation of the level structure is provided in terms of particle-hole configurations arising from core breaking states both from the N = 82 and Z = 50 shells across the gap. The interpretation is based on empirical calculations [19,46,47] leading to positive- and negative-parity particle-

hole multiplets, where the energies are obtained from the single-particle energies from neighboring nuclei and from the analogous particle-hole states in ²⁰⁸Pb. These empirical calculations, together with the experimental information on the β and β -*n* feeding, the level lifetimes, and the γ -decay branches provide guidance for the identification of the levels as proton-hole members of the multiplets, facilitating tentative spin-parity assignments to the new levels.

The number of states is consistent with the one calculated from the angular momentum couplings. The identification of all remaining missing levels from the $v f_{7/2} h_{11/2}^{-1}$ and $v f_{7/2} d_{3/2}^{-1}$ neutron-hole configurations has been completed. A tentative interpretation has been provided for the rest of observed states, where we have been able to observe most of the expected p-h levels with angular momenta close to 7.

Most of the missing information is related to the anticipated low-spin states, which are very unlikely to be populated in the ¹³²In (7⁻) β decay. However, the identification of many γ rays around 7 MeV from the ^{133g,m}In β decay strongly suggests feeding of those missing low-spin multiplet states. Enhanced statistics for this decay will be beneficial to provide more firm assignments.

In conclusion, the knowledge about states in the doubly magic 132 Sn has been largely expanded by the investigation of the β decay of 132 In and β -*n* decay of 133 In performed at the ISOLDE facility at CERN. The identification of particle-hole multiplets both for protons and neutrons and the transition rates connecting different p-h configurations and states within multiplets may provide input on the two-body matrix elements and single-particle states. The new data challenge the theoretical description of 132 Sn, which is relevant for the understanding of nuclear structure in the region.

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