



CHORUS

This is the accepted manuscript made available via CHORUS. The article has been published as:

Toward establishing low-lying Λ and Σ hyperon resonances with the $K[\overline{}] + d \rightarrow \pi + Y + N$ reaction

H. Kamano and T.-S. H. Lee

Phys. Rev. C **94**, 065205 — Published 21 December 2016

DOI: [10.1103/PhysRevC.94.065205](https://doi.org/10.1103/PhysRevC.94.065205)

1 **Towards establishing low-lying Λ and Σ hyperon resonances with**
2 **$\bar{K} + d \rightarrow \pi + Y + N$ reaction**

3 H. Kamano^{1,2} and T.-S. H. Lee³

4 ¹*KEK Theory Center, Institute of Particle and Nuclear Studies (IPNS),*
5 *High Energy Accelerator Research Organization (KEK), Tsukuba, Ibaraki 305-0801, Japan*

6 ²*J-PARC Branch, KEK Theory Center,*
7 *IPNS, KEK, Tokai, Ibaraki 319-1106, Japan*

8 ³*Physics Division, Argonne National Laboratory, Argonne, Illinois 60439, USA*

9 **Abstract**

10 A model for the $\bar{K}d \rightarrow \pi Y N$ reactions with $Y = \Lambda, \Sigma$ is developed, aiming at establishing the
11 low-lying Λ and Σ hyperon resonances through analyzing the forthcoming data from the J-PARC
12 E31 experiment. The off-shell amplitudes generated from the dynamical coupled-channels (DCC)
13 model, which was developed in Phys. Rev. C **90**, 065204 (2014), are used as input to the calculations
14 of the elementary $\bar{K}N \rightarrow \bar{K}N$ and $\bar{K}N \rightarrow \pi Y$ subprocesses in the $\bar{K}d \rightarrow \pi Y N$ reactions. It is
15 shown that the cross sections for the J-PARC E31 experiment with a rather high incoming- \bar{K}
16 momentum, $|\vec{p}_{\bar{K}}| = 1$ GeV, can be predicted reliably only when the input $\bar{K}N \rightarrow \bar{K}N$ amplitudes
17 are generated from a $\bar{K}N$ model, such as the DCC model used in this investigation, which describes
18 the data of the $\bar{K}N$ reactions at energies far beyond the $\bar{K}N$ threshold. We find that the data
19 of the threefold differential cross section $d\sigma/(dM_{\pi\Sigma}d\Omega_{p_n})$ for the $K^-d \rightarrow \pi\Sigma n$ reaction below the
20 $\bar{K}N$ threshold can be used to test the predictions of the resonance poles associated with $\Lambda(1405)$.
21 We also find that the momentum dependence of the threefold differential cross sections for the
22 $K^-d \rightarrow \pi^- \Lambda p$ reaction can be used to examine the existence of a low-lying $J^P = 1/2^+$ Σ resonance
23 with a pole mass $M_R = 1457 - i39$ MeV, which was found from analyzing the K^-p reaction data
24 within the employed DCC model.

25 PACS numbers: 14.20.Jn, 13.75.Jz, 13.60.Le, 13.30.Eg

26 **I. INTRODUCTION**

27 Recently, the spectroscopic study of Λ and Σ hyperon resonances with strangeness $S =$
 28 -1 (collectively referred to as Y^*) has made significant progress. This advance mainly
 29 comes from using sophisticated coupled-channels approaches [1–4] to perform comprehen-
 30 sive partial-wave analyses of the existing data of K^-p reactions in a wide energy region from
 31 their thresholds to a rather high energy with the invariant mass $W = 2.1$ GeV. With this
 32 analysis, the systematic extraction of Y^* resonances defined by poles of the scattering am-
 33 plitudes in the complex-energy plane was accomplished. It has been established [5] that the
 34 resonance poles can be identified with the (complex-)energy eigenstates of the Hamiltonian
 35 of the underlying fundamental theory, which are obtained under the purely outgoing wave
 36 boundary condition. Thus the Y^* resonance parameters extracted through the coupled-
 37 channels analyses of Refs. [1–4] have well defined theoretical meaning, while it is often not
 38 straightforward to interpret the Breit-Wigner parameters listed by Particle Data Group
 39 (PDG) [6]. In addition, attempts [7–9] are being made to develop methods for relating the
 40 meson and baryon resonance poles to the Lattice QCD calculations.

41 In this work, we consider the dynamical coupled-channels (DCC) model developed in
 42 Ref. [2] for the meson-baryon reactions in the $S = -1$ sector. This model was developed by
 43 extending the theoretical framework of Ref. [10], which was originally formulated to study
 44 πN , γN , eN , and νN reactions in the nucleon resonance region [11–24], to include the
 45 meson-baryon channels with strangeness $S = -1$. Within this DCC model, the T -matrix
 46 elements for each partial wave can be obtained by solving the following coupled integral
 47 equation [2]:

$$T_{\beta,\alpha}(p_\beta, p_\alpha; W) = V_{\beta,\alpha}(p_\beta, p_\alpha; W) + \sum_{\delta} \int p^2 dp V_{\beta,\delta}(p_\beta, p; W) G_{\delta}(p; W) T_{\delta,\alpha}(p, p_\alpha; W), \quad (1)$$

48 with

$$V_{\beta,\alpha}(p_\beta, p_\alpha; W) = v_{\beta,\alpha}(p_\beta, p_\alpha) + \sum_{Y_{0,n}^*} \frac{\Gamma_{Y_{0,n}^*,\beta}^\dagger(p_\beta) \Gamma_{Y_{0,n}^*,\alpha}(p_\alpha)}{W - M_{Y_{0,n}^*}}, \quad (2)$$

49 where W is the invariant mass of the reaction; the subscripts α , β , and δ represent the
 50 four two-body channels ($\bar{K}N$, $\pi\Sigma$, $\pi\Lambda$, $\eta\Lambda$, and $K\Xi$) and the two quasi-two-body channels
 51 ($\pi\Sigma^*$ and \bar{K}^*N) that can decay into the three-body $\pi\pi\Lambda$ and $\pi\bar{K}N$ channels, respectively;
 52 p_α is the magnitude of the momentum of channel α in the center-of-mass (CM) frame; G_{δ}
 53 is the Green's function of channel δ ; $M_{Y_{0,n}^*}$ is the mass of the n th bare excited hyperon
 54 state $Y_{0,n}^*$ included in the given partial wave; $v_{\beta,\alpha}$ represents the hadron-exchange potentials
 55 derived from the effective Lagrangian that respects the SU(3) flavor symmetry; and the bare
 56 vertex interaction $\Gamma_{Y_{0,n}^*,\alpha}$ ($\Gamma_{Y_{0,n}^*,\beta}^\dagger$) defines the $\alpha \rightarrow Y_{0,n}^*$ ($Y_{0,n}^* \rightarrow \beta$) transition. The model
 57 parameters contained in the potential $V_{\beta,\alpha}$ were fixed by fitting more than 17,000 data of
 58 both unpolarized and polarized observables of the $K^-p \rightarrow \bar{K}N, \pi\Sigma, \pi\Lambda, \eta\Lambda, K\Xi$ reactions.
 59 As a result, we obtained two distinct sets of the model parameters, referred to as Model
 60 A and Model B. Both models describe the existing K^-p reaction data equally well over a
 61 wide energy range from the thresholds up to $W = 2.1$ GeV. From Model A (Model B),
 62 18 (20) of Y^* resonances were extracted in the energy region above the $\bar{K}N$ threshold and
 63 below $W = 2.1$ GeV. It is found that some of the extracted low-lying Y^* resonances may
 64 correspond to one- and/or two-star resonances assigned by Particle Data Group [6] or may

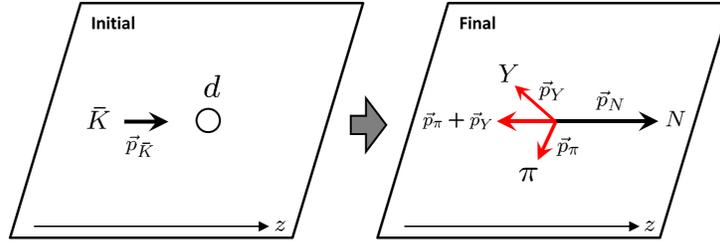


FIG. 1. Kinematics of the $\bar{K}d \rightarrow \pi Y N$ reaction considered in this work. The outgoing N (outgoing πY -pair) momentum is in the direction (opposite direction) of the incoming- \bar{K} momentum.

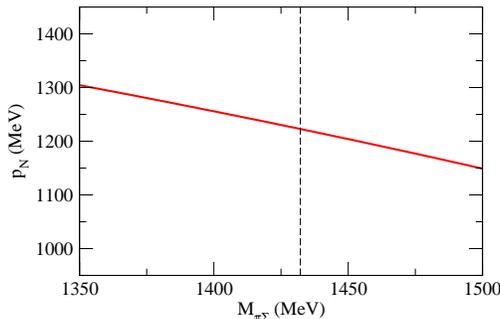


FIG. 2. The outgoing nucleon momentum $p_N \equiv |\vec{p}_N|$ (solid line) as function of the kinematically allowed πY invariant mass $M_{\pi Y}$ for the incoming- \bar{K} momentum $|\vec{p}_{\bar{K}}| = 1$ GeV. Here the case that $Y = \Sigma$ is presented.

65 be new resonances. Furthermore, two $J^P = 1/2^-$ Λ resonances are found below the $\bar{K}N$
 66 threshold in both Model A and Model B, which is similar to the results from the chiral
 67 unitary models (see, e.g., Refs. [25, 26]) and the Jülich model [27].

68 Although a number of new and/or unestablished low-lying Y^* resonances were found in
 69 the DCC analysis of Refs. [2, 3], their existence and pole-mass values are rather different
 70 between Model A and Model B. This is of course due to the fact that the existing K^-p
 71 reaction data used in the analysis are *incomplete*, as discussed in Refs. [2, 3]. In addition,
 72 there is a limitation of using the K^-p reaction data for establishing low-lying Y^* resonances
 73 because the K^-p reactions cannot directly access the energy region below the $\bar{K}N$ threshold,
 74 and also it is practically not easy to measure precisely the K^-p reactions in the energy region
 75 just above the $\bar{K}N$ threshold where the incoming- \bar{K} momentum becomes very low. One of
 76 the most promising approaches to overcome this limitation would be a combined analysis of
 77 the K^-p reactions and the $K^-d \rightarrow \pi Y N$ reactions. This is based on the observation that
 78 the two-body πY subsystem in the final state of the $K^-d \rightarrow \pi Y N$ reactions can be in the
 79 energy region below the $\bar{K}N$ threshold even if the incoming- \bar{K} momentum is rather high.

80 As a first step towards accomplishing such a combined analysis of the $\bar{K}N$ and $\bar{K}d$ reac-
 81 tions, in this work we apply the multiple scattering theory [28, 29] to predict the differential
 82 cross sections of the $\bar{K}d \rightarrow \pi Y N$ reaction by using the $\bar{K}N$ reaction amplitudes generated
 83 from the DCC model of Ref. [2]. We focus on the kinematics that the incoming \bar{K} has a
 84 rather high momentum of $|\vec{p}_{\bar{K}}| = 1$ GeV and the outgoing nucleon N is detected at very
 85 forward angles with $\theta_{p_N} \sim 0$, which is the same as the setup of the J-PARC E31 experi-
 86 ment [30]. At this special parallel kinematics, the outgoing N and the outgoing πY pair are

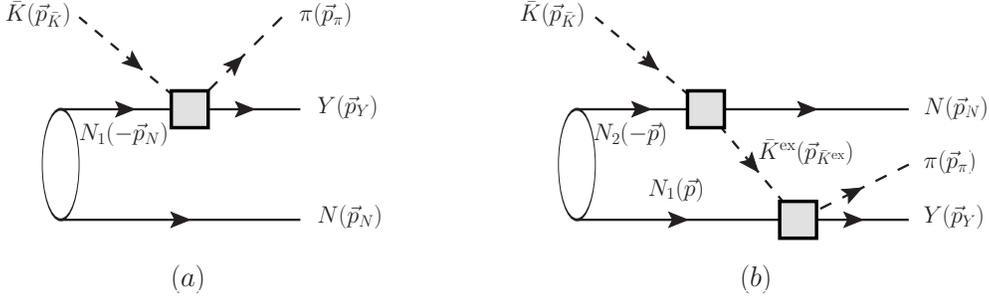


FIG. 3. Diagrammatical representation of the $\bar{K}d \rightarrow \pi Y N$ reaction processes considered in this work: (a) the impulse process; (b) the \bar{K} -exchange process. The deuteron wave function (open circles) is taken from the one constructed with the Argonne V18 potential [35], while the off-shell amplitudes describing the meson-baryon subprocesses (filled squares) are taken from our DCC model developed in Ref. [2].

87 scattered back-to-back, as illustrated in Fig. 1, and have almost no correlation in experimen-
 88 tal measurements. In fact, as can be seen from Fig. 2, the forward moving nucleon momenta
 89 (solid curve) become $|\vec{p}_N| > |\vec{p}_K| = 1$ GeV for the invariant mass of the πY subsystem
 90 relevant to our study (horizontal axis), which means that the momentum of the πY pair is
 91 in an opposite direction to \vec{p}_N . Consequently, it is the best for examining Y^* resonances
 92 through their decays into πY states. In addition, since the forward moving nucleon carries
 93 high energy-momentum, the recoiled πY pair can be even below the $\bar{K}N$ threshold, which
 94 is also illustrated in Fig. 2. We thus can make predictions for investigating low-lying Y^*
 95 resonances, including the long-standing problem associated with $\Lambda(1405)$ that was also the
 96 focus of Refs. [31–34]. The data from the J-PARC E31 experiment [30] can then be used
 97 to test our results. In particular, we would like to examine how the predicted cross sections
 98 can be used to distinguish the resonance parameters extracted within Model A and Model
 99 B employed in our calculations.

100 Following the previous works [31–33] and justified by the special kinematics mentioned
 101 above, we assume that the scattering amplitude for $\bar{K}d \rightarrow \pi Y N$ includes the single-
 102 scattering (impulse) term and the \bar{K} -exchange term, as illustrated in Fig. 3. While such
 103 a perturbative approach neglects the higher-order scattering processes in a recent calcula-
 104 tion [34] based on the AGS-type of three-body scattering formulation [36], it is supported by
 105 many earlier studies of intermediate and high energy reactions on deuteron; see, for example,
 106 a recent study of $\gamma d \rightarrow \pi N N$ of Ref. [37]. Thus it is reasonable to assume that our results as
 107 well as the results of Refs. [31–33] account for the main features of the $\bar{K}d \rightarrow \pi Y N$ reaction
 108 and can be used to explore the feasibility of using the experiment at J-PARC to investigate
 109 the low-lying hyperon resonances.

110 An essential difference between this work and the previous works [31–34] is that we
 111 employ the (off-shell) $\bar{K}N$ reaction amplitudes generated from the DCC model developed
 112 in Ref. [2]. This DCC model describes the $\bar{K}N$ reaction data over a very wide energy range
 113 from the thresholds up to $W = 2.1$ GeV. On the other hand, the models for the meson-
 114 baryon subprocesses employed in Refs. [31–34] were constructed by fitting only the K^-p
 115 reaction data just near the $\bar{K}N$ threshold. To see how these $\bar{K}N$ models can be used in the
 116 calculations, it is instructive here to examine the kinematics of the \bar{K} -exchange mechanism
 117 illustrated in Fig. 3(b). The range of the invariant mass of the outgoing πY system ($M_{\pi Y}$)
 118 we are interested in is $m_\pi + m_Y \leq M_{\pi Y} \lesssim 1.5$ GeV, where m_π (m_Y) is the mass of π

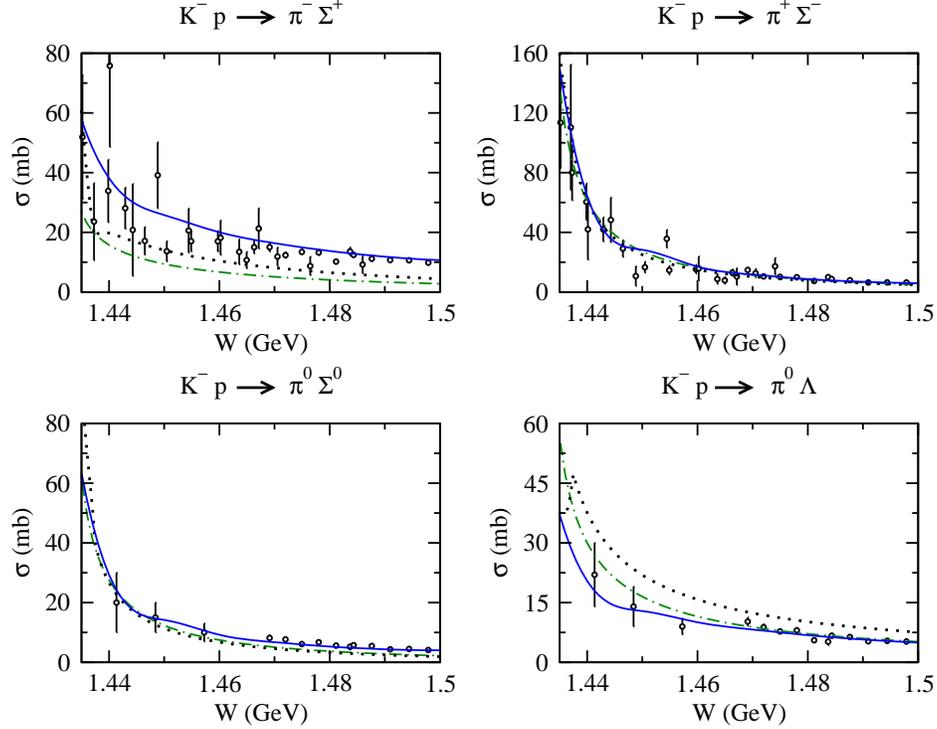


FIG. 4. Total cross sections for $K^- p \rightarrow \pi Y$ reactions near the threshold. Blue solid curves are Model B in Ref. [2], green dotted-dashed curves are the E-dep. model in Ref. [34], and black dotted curves are from the model developed in Ref. [38] that was used for the calculation in Refs. [31–33].

119 (Y). Thus the $\bar{K}^{\text{ex}} N_1 \rightarrow \pi Y$ amplitudes used for calculating the \bar{K} -exchange mechanism
 120 must be generated from models which can reproduce well the data near the $\bar{K}N$ threshold.
 121 As seen in Fig. 4, the models used in Refs. [31, 32, 34] and the DCC models employed in
 122 our calculations are all valid for this calculation in the invariant mass $M_{\pi Y}$ covered by the
 123 J-PARC E31 experiment shown in Fig. 2.

124 The situation is very different for the calculations of $\bar{K}N_2 \rightarrow \bar{K}^{\text{ex}}N$ amplitudes in
 125 Fig. 3(b). In the lower panel of Fig. 5, we show the ranges of the invariant mass ($W_{1\text{st}}^{\text{ex}}$)
 126 of the $\bar{K}N_2 \rightarrow \bar{K}^{\text{ex}}N$ subprocess, which can be formed from the incoming- \bar{K} momentum
 127 $|\vec{p}_K| = 1$ GeV, the scattering angle of outgoing- N $\theta_{p_N} = 0$, and the momentum of initial
 128 nucleon N_2 with $|\vec{p}| < 0.2$ GeV within which the deuteron wave function is large. We see
 129 that for a rather high incoming- \bar{K} momentum with $|\vec{p}_K| = 1$ GeV, the allowed ranges for
 130 $W_{1\text{st}}^{\text{ex}}$ are in the well above the $\bar{K}N$ threshold region. In the upper panel of Fig. 5, we see
 131 that only the DCC model can describe the data in the whole range. Thus the models used
 132 in Refs. [31, 32, 34] have large uncertainties in calculating the $\bar{K}N_2 \rightarrow \bar{K}^{\text{ex}}N$ amplitudes for
 133 predicting $\bar{K}d \rightarrow \pi Y N$ at $|\vec{p}_K| = 1$ GeV to compare with the data from the J-PARC E31
 134 experiment [30]. In this work, we will also discuss how these uncertainties associated with
 135 the $\bar{K}N_2 \rightarrow \bar{K}^{\text{ex}}N$ amplitudes affect the resulting $\bar{K}d \rightarrow \pi Y N$ reactions cross sections.

136 In Sec. II, we first give the notations for kinematical variables and the cross section
 137 formulas necessary for the presentation of this work. We then give the formula for calculating
 138 the impulse and \bar{K} -exchange amplitudes of the $\bar{K}d \rightarrow \pi Y N$ reactions. The predicted results
 139 for the $\bar{K}d \rightarrow \pi Y N$ reaction from our model are presented in Sec. III. The comparisons
 140 with the results from using the S-wave $\bar{K}N$ models are also given there. A summary and

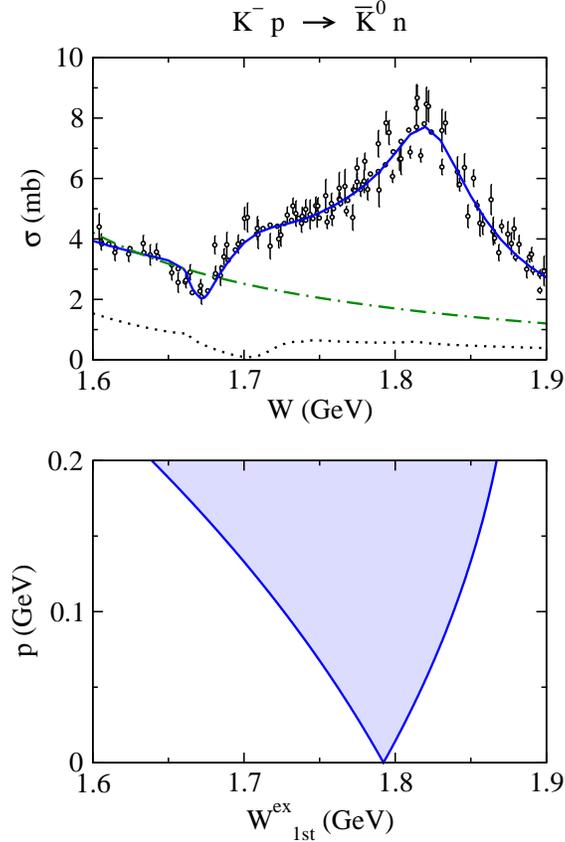


FIG. 5. Upper panel: Total cross section for $K^-p \rightarrow \bar{K}^0n$ in the energy region relevant to the $\bar{K}N_2 \rightarrow \bar{K}^{\text{ex}}N$ subprocess in the \bar{K} -exchange process [Fig. 3(b)]. Blue solid curve is Model B in Ref. [2], green dotted-dashed curve is the E-dep. model in Ref. [34], and black dotted curves is from the model developed in Ref. [38] that was used for the calculation in Refs. [31–33]. Lower panel: Allowed ranges of the invariant mass $W_{1\text{st}}^{\text{ex}}$ for the $\bar{K}N_2 \rightarrow \bar{K}^{\text{ex}}N$ subprocess as $p \equiv |-\vec{p}|$ is varied. Here the incoming- \bar{K} momentum and the scattering angle of outgoing N are fixed as $|\vec{p}_{\bar{K}}| = 1$ GeV and $\theta_{pN} = 0$, respectively.

141 the prospect for future works are given in Sec. IV.

142 II. FORMULATION

143 In this section, we present the formulas for the calculations of the differential cross sections
 144 for $\bar{K} + d \rightarrow \pi + Y + N$ that can be used to compare with the data from the J-PARC E31
 145 experiment.

146 A. Kinematics and cross sections

147 We perform calculations in the laboratory (LAB) frame in which the incoming \bar{K} is in
 148 the quantization z -direction and the outgoing N is on the x - z plane. The momenta for the

149 $\bar{K} + d \rightarrow \pi + Y + N$ reaction, denoted as p_a ($a = \bar{K}, d, \pi, Y, N$), can then be written as

$$p_{\bar{K}} = (E_{\bar{K}}(\vec{p}_{\bar{K}}), 0, 0, |\vec{p}_{\bar{K}}|), \quad (3)$$

$$p_d = (m_d, \vec{0}), \quad (4)$$

$$p_{\pi} = (E_{\pi}(\vec{p}_{\pi}), \vec{p}_{\pi}), \quad (5)$$

$$p_Y = (E_Y(\vec{p}_Y), \vec{p}_Y), \quad (6)$$

$$p_N = (E_N(\vec{p}_N), |\vec{p}_N| \sin \theta_{p_N}, 0, |\vec{p}_N| \cos \theta_{p_N}), \quad (7)$$

150 where $E_a(\vec{p}_a) = (m_a^2 + \vec{p}_a^2)^{1/2}$ is the relativistic energy for a particle a with mass m_a and
 151 momentum \vec{p}_a . It is convenient to introduce the momentum \vec{q}_{π} of the outgoing π in the
 152 center-of-mass (CM) frame of the final πY subsystem. For a given invariant mass $M_{\pi Y}$ of
 153 the πY subsystem, the magnitude of \vec{q}_{π} is given by

$$|\vec{q}_{\pi}| = \frac{1}{2M_{\pi Y}} \sqrt{\lambda(M_{\pi Y}^2, m_{\pi}^2, m_Y^2)}, \quad (8)$$

154 where $\lambda(a, b, c)$ is the Källén function defined by $\lambda(a, b, c) = a^2 + b^2 + c^2 - 2ab - 2bc - 2ac$.
 155 For given $M_{\pi Y}$ and $\cos \theta_{p_N}$, $|\vec{p}_N|$ is obtained by solving $E_{\bar{K}}(\vec{p}_{\bar{K}}) + m_d = E_N(\vec{p}_N) + E_{\pi Y}$ where
 156 $E_{\pi Y} = \sqrt{M_{\pi Y}^2 + \vec{P}_{\pi Y}^2}$ and $\vec{P}_{\pi Y} \equiv \vec{p}_{\pi} + p_Y = \vec{p}_{\bar{K}} - \vec{p}_N$. The momenta \vec{p}_{π} for the outgoing π
 157 and \vec{p}_Y for the outgoing Y can then be given by

$$\vec{p}_{\pi} = \vec{q}_{\pi} + \frac{\vec{P}_{\pi Y}}{M_{\pi Y}} \left[\frac{\vec{P}_{\pi Y} \cdot \vec{q}_{\pi}}{E_{\pi Y} + M_{\pi Y}} + E_{\pi}(\vec{q}_{\pi}) \right], \quad (9)$$

158

$$\vec{p}_Y = -\vec{q}_{\pi} + \frac{\vec{P}_{\pi Y}}{M_{\pi Y}} \left[-\frac{\vec{P}_{\pi Y} \cdot \vec{q}_{\pi}}{E_{\pi Y} + M_{\pi Y}} + E_Y(\vec{q}_{\pi}) \right], \quad (10)$$

159 With the above formulas, the kinematical variables [Eqs. (3)-(7)] are completely fixed by
 160 the incoming- \bar{K} momentum $\vec{p}_{\bar{K}}$, the solid angle $\Omega_{p_N} = (\theta_{p_N}, \phi_{p_N} \equiv 0)$ of the outgoing N on
 161 the x - z plane, the solid angle $\Omega_{q_{\pi}} = (\theta_{q_{\pi}}, \phi_{q_{\pi}})$ of the outgoing π in the πY CM frame, and
 162 the πY invariant mass $M_{\pi Y}$.

163 With the normalization $\langle \vec{p}' | \vec{p} \rangle = \delta(\vec{p}' - \vec{p})$ for the plane-wave one-particle state, the
 164 unpolarized differential cross sections investigated in this work are given by

$$\frac{d\sigma}{dM_{\pi Y} d\Omega_{p_N}} = \int d\Omega_{q_{\pi}} \frac{d\sigma}{dM_{\pi Y} d\Omega_{p_N} d\Omega_{q_{\pi}}}, \quad (11)$$

165

$$\begin{aligned} \frac{d\sigma}{dM_{\pi Y} d\Omega_{p_N} d\Omega_{q_{\pi}}} &= (2\pi)^4 \frac{E_{\bar{K}}(\vec{p}_{\bar{K}})}{|\vec{p}_{\bar{K}}|} \frac{E_{\pi}(\vec{p}_{\pi}) E_Y(\vec{p}_Y) E_N(\vec{p}_N) |\vec{q}_{\pi}| |\vec{p}_N|^2}{|[E_{\bar{K}}(\vec{p}_{\bar{K}}) + m_d] |\vec{p}_N| - E_N(\vec{p}_N) |\vec{p}_{\bar{K}}| \cos \theta_{p_N}|} \\ &\times \frac{1}{(2J_d + 1)} \sum_{\text{spins}} |T_{\pi Y N, \bar{K} d}|^2, \end{aligned} \quad (12)$$

166 where $d\Omega_p = d\phi_p d\cos \theta_p$; $J_d = 1$ is the spin of the deuteron; and $T_{\pi Y N, \bar{K} d}$ is the T -matrix
 167 element for the $\bar{K} d \rightarrow \pi Y N$ reaction.

B. Model for $\bar{K}d \rightarrow \pi Y N$ reaction

As discussed in Sec. I, the cross section for the $\bar{K}d \rightarrow \pi Y N$ reaction will be calculated from the mechanisms illustrated in Fig. 3. The T -matrix element $T_{\pi Y N, \bar{K}d}$ appearing in Eq. (12) is given as a sum of contributions from the impulse ($T_{\pi Y N, \bar{K}d}^{\text{imp}}$) and \bar{K} -exchange ($T_{\pi Y N, \bar{K}d}^{\bar{K}\text{-ex}}$) processes:

$$T_{\pi Y N, \bar{K}d} = T_{\pi Y N, \bar{K}d}^{\text{imp}} + T_{\pi Y N, \bar{K}d}^{\bar{K}\text{-ex}}. \quad (13)$$

The T -matrix element for the impulse process [Fig. 3(a)] is given by

$$\begin{aligned} T_{\pi Y N, \bar{K}d}^{\text{imp}} &= \sqrt{2} \langle \pi(\vec{p}_\pi, I_\pi^z); Y(\vec{p}_Y, S_Y^z, I_Y^z); N(\vec{p}_N, S_N^z, I_N^z) | t_{\pi Y, \bar{K}N_1} | \Psi_d^{(M_d)}; \bar{K}(\vec{p}_{\bar{K}}, I_{\bar{K}}^z) \rangle \\ &= \sqrt{2} \sum_{S_{N_1}^z} T_{\pi(I_\pi^z)Y(S_Y^z, I_Y^z), \bar{K}(I_{\bar{K}}^z)N_1(S_{N_1}^z, -I_N^z)}(\vec{p}_\pi, \vec{p}_Y; \vec{p}_{\bar{K}}, -\vec{p}_N; W^{\text{imp}}) \\ &\quad \times \Psi_d^{(M_d)}(-\vec{p}_N, S_{N_1}^z, -I_N^z; \vec{p}_N, S_N^z, I_N^z), \end{aligned} \quad (14)$$

where I_a^z (S_a^z) is the quantum number for the z -component of the isospin I_a (the spin S_a) of the particle a ; and M_d is that of the deuteron spin. The factor $\sqrt{2}$ comes from the antisymmetry property of the deuteron wave function given by the following standard form:

$$\begin{aligned} \Psi_d^{(M_d)}(\vec{p}, m_{s1}, m_{t1}; -\vec{p}, m_{s2}, m_{t2}) &= \left(\frac{1}{2}m_{t1}, \frac{1}{2}m_{t2} | 00\right) \\ &\quad \times \sum_{LM_L M_s} (LM_L, 1M_s | 1M_d) \left(\frac{1}{2}m_{s1}, \frac{1}{2}m_{s2} | 1M_s\right) \\ &\quad \times Y_{LM_L}(\hat{p}) R_L(|\vec{p}|), \end{aligned} \quad (15)$$

Here $(l_1 m_1, l_2 m_2 | l m)$ is the Clebsch-Gordan coefficient for $l_1 \otimes l_2 \rightarrow l$; $Y_{LM}(\hat{p})$ is the spherical harmonics; and $R_L(|\vec{p}|)$ is the radial wave function. The radial wave function is normalized as

$$\sum_{L=0,2} \int_0^\infty p^2 dp |R_L(p)|^2 = 1. \quad (16)$$

In this work, the radial wave function, $R_L(|\vec{p}|)$ with $L = 0, 2$, is taken from Ref. [35].

The half-off-shell $\bar{K}N_1 \rightarrow \pi Y$ scattering in Eq. (14) can be related to the one in its CM frame by

$$\begin{aligned} T_{\pi(I_\pi^z)Y(S_Y^z, I_Y^z), \bar{K}(I_{\bar{K}}^z)N_1(S_{N_1}^z, -I_N^z)}(\vec{p}_\pi, \vec{p}_Y; \vec{p}_{\bar{K}}, -\vec{p}_N; W^{\text{imp}}) &= \\ \sqrt{\frac{E_\pi(\vec{q}_\pi) E_Y(-\vec{q}_\pi) E_{\bar{K}}(\vec{q}_{\bar{K}}) E_N(-\vec{q}_{\bar{K}})}{E_\pi(\vec{p}_\pi) E_Y(\vec{p}_Y) E_{\bar{K}}(\vec{p}_{\bar{K}}) E_N(-\vec{p}_N)}} T_{\pi(I_\pi^z)Y(S_Y^z, I_Y^z), \bar{K}(I_{\bar{K}}^z)N_1(S_{N_1}^z, -I_N^z)}(\vec{q}_\pi, -\vec{q}_\pi; \vec{q}_{\bar{K}}, -\vec{q}_{\bar{K}}; W^{\text{imp}}), \end{aligned} \quad (17)$$

where $\vec{q}_{\bar{K}}$ is the momentum of the incoming \bar{K} in the CM frame of the final πY system; the Lorentz-boost factor appears in the right hand side¹; and the invariant mass W^{imp} for the $\bar{K}N_1 \rightarrow \pi Y$ subprocess is defined by

$$W^{\text{imp}} = M_{\pi Y}. \quad (18)$$

¹ Strictly speaking, the Wigner rotations also take place for the particle spins through the Lorentz boost. However, those are omitted here because those do not affect the unpolarized differential cross sections considered in this work.

Furthermore, the partial-wave expansion of the amplitude in the CM frame is expressed as

$$\begin{aligned}
T_{\pi(I_{\pi}^z)Y(S_Y^z, I_Y^z), \bar{K}(I_{\bar{K}}^z)N_1(S_{N_1}^z, -I_N^z)}^{\text{CM}}(\vec{q}_{\pi}, -\vec{q}_{\pi}; \vec{q}_{\bar{K}}, -\vec{q}_{\bar{K}}; W^{\text{imp}}) = \\
\sum_{JLJ^z L_f^z L_i^z} \sum_{II^z} Y_{LL_f^z}(\hat{q}_f) Y_{LL_i^z}^*(\hat{q}_i) (LL_f^z, S_Y S_Y^z | J J^z) (LL_i^z, S_{N_1} S_{N_1}^z | J J^z) \\
\times (I_{\pi} I_{\pi}^z, I_Y I_Y^z | II^z) (I_{\bar{K}} I_{\bar{K}}^z, I_{N_1} - I_N^z | II^z) T_{\pi Y, \bar{K} N_1}^{(IJL)}(q_{\pi}, q_{\bar{K}}; W^{\text{imp}}), \quad (19)
\end{aligned}$$

184 As already mentioned, in this work we take the partial-wave amplitudes $T_{\pi Y, \bar{K} N_1}^{(IJL)}(q_{\pi}, q_{\bar{K}}; W^{\text{imp}})$
185 from the DCC model developed in Ref. [2].

186 For the \bar{K} -exchange process [Fig. 3(b)], the corresponding T -matrix element is expressed
187 as

$$\begin{aligned}
T_{\pi Y N, \bar{K} d}^{\bar{K}\text{-ex}} &= \sqrt{2} \langle \pi(\vec{p}_{\pi}, I_{\pi}^z); Y(\vec{p}_Y, S_Y^z, I_Y^z); N(\vec{p}_N, S_N^z, I_N^z) | \\
&\quad \times \hat{t}_{\pi Y, \bar{K}^{\text{ex}} N_1} \hat{G}_{\bar{K}^{\text{ex}} N N_1} \hat{t}_{\bar{K}^{\text{ex}} N, \bar{K} N_2} | \Psi_d^{(M_d)}; \bar{K}(\vec{p}_{\bar{K}}, I_{\bar{K}}^z) \rangle \\
&= \sum_{S_{N_1}^z S_{N_2}^z} \sum_{I_{\bar{K}^{\text{ex}}}^z I_{N_1}^z I_{N_2}^z} \int d\vec{p}_{\bar{K}^{\text{ex}}} \\
&\quad \times T_{\pi(I_{\pi}^z)Y(S_Y^z, I_Y^z), \bar{K}^{\text{ex}}(I_{\bar{K}^{\text{ex}}}^z)N_1(S_{N_1}^z, I_{N_1}^z)}(\vec{p}_{\pi}, \vec{p}_Y; \vec{p}_{\bar{K}^{\text{ex}}}, \vec{p}; W_{2\text{nd}}^{\text{ex}}) \\
&\quad \times \frac{1}{E - E_{\bar{K}^{\text{ex}}}(\vec{p}_{\bar{K}^{\text{ex}}}) - E_N(\vec{p}_N) - E_{N_1}(\vec{p}) + i\varepsilon} \\
&\quad \times T_{\bar{K}^{\text{ex}}(I_{\bar{K}^{\text{ex}}}^z)N(S_N^z, I_N^z), \bar{K}(I_{\bar{K}}^z)N_2(S_{N_2}^z, I_{N_2}^z)}(\vec{p}_{\bar{K}^{\text{ex}}}, \vec{p}_N; \vec{p}_{\bar{K}}, -\vec{p}; W_{1\text{st}}^{\text{ex}}) \\
&\quad \times \Psi_d^{(M_d)}(\vec{p}, S_{N_1}^z, I_{N_1}^z; -\vec{p}, S_{N_2}^z, I_{N_2}^z), \quad (20)
\end{aligned}$$

188 where $\vec{p} = \vec{p}_{\pi} + \vec{p}_Y - \vec{p}_{\bar{K}^{\text{ex}}} = \vec{p}_{\bar{K}} - \vec{p}_N - \vec{p}_{\bar{K}^{\text{ex}}}$; and E is the total scattering energy in the
189 LAB frame. $W_{1\text{st}}^{\text{ex}}$ and $W_{2\text{nd}}^{\text{ex}}$ are respectively the invariant mass for the $\bar{K} N_2 \rightarrow \bar{K}^{\text{ex}} N$ and
190 $\bar{K}^{\text{ex}} N_1 \rightarrow \pi Y$ subprocesses that describe the first and second meson-baryon interaction
191 vertices [filled squares in Fig. 3(b)] in the \bar{K} -exchange process. The explicit form of $W_{1\text{st}}^{\text{ex}}$
192 and $W_{2\text{nd}}^{\text{ex}}$ are given by

$$W_{1\text{st}}^{\text{ex}} = \sqrt{[E_{\bar{K}}(\vec{p}_{\bar{K}}) + m_d - E_{N_1}(\vec{p})]^2 - (\vec{p}_N + \vec{p}_{\bar{K}^{\text{ex}}})^2}, \quad (21)$$

193

$$W_{2\text{nd}}^{\text{ex}} = M_{\pi Y}. \quad (22)$$

194 Again, the off-shell plane-wave amplitude for the $\bar{K} N_2 \rightarrow \bar{K}^{\text{ex}} N$ and $\bar{K}^{\text{ex}} N_1 \rightarrow \pi Y$ subpro-
195 cesses are constructed with the partial-wave amplitudes generated from the DCC model [2]
196 in a way similar to Eqs. (17) and (19).

197 III. RESULTS AND DISCUSSION

198 With the model described in the previous section, we can use Eqs. (11) and (12) to
199 calculate the differential cross sections for the $K^- d \rightarrow \pi Y N$ reactions. We will first present
200 our predictions for using the forthcoming data from the J-PARC E31 experiment to examine
201 the low-lying Y^* resonances that were extracted [3] from the two DCC models, Model A
202 and Model B, of Ref. [2]. We then discuss the differences between our results with those
203 given in Refs. [31, 32, 34].

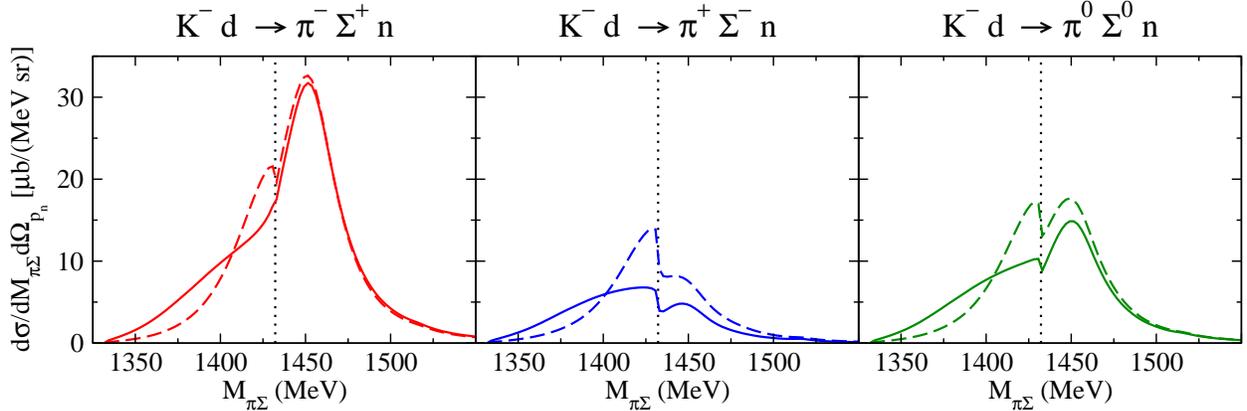


FIG. 6. Threefold differential cross section $d\sigma/(dM_{\pi\Sigma}d\Omega_{p_n})$ for the $K^-d \rightarrow \pi\Sigma n$ reactions at $|\vec{p}_{K^-}| = 1$ GeV and $\theta_{p_n} = 0$. Solid curves (dashed curves) are the full results for which the off-shell partial-wave amplitudes of Model A (Model B) of our DCC model [2] are used for the two-body meson-baryon subprocesses. Dotted vertical lines indicate the $\pi\Sigma$ invariant mass at the $\bar{K}N$ threshold.

A. Predictions for J-PARC E31 experiment

To make predictions for the J-PARC E31 experiment, we consider the kinematics that the momentum of the incoming K^- is set as $|\vec{p}_{K^-}| = 1$ GeV and the momentum of the outgoing N is chosen to be in the K^- direction with $\theta_{p_N} = 0$. We perform calculations using the $\bar{K}N \rightarrow \bar{K}N$ and $\bar{K}N \rightarrow \pi Y$ amplitudes generated from both of the DCC models (Model A and Model B) constructed in Ref. [2]. The predicted K^-d results are denoted as Model A and Model B accordingly.

First of all, we observe that the impulse process [Fig. 3(a)] gives negligible contribution at the considered kinematics with $|\vec{p}_{K^-}| = 1$ GeV and $\theta_{p_N} = 0$, and the cross sections are completely dominated by the \bar{K} -exchange process [Fig. 3(b)]. This is expected since the impulse amplitude (14) contains the deuteron wave function $\Psi_d(-\vec{p}_N, \vec{p}_N)$, which becomes very small in the considered kinematics where the momentum \vec{p}_N is very high, $|\vec{p}_N| \sim 1.2$ GeV, as indicated in Fig. 2. Therefore, in the following, our discussions are focused on the \bar{K} -exchange process.

Figure 6 shows the predicted threefold differential cross section $d\sigma/(dM_{\pi\Sigma}d\Omega_n)$ for the $K^-d \rightarrow \pi\Sigma n$ reactions. There are two noticeable features. First, there is a significant enhancement of the cross section at $M_{\pi\Sigma} \sim 1.45$ GeV. Second, a varying structure, partly due to the cusp from the opening of the $\bar{K}N$ channel, appears in the considered $M_{\pi\Sigma}$ region, and its shape depends on the model and the charge state of the final $\pi\Sigma$ system. We analyze their origins in the following.

The enhancement of the cross section in Fig. 6 at $M_{\pi\Sigma} \sim 1.45$ GeV is mainly due to the fact that the meson-baryon amplitudes are in general the largest at the on-shell kinematics and the deuteron wave function $\Psi_d(\vec{p}, -\vec{p})$ is the largest at $|\vec{p}| = 0$. At $M_{\pi\Sigma} \sim 1.45$ GeV, all of the meson-baryon subprocesses and three-body propagator in the \bar{K} -exchange process become almost on-shell when the momenta of the nucleons inside the deuteron are near $|\vec{p}| = 0$ in the integrand of Eq. (20). Thus the magnitude of \bar{K} -exchange amplitude $|T_{\pi Y N, \bar{K}d}^{\bar{K}\text{-ex}}|$ gets a large enhancement at $M_{\pi\Sigma} \sim 1.45$ GeV. This is similar to what was discussed in Ref. [34]. In fact, we confirm that the enhancement disappears if we omit the contribution

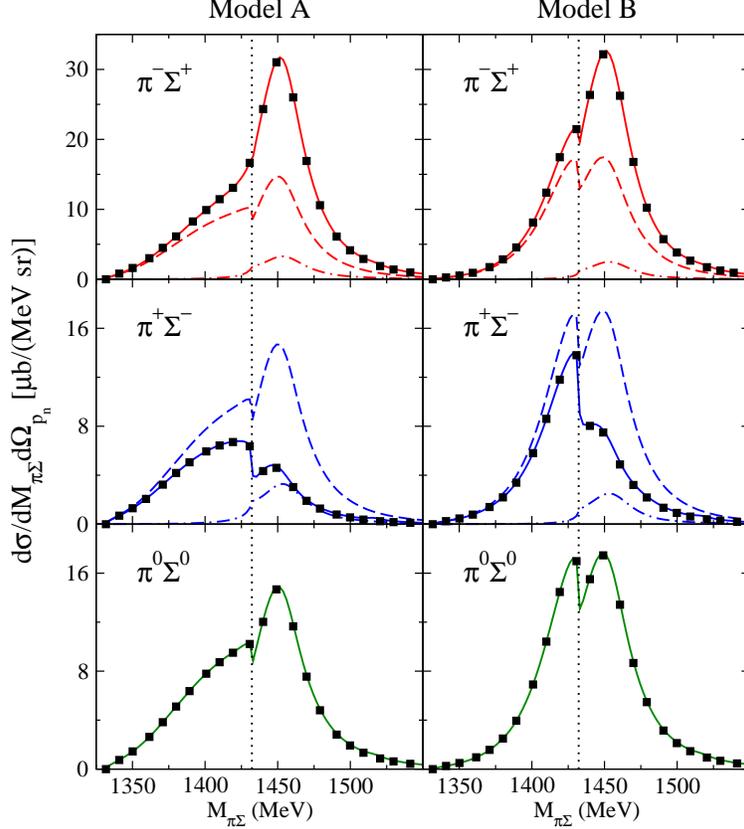


FIG. 7. Threefold differential cross section $d\sigma/(dM_{\pi\Sigma}d\Omega_{p_n})$ for the $K^-d \rightarrow \pi\Sigma n$ reactions with $|\vec{p}_{K^-}| = 1$ GeV and $\theta_{p_n} = 0$. Top, middle, and bottom panels are the results for $K^-d \rightarrow \pi^-\Sigma^+n$, $K^-d \rightarrow \pi^+\Sigma^-n$, and $K^-d \rightarrow \pi^0\Sigma^0n$, respectively. The results from Model A (Model B) are presented in left panels (right panels). Each of curves and points is: the full results (solid curves); the results in which only the S -wave amplitude (filled squares), the S_{01} amplitude (dashed curves), or the S_{11} amplitude (dashed-dotted curves) is included in $\bar{K}^{\text{ex}}N_1 \rightarrow \pi\Sigma$ of the \bar{K} -exchange process. Dotted vertical lines indicate the $\pi\Sigma$ invariant mass at the $\bar{K}N$ threshold.

from the $|\vec{p}| < 0.2$ GeV region in the loop integration in Eq. (20).

We now examine the varying structure of $d\sigma/(dM_{\pi\Sigma}d\Omega_{p_n})$ in Fig. 6. For this purpose, we first observe in Fig. 7 that the results (filled squares) from keeping only the S wave of the $\bar{K}^{\text{ex}}N_1 \rightarrow \pi\Sigma$ amplitude agree almost perfectly with the full results (solid curves). This indicates that the $\bar{K}^{\text{ex}}N_1 \rightarrow \pi\Sigma$ subprocess is completely dominated by the S -wave amplitudes in the considered kinematics. We note that this explains why a peak due to the $\Lambda(1520)3/2^-$ resonance does not appear at $M_{\pi\Sigma} \sim 1.52$ GeV in contrast to the case of the K^-p reactions. In the same figure, we also show the contributions from S_{01} (dashed curves) and S_{11} (dashed-dotted curves) partial waves² of the $\bar{K}^{\text{ex}}N_1 \rightarrow \pi\Sigma$ subprocess. Clearly, the main contributions to the full results (solid curves) are from the S_{01} wave that show the clear cusp structure near the $\bar{K}N$ threshold. However, their interference with the S_{11} wave is significant and is constructive (destructive) for the $\pi^-\Sigma^+$ ($\pi^+\Sigma^-$) production reactions. Such interference is absent for the $\pi^0\Sigma^0$ production reaction, since only the S_{01} wave of the

² The partial wave of the two-body $\bar{K} + N \rightarrow M(0^-) + B(\frac{1}{2}^+)$ reactions is denoted as L_{IJJ} , which means that the partial wave has a total angular momentum J , a total isospin I , and a parity $P = (-)^L$.

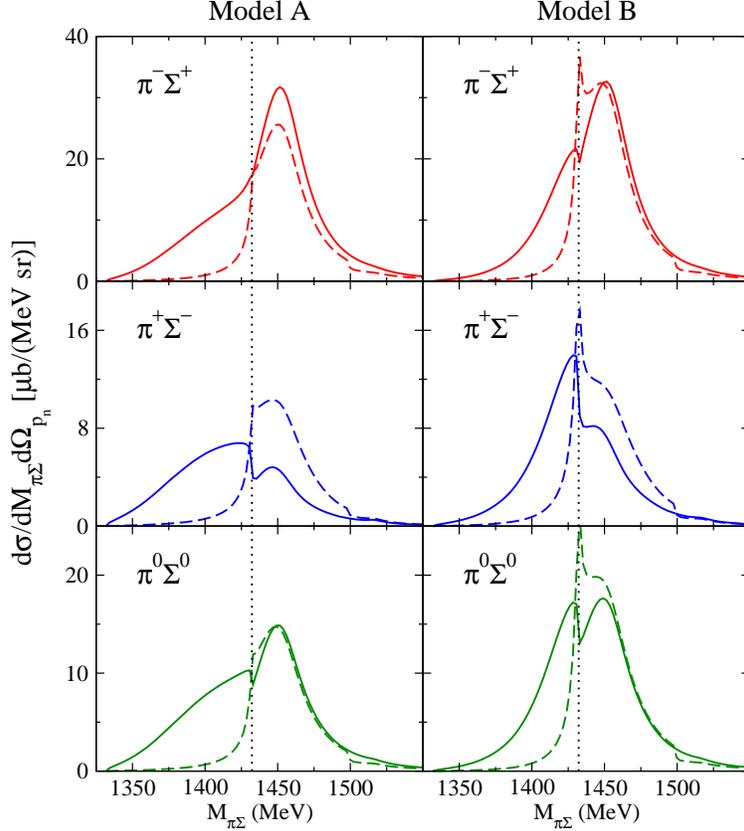


FIG. 8. Threefold differential cross section $d\sigma/(dM_{\pi\Sigma}d\Omega_{p_n})$ for the $K^-d \rightarrow \pi\Sigma n$ reactions with $|\vec{p}_{K^-}| = 1$ GeV and $\theta_{p_n} = 0$. Top, middle, and bottom panels are the results for $K^-d \rightarrow \pi^-\Sigma^+n$, $K^-d \rightarrow \pi^+\Sigma^-n$, and $K^-d \rightarrow \pi^0\Sigma^0n$, respectively. The results from Model A (Model B) are presented in left panels (right panels). Solid curves are the full results, while dashed curves are the same as solid curves except that only the nonresonant contribution is included for the S_{01} amplitude of the $\bar{K}^{\text{ex}}N_1 \rightarrow \pi\Sigma$ subprocess. Dotted vertical lines indicate the $\pi\Sigma$ invariant mass at the $\bar{K}N$ threshold.

245 $\bar{K}^{\text{ex}}N_1 \rightarrow \pi\Sigma$ subprocess can contribute to the cross section.

246 We next examine how the characteristic differences between Model A and Model B in the
 247 shape of the cross sections below the $\bar{K}N$ threshold (compare solid and dashed curves in
 248 Fig. 6) can be related to resonances in the S_{01} partial wave of the $\bar{K}^{\text{ex}}N_1 \rightarrow \pi\Sigma$ subprocess.
 249 For this purpose, we first observe in Fig. 8 that the cross sections become very small below
 250 the $\bar{K}N$ threshold if we take into account only the nonresonant contribution for the S_{01}
 251 wave of $\bar{K}^{\text{ex}}N_1 \rightarrow \pi\Sigma$. With this observation, we expect that S_{01} ($J^P = 1/2^-$) Λ resonances
 252 are actually the main contribution of the cross sections below the $\bar{K}N$ threshold and are
 253 the origin of the difference in its shape between Model A and Model B. As mentioned in
 254 Sec. I, our DCC analysis of the K^-p reactions [2] predicts two S_{01} ($J^P = 1/2^-$) Λ resonances
 255 below the $\bar{K}N$ threshold in both Model A and Model B [3], as shown in Fig. 9. Here, the
 256 higher mass pole (A1 and B1) would correspond to the $\Lambda(1405)$ resonance, while another Λ
 257 resonance with lower mass (A2 and B2) is similar to what was obtained in the chiral unitary
 258 models (see, e.g., Ref. [26]) and the Jülich model [27]. Although both Model A and Model
 259 B find two Λ resonances, their pole positions are rather different. One can see from Fig. 9

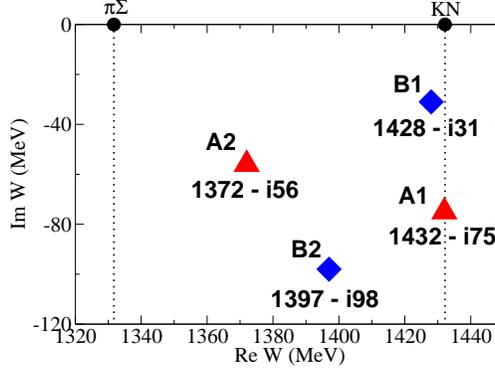


FIG. 9. Pole positions of S_{01} ($J^P = 1/2^-$) Λ resonances located below the $\bar{K}N$ threshold [3], which were extracted within the DCC models developed in Ref. [2]. Red triangles (blue diamonds) are the resonance pole positions obtained from Model A (Model B).

TABLE I. The product of coupling strengths $g_{\pi\Sigma Y^*}g_{\bar{K}NY^*}$ at pole positions for $J^P = 1/2^-$ Λ resonances located below the $\bar{K}N$ threshold. The pole mass M_R is presented as $(\text{Re}(M_R), -\text{Im}(M_R))$, and $g_{\pi\Sigma Y^*}g_{\bar{K}NY^*} = |g_{\pi\Sigma Y^*}g_{\bar{K}NY^*}|e^{i\phi}$ is presented as $(|g_{\pi\Sigma Y^*}g_{\bar{K}NY^*}|, \phi)$. The product $g_{\pi\Sigma Y^*}g_{\bar{K}NY^*}$ is defined as the residue of the T -matrix element $T_{\pi\Sigma, \bar{K}N}$ at the resonance pole position.

	Pole mass M_R (MeV)	$g_{\pi\Sigma Y^*}g_{\bar{K}NY^*}$ (MeV $^{-1}$, deg.)	$ g_{\pi\Sigma Y^*}g_{\bar{K}NY^*}/\text{Im}(M_R) ^2$ (MeV $^{-4}$)
A1	(1432, 75)	$(15.42 \times 10^{-4}, 170)$	4.23×10^{-10}
B1	(1428, 31)	$(7.94 \times 10^{-4}, 102)$	6.56×10^{-10}
A2	(1372, 56)	$(21.54 \times 10^{-4}, -24)$	14.79×10^{-10}
B2	(1397, 98)	$(13.87 \times 10^{-4}, -56)$	2.00×10^{-10}

260 that the pole A1 (B2) has larger imaginary part than the pole B1 (A2) and is far away
 261 from the real energy axis. In addition, the products of their coupling strengths to the $\pi\Sigma$
 262 and $\bar{K}N$ channels, $g_{\pi\Sigma Y^*} \times g_{\bar{K}NY^*}$, are rather different as seen in Table I. The contribution
 263 of a resonance with complex mass M_R in the $\bar{K}^{\text{ex}}N_1 \rightarrow \pi\Sigma$ subprocess to the \bar{K} -exchange
 264 amplitude $T_{\pi\Sigma n, K-d}^{\bar{K}\text{-ex}}$ can be schematically expressed at $M_{\pi\Sigma} = \text{Re}(M_R)$ as

$$\begin{aligned}
 T_{\pi\Sigma n, K-d}^{\bar{K}\text{-ex}} &\sim \left[F(M_{\pi\Sigma}) \times \frac{g_{\pi\Sigma Y^*}g_{\bar{K}NY^*}}{M_{\pi\Sigma} - M_R} + \dots \right]_{M_{\pi\Sigma}=\text{Re}(M_R)} \\
 &= F(\text{Re}(M_R)) \times \frac{g_{\pi\Sigma Y^*}g_{\bar{K}NY^*}}{i\text{Im}(M_R)} + \dots, \quad (23)
 \end{aligned}$$

265 where $F(M_{\pi\Sigma})$ is a regular function of $M_{\pi\Sigma}$ and is expected not to be much different between
 266 Model A and Model B. The value of $|g_{\pi\Sigma Y^*}g_{\bar{K}NY^*}/\text{Im}(M_R)|^2$ can therefore be used to measure
 267 the effect of a resonance on the cross section. In the third column of Table I, we see that
 268 $|g_{\pi\Sigma Y^*}g_{\bar{K}NY^*}/\text{Im}(M_R)|^2$ of the resonance B1 is larger than that of A1. Thus B1 has larger
 269 effects than A1 on the cross sections near the $\bar{K}N$ threshold, as can be seen from clear peaks
 270 in the cross sections at $M_{\pi\Sigma} \sim 1.42$ GeV that appear only in Model B. At lower energy, the
 271 cross sections are influenced by the second resonances A2 and B2. From Table I, we see that
 272 $|g_{\pi\Sigma Y^*}g_{\bar{K}NY^*}/\text{Im}(M_R)|^2$ of the resonance A2 is much larger than that of B2. This explains

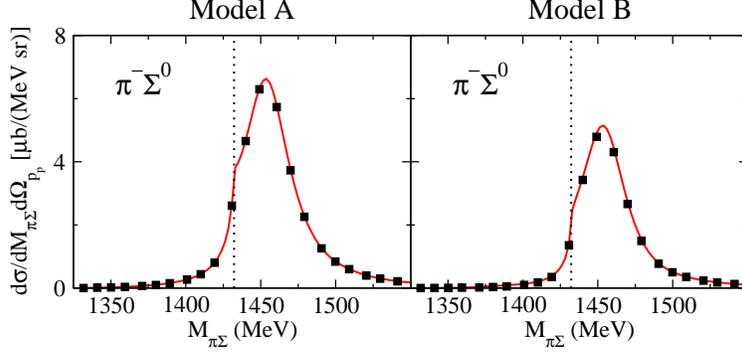


FIG. 10. Threefold differential cross section $d\sigma/(dM_{\pi\Sigma}d\Omega_{pp})$ for the $K^-d \rightarrow \pi^-\Sigma^0 p$ reaction at $|\vec{p}_{K^-}| = 1$ GeV and $\theta_{pp} = 0$. The results from Model A (Model B) are presented in the left panel (right panel). Solid curves are the full results, while filled squares are the results in which only the S_{11} amplitude is included for $\bar{K}^{\text{ex}}N_1 \rightarrow \pi\Sigma$ of the \bar{K} -exchange process. Dotted vertical lines indicate the $\pi\Sigma$ invariant mass at the $\bar{K}N$ threshold.

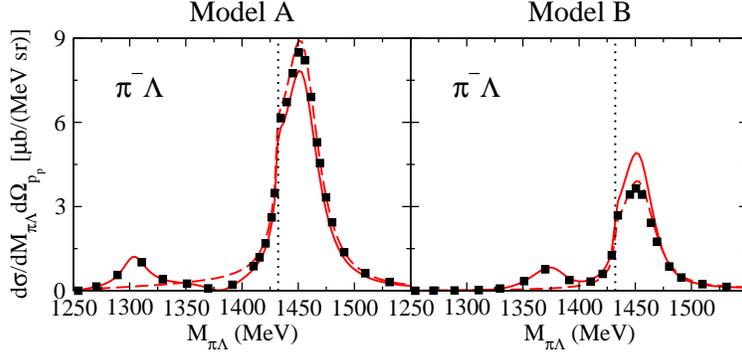


FIG. 11. Threefold differential cross section $d\sigma/(dM_{\pi\Lambda}d\Omega_{pp})$ for the $K^-d \rightarrow \pi^-\Lambda p$ reaction at $|\vec{p}_{K^-}| = 1$ GeV and $\theta_{pp} = 0$. The results from Model A (Model B) are presented in the left panel (right panel). Each of curves and points is: the full results (solid curves); the results in which only the S_{11} amplitude (dashed curves) or the S_{11} and P_{13} amplitudes (filled squares) is included for $\bar{K}^{\text{ex}}N_1 \rightarrow \pi\Lambda$ of the \bar{K} -exchange process. Dotted vertical lines indicate the $\pi\Lambda$ invariant mass at the $\bar{K}N$ threshold.

273 why the cross sections at $M_{\pi\Sigma} \lesssim 1.4$ GeV in Model A are larger than Model B.

274 We now turn to presenting the predicted cross sections for $K^-d \rightarrow \pi^-\Sigma^0 p$ and $K^-d \rightarrow$
 275 $\pi^-\Lambda p$ at the same kinematics $|\vec{p}_{K^-}| = 1$ GeV and $\theta_{pp} = 0$. Since the $\pi^-\Sigma^0$ and $\pi^-\Lambda$ states
 276 contain only the isospin $I = 1$ component, these reactions will be useful for investigating the
 277 low-lying Σ resonances. It is noted that the data for such reactions can also be obtained by
 278 extending the measurements of the the J-PARC E31 experiment [39]. Similar to the results
 279 for the $K^-d \rightarrow \pi\Sigma n$ reactions presented above, we find that (a) the impulse process gives
 280 negligible contribution to the cross sections for both $K^-d \rightarrow \pi^-\Sigma^0 p$ and $K^-d \rightarrow \pi^-\Lambda p$, and
 281 (b) the characteristic enhancement appears at $M_{\pi Y} \sim 1.45$ GeV as seen in Figs. 10 and 11.

282 For $K^-d \rightarrow \pi^-\Sigma^0 p$, we find that the $\bar{K}^{\text{ex}}N_1 \rightarrow \pi\Sigma$ subprocess is completely dominated
 283 by the S_{11} amplitude. This is shown in Fig. 10. We see that the results (filled squares)
 284 from the calculations keeping only the S_{11} amplitude of the $\bar{K}^{\text{ex}}N_1 \rightarrow \pi\Sigma$ subprocess agree
 285 almost perfectly with the results (solid curves) from the calculations including all partial

286 waves. The cross section becomes very small below the $\bar{K}N$ threshold, and this would
 287 be because no resonance exists in the S_{11} wave in the corresponding energy region. It is
 288 found that Model B shows the cross section $\sim 20\%$ smaller than Model A at its maximum
 289 ($M_{\pi\Sigma} \sim 1.45$ GeV). Since the on-shell S_{11} amplitudes for the $\bar{K}^{\text{ex}}N_1 \rightarrow \pi\Sigma$ subprocess are
 290 not much different between the two models at $M_{\pi\Sigma} \sim 1.45$ GeV [2], the difference in the
 291 magnitude of the $K^-d \rightarrow \pi^-\Sigma^0p$ cross section might partly come from that in the off-shell
 292 behavior of the $\bar{K}^{\text{ex}}N_1 \rightarrow \pi\Sigma$ subprocess.

293 The predicted differential cross sections for the $K^-d \rightarrow \pi^-\Lambda p$ reaction are given in
 294 Fig. 11. By comparing the solid and filled squares, it is clear that the S_{11} and P_{13} waves of
 295 the $\bar{K}^{\text{ex}}N_1 \rightarrow \pi\Lambda$ subprocess completely dominate the cross section in the region below the
 296 $\bar{K}N$ threshold. A resonance corresponding to $\Sigma(1385)3/2^+$ in the P_{13} wave was identified
 297 in both Model A and Model B. For Model B (the right panel of Fig. 11), there is a peak at
 298 $M_{\pi\Lambda} \sim 1.38$ GeV, where the contribution from the S_{11} amplitude is very weak. On the other
 299 hand, we find that in Model A the S_{11} -wave contribution and the P_{13} -wave contribution from
 300 $\Sigma(1385)3/2^+$ are comparable and interfere destructively, and, as a result, a dip is produced
 301 at $M_{\pi\Lambda} \sim 1.38$ GeV. We find that Model A has another P_{13} resonance with lower mass than
 302 $\Sigma(1385)3/2^+$. This is the origin of the peak at $M_{\pi\Lambda} \sim 1.3$ GeV in the left panel of Fig. 11.
 303 These kinds of visible differences between Model A and Model B can occur below the $\bar{K}N$
 304 threshold, because at present our DCC models for the $\bar{K}N$ reactions have been constructed
 305 by fitting only to the K^-p reaction data. We expect that such a different behavior of the
 306 two-body subprocesses below the $\bar{K}N$ threshold, which cannot be directly constrained by
 307 the $\bar{K}N$ reaction data, needs to be judged by the data of $\bar{K}d$ reactions. The upcoming data
 308 from the J-PARC E31 experiment are thus highly desirable to improve our DCC models in
 309 the $S = -1$ sector.

310 We also see in Fig. 11 that above the $\bar{K}N$ threshold, the P_{13} wave of the $\bar{K}^{\text{ex}}N_1 \rightarrow \pi\Lambda$
 311 subprocess is negligible and the main contribution to the cross section comes from the S_{11}
 312 wave. However, the behavior of the S_{11} partial-wave amplitudes for $\bar{K}N \rightarrow \pi\Lambda$ is rather
 313 different between Model A and Model B at $W \lesssim 1.7$ GeV (see Fig. 27 in Ref. [2]), and this
 314 is the origin of the the sizable difference in the magnitude of the cross section above the
 315 $\bar{K}N$ threshold. For Model A (left panel), the difference between the solid and dashed curves
 316 are quite small, and hence the cross section above the $\bar{K}N$ threshold is almost completely
 317 dominated by the S_{11} wave. On the other hand, this difference is about 30% for Model
 318 B (right panel) and is found to come from a P_{11} ($J^P = 1/2^+$) Σ resonance with pole
 319 mass $M_R = 1457 - i39$ MeV [3]. This resonance might correspond to the one-star $\Sigma(1480)$
 320 resonance assigned by PDG [6]. At present this resonance was found only in Model B, and
 321 this is why the contribution of P_{11} wave is negligible in the $K^-d \rightarrow \pi^-\Lambda p$ cross section for
 322 Model A.

323 The above result suggests that the $K^-d \rightarrow \pi^-\Lambda p$ cross section may provide a useful
 324 constraint for judging this unestablished low-lying Σ resonance with spin-parity $J^P = 1/2^+$.
 325 To investigate this, we examine the threefold differential cross sections at different values
 326 of the incoming- \bar{K} momentum. In Fig. 12, we present $d\sigma/(dM_{\pi\Lambda}d\Omega_{p_p})$ at $|\vec{p}_{\bar{K}}| = 1$ GeV
 327 and 0.7 GeV. We find that the interference pattern in the cross section changes as $|\vec{p}_{\bar{K}}|$
 328 changes. For the cross section at $|\vec{p}_{\bar{K}}| = 1$ GeV, the contribution from the P_{11} wave of the
 329 $\bar{K}^{\text{ex}}N_1 \rightarrow \pi\Lambda$ subprocess shows a constructive interference with the other contributions,
 330 while at $|\vec{p}_{\bar{K}}| = 0.7$ GeV, it shows a destructive interference. This visible difference of
 331 the interference pattern originating from the P_{11} wave of the $\bar{K}^{\text{ex}}N_1 \rightarrow \pi\Lambda$ subprocess will
 332 provide critical information for judging the unestablished $J^P = 1/2^+$ Σ resonance. Therefore

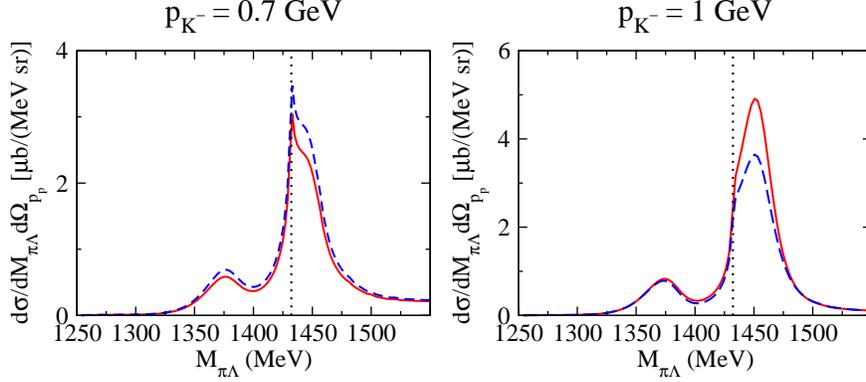


FIG. 12. Threefold differential cross section $d\sigma/(dM_{\pi\Lambda}d\Omega_{p_p})$ for the $K^-d \rightarrow \pi^-\Lambda p$ reaction at $\theta_{p_p} = 0$, computed with Model B. The left (right) panel is the result at $|\vec{p}_{K^-}| = 0.7$ GeV ($|\vec{p}_{K^-}| = 1$ GeV). Solid curves are the full results, while dashed curves are the results in which the P_{11} amplitude for $\bar{K}^{\text{ex}}N_1 \rightarrow \pi\Lambda$ in the \bar{K} -exchange process is turned off. Dotted vertical lines indicate the $\pi\Lambda$ invariant mass at the $\bar{K}N$ threshold.

333 it is highly desirable to measure the $K^-d \rightarrow \pi^-\Lambda p$ cross section for several $|\vec{p}_{K^-}|$ values.

334 B. Comparison with the results from the S -wave $\bar{K}N$ models

335 The differential cross sections at $|\vec{p}_{K^-}| = 1$ GeV are also predicted in Ref. [34]. We first
 336 note that our predicted cross sections shown in Fig. 6 are much larger than those given
 337 in Fig. 12 of Ref. [34]. We find that it is mainly due to the large difference between the
 338 amplitudes used in the calculations of $\bar{K}N_2 \rightarrow \bar{K}^{\text{ex}}N$ in the \bar{K} -exchange process [Fig. 3(b)],
 339 where the incoming \bar{K} has a large momentum. As seen in Fig. 5, the S -wave $\bar{K}N$ model
 340 used in Ref. [34] underestimates the $\bar{K}N \rightarrow \bar{K}N$ cross section greatly in the invariant-mass
 341 region around $W = 1.8$ GeV, which is covered in the loop integration of Eq. (20) over
 342 the momentum of the nucleon in the deuteron. In such a high- W region far beyond the
 343 $\bar{K}N$ threshold, it is necessary to include the higher partial-wave contributions. This can be
 344 understood from Fig. 5 where we compare the $K^-p \rightarrow \bar{K}^0n$ cross sections from our DCC
 345 model and the two S -wave models of Refs. [34, 38]. If we keep only the S -wave part of
 346 the amplitude in our calculation, our results (solid curve) in Fig. 5 are actually reduced to
 347 the values close to the results (dot-dashed and dotted curves) of the two S -wave models.
 348 Accordingly, we see in Fig. 13 that the magnitude of $d\sigma/(dM_{\pi\Sigma}d\Omega_{p_n})$ for the $K^-d \rightarrow \pi\Sigma n$
 349 reactions are drastically reduced if we include only the S -wave amplitudes for $\bar{K}N_2 \rightarrow \bar{K}^{\text{ex}}N$
 350 in the \bar{K} -exchange process. This result indicates that the use of appropriate amplitudes that
 351 reproduce the $\bar{K}N$ reactions up to a very high energy is inevitable for obtaining the K^-d
 352 reaction cross sections that are comparable with the experimental data. The same argument
 353 would also apply to the other studies of the K^-d reaction [31–33], where the amplitudes for
 354 the meson-baryon subprocesses are obtained by fitting only to the near-threshold data of $\bar{K}N$
 355 reactions. It is noted that the higher-order scattering processes were also taken into account
 356 in Ref. [34]. By performing calculations using their S -wave $\bar{K}N$ model, however, we confirm
 357 that in the considered kinematics their results are nearly saturated by the impulse and \bar{K} -
 358 exchange processes and the higher-order effects seem subdominant. Therefore, the use of
 359 appropriate $\bar{K}N$ scattering amplitudes, which can make the K^-d reaction cross sections

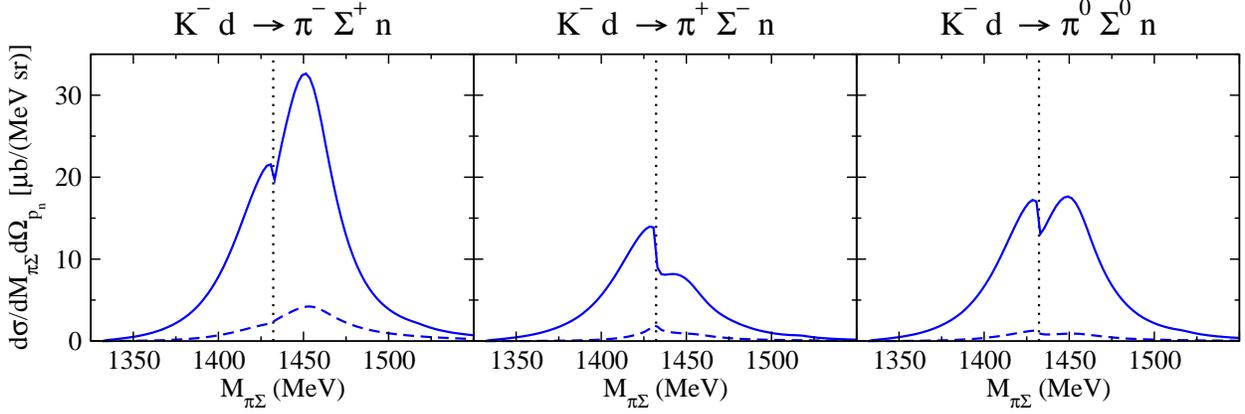


FIG. 13. Threefold differential cross section $d\sigma/(dM_{\pi\Sigma}d\Omega_{p_n})$ for the $K^-d \rightarrow \pi\Sigma n$ reactions at $|\vec{p}_{K^-}| = 1$ GeV and $\theta_{p_n} = 0$. Solid curves represent the full result, while dashed curves represent the results in which only the S -wave amplitudes are included for $\bar{K}N_2 \rightarrow \bar{K}^{\text{ex}}N$ of the \bar{K} -exchange process. Dotted vertical lines indicate the $\pi\Sigma$ invariant mass at the $\bar{K}N$ threshold.

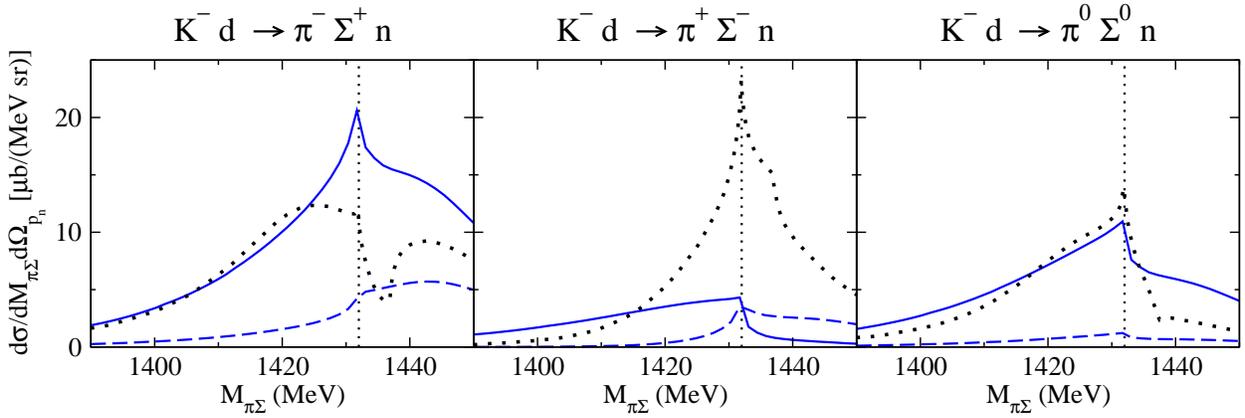


FIG. 14. Threefold differential cross section $d\sigma/(dM_{\pi\Sigma}d\Omega_{p_n})$ for the $K^-d \rightarrow \pi\Sigma n$ reactions at $|\vec{p}_{K^-}| = 0.6$ GeV and $\theta_{p_n} = 0$. Solid curves are the full results from our Model B, while dashed curves are the results from Model B in which only the the S -wave amplitudes are included for all meson-baryon subprocesses. Dotted curves are the results in Ref. [31], where the S -wave $\bar{K}N$ model developed in Ref. [38] are used for calculating the meson-baryon subprocesses. Dotted vertical lines indicate the $\pi\Sigma$ invariant mass at the $\bar{K}N$ threshold.

360 order(s) of magnitude larger, seems more important than the higher-order effects.

361 We next compare our results at $|\vec{p}_{K^-}| = 0.6$ GeV with those given in Ref. [31]. In Fig. 14,
 362 we see that our “ S -wave only” results at $|\vec{p}_{K^-}| = 0.6$ GeV are much smaller than the results
 363 in Ref. [31]. The results in Ref. [31] are even comparable or larger than our full results
 364 in which higher partial waves are also included. This can be understood from Fig. 15.
 365 For the $\bar{K}N_2 \rightarrow \bar{K}^{\text{ex}}N$ subprocess, the $K^-p \rightarrow \bar{K}^0n$ and $K^-n \rightarrow K^-n$ charge states can
 366 contribute. We see that at $W \sim 1.6$ GeV, which corresponds to a typical invariant mass of
 367 the $\bar{K}N_2 \rightarrow \bar{K}^{\text{ex}}N$ subprocess for $|\vec{p}_{K^-}| = 0.6$ GeV, the S -wave $\bar{K}N$ model used in Ref. [31]
 368 gives a large cross section for $K^-n \rightarrow K^-n$, which is even larger than our full results. Since
 369 all the $\bar{K}N$ models give similar cross sections near the threshold, we can conclude that this

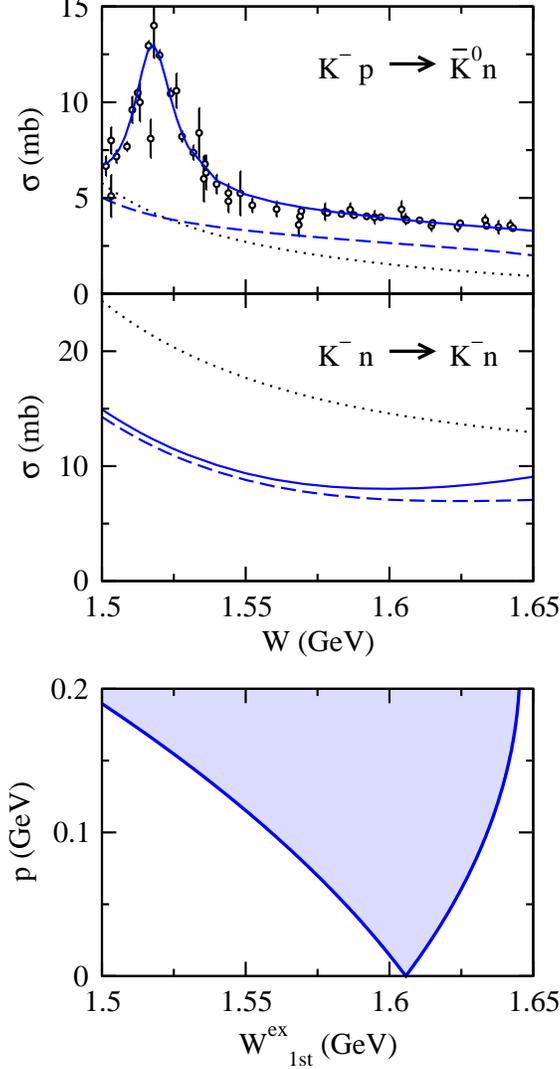


FIG. 15. Upper panel: Total cross section for $K^- p \rightarrow \bar{K}^0 n$ in the energy region relevant to the $\bar{K} N_2 \rightarrow \bar{K}^{ex} N$ subprocess in the \bar{K} -exchange process [Fig. 3(b)] for the case of $|\vec{p}_{\bar{K}}| = 0.6$ GeV and $\theta_{p_N} = 0$. Solid (dashed) curve is the full (S -wave only) result from Model B of Ref. [2], while dotted curve is from the model developed in Ref. [38] that was used for the calculation in Refs. [31–33]. Middle panel: Same as the upper panel but for $K^- n \rightarrow \bar{K}^- n$. Lower panel: Allowed ranges of the invariant mass W_{1st}^{ex} for the $\bar{K} N_2 \rightarrow \bar{K}^{ex} N$ subprocess as $p \equiv |-\vec{p}|$ is varied. Here the incoming- \bar{K} momentum and the scattering angle of outgoing N are fixed as $|\vec{p}_{\bar{K}}| = 0.6$ GeV and $\theta_{p_N} = 0$.

370 is the origin of the large $K^- d \rightarrow \pi \Sigma n$ reaction cross section found in Ref. [31]. Furthermore,
 371 the $K^- n \rightarrow K^- n$ cross sections are larger than $K^- p \rightarrow K^0 n$ cross sections and thus has
 372 a larger contribution to the \bar{K} -exchange amplitudes. This is why the result from Ref. [31]
 373 has a large cross section for $K^- d \rightarrow \pi \Sigma n$ at $p_K = 0.6$ GeV. This observation also indicates
 374 that one must use the $\bar{K} N$ amplitudes that are well tested by the $\bar{K} N$ reaction data up to
 375 a high energy region far beyond the $\bar{K} N$ threshold.

376 **IV. SUMMARY AND FUTURE DEVELOPMENTS**

377 Aiming at establishing low-lying Y^* resonances through analyzing the forthcoming data
 378 from the J-PARC E31 experiment, we have developed a model for the $\bar{K}d \rightarrow \pi YN$ reac-
 379 tion. At the kinematics of this experiment that the outgoing nucleon is in the direction
 380 of the incoming \bar{K} , the cross sections for this reaction are dominated by the \bar{K} -exchange
 381 mechanism. The amplitudes of this \bar{K} -exchange process are calculated in our approach by
 382 using the off-shell amplitudes of $\bar{K}N \rightarrow \bar{K}N$ and $\bar{K}N \rightarrow \pi Y$ generated from the dynamical
 383 coupled-channels (DCC) model developed in Ref. [2]. This DCC model was constructed
 384 by fitting the existing data of $K^-p \rightarrow \bar{K}N, \pi\Sigma, \pi\Lambda, \eta\Lambda, K\Xi$ reactions over the wide energy
 385 region from the thresholds up to $W = 2.1$ GeV.

386 Most previous works used elementary meson-baryon amplitudes that were constructed
 387 by fitting only to the $\bar{K}N$ reaction data near the threshold. However, we have shown that if
 388 the incoming- \bar{K} momentum is rather high as in the case of the J-PARC E31 experiment, the
 389 use of such amplitudes would result in the cross section that is order(s) of magnitude smaller
 390 than the one calculated using the appropriate meson-baryon amplitudes that reproduce the
 391 $\bar{K}N$ reactions in the energy region far beyond the $\bar{K}N$ threshold. This is because the meson-
 392 baryon subprocess produced by the reaction between the incoming \bar{K} and the nucleon inside
 393 of the deuteron can have a very high invariant mass, even if the invariant mass of the final
 394 πY system is quite low.

395 We have shown that the $\bar{K}d \rightarrow \pi YN$ reactions are useful for studying low-lying Y^*
 396 resonances. In fact, by comparing the results between our two models, Model A and Model B,
 397 we have found that the behavior of the threefold differential cross sections for $K^-d \rightarrow \pi\Sigma n$
 398 [$K^-d \rightarrow \pi^-\Lambda p$] below the $\bar{K}N$ threshold are sensitive to the existence and position of the
 399 S_{01} resonance poles including $\Lambda(1405)1/2^-$ [the P_{13} resonance poles including $\Sigma(1385)3/2^+$].
 400 We have also demonstrated that the $K^-d \rightarrow \pi^-\Lambda p$ reaction data would provide useful
 401 information for judging the existence of an unestablished low-lying $J^P = 1/2^+$ Σ resonance
 402 with the pole mass $M_R = 1457 - i39$ MeV, which is currently found only in Model B.

403 Here we note that we have followed the previous works [31–33] to consider only the
 404 impulse and \bar{K} -exchange processes and ignore other higher-order three-particle final state
 405 interactions. One possible important correction is the π -exchange mechanism when the
 406 invariant mass of the outgoing πN state in the final πYN state is near the $\Delta(1232)$ region.
 407 We have found that it has negligible effects to change our results in the considered special
 408 kinematics shown in Fig. 1. Nevertheless, our results on the differences between Models A
 409 and B should be further quantified by performing the complete three-particle calculation.
 410 This is, however, rather difficult within the framework using the $\bar{K}N$ amplitudes of the DCC
 411 model of Ref. [2] mainly because of the presence of multi-channel final states, such as $\pi\Lambda N$,
 412 $\pi\Sigma N$, $\eta\Lambda N$, and $K\Xi N$, and of the non-separable nature of our meson-baryon amplitudes,
 413 which is different from those used in Ref. [34] where the separable nature of the two-body
 414 amplitudes was a key to solving the three-body scattering equation. Clearly, this requires a
 415 separated long-term effort.

416 A necessary and immediate next step towards constructing a reliable $\bar{K}d$ reaction model
 417 that can be used for the spectroscopic study of low-lying Y^* resonances would be to include
 418 the baryon-exchange processes in addition to \bar{K} - and π -exchange processes, so that we can
 419 apply our $\bar{K}d$ reaction model to wider kinematical region. Also, the inclusion of baryon-
 420 exchange process would make our model applicable to the study of YN and YY interactions,
 421 where the latter is quite interesting in relation to a possible existence of the H dibaryons.

422 Our investigations in this direction will be presented elsewhere.

423 ACKNOWLEDGMENTS

424 The authors would like to thank Dr. S. Ohnishi for illuminating discussions on his recent
425 studies of $K^-d \rightarrow \pi\Sigma n$. H.K. would also like to thank Prof. H. Noumi for useful commu-
426 nications on the status of the J-PARC E31 experiment. This work was supported by the
427 Japan Society for the Promotion of Science (JSPS) KAKENHI Grant No. 25800149, and by
428 the U.S. Department of Energy, Office of Nuclear Physics Division, under Contract No. DE-
429 AC02-06CH11357. This research used resources of the National Energy Research Scientific
430 Computing Center and resources provided on Blues and Fusion, high-performance comput-
431 ing cluster operated by the Laboratory Computing Resource Center at Argonne National
432 Laboratory.

-
- 433 [1] H. Zhang, J. Tulpan, M. Shrestha, and D. M. Manley, Phys. Rev. C **88**, 035204 (2013); 035205
434 (2013).
- 435 [2] H. Kamano, S. X. Nakamura, T.-S. H. Lee, and T. Sato, Phys. Rev. C **90**, 065204 (2014).
- 436 [3] H. Kamano, S. X. Nakamura, T.-S. H. Lee, and T. Sato, Phys. Rev. C **92**, 025205 (2015).
- 437 [4] C. Fernandez-Ramirez, I. V. Danilkin, D. M. Manley, V. Mathieu, and A. P. Szczepaniak,
438 Phys. Rev. D **93**, 034029 (2016).
- 439 [5] R. de la Madrid, Nucl. Phys. **A812**, 13 (2008); R. de la Madrid and M. Gadella, Am. J. Phys.
440 **70**, 626 (2002); references therein.
- 441 [6] K. A. Olive *et al.* (Particle Data Group), Chin. Phys. C **38**, 090001 (2014).
- 442 [7] D. J. Wilson, J. J. Dudek, R. G. Edwards, and C. E. Thomas, Phys. Rev. D **91** 054008 (2015);
443 D. J. Wilson, R. A. Briceno, J. J. Dudek, R. G. Edwards, and C. E. Thomas, Phys. Rev. D
444 **92**, 094502 (2015); J. J. Dudek, R. G. Edwards, and D. J. Wilson, Phys. Rev. D **93**, 094506
445 (2016).
- 446 [8] J. M. M. Hall, A. C.-P. Hsu, D. B. Leinweber, A. W. Thomas, and R. D. Young, Phys. Rev.
447 D **87**, 094510 (2013); J. J. Wu, T.-S. H. Lee, A. W. Thomas, and R. D. Young, Phys. Rev.
448 C **90**, 055206 (2014); Z. W. Liu, W. Kamleh, D. B. Leinweber, F. M. Stokes, A. W. Thomas,
449 and J. J. Wu, Phys. Rev. Lett. **116**, 082004 (2016).
- 450 [9] R. Molina and M. Döring, arXiv:1512.05831.
- 451 [10] A. Matsuyama, T. Sato, and T.-S. H. Lee, Phys. Rep. **439**, 193 (2007).
- 452 [11] B. Juliá-Díaz, T.-S. H. Lee, A. Matsuyama, and T. Sato, Phys. Rev. C **76**, 065201 (2007).
- 453 [12] B. Juliá-Díaz, T.-S. H. Lee, A. Matsuyama, T. Sato, and L. C. Smith, Phys. Rev. C **77**, 045205
454 (2008).
- 455 [13] J. Durand, B. Julia-Diaz, T.-S. H. Lee, B. Saghai, and T. Sato, Phys. Rev. C **78**, 025204
456 (2008).
- 457 [14] H. Kamano, B. Juliá-Díaz, T.-S. H. Lee, A. Matsuyama, and T. Sato, Phys. Rev. C **79**, 025206
458 (2009).
- 459 [15] B. Juliá-Díaz, H. Kamano, T.-S. H. Lee, A. Matsuyama, T. Sato, and N. Suzuki, Phys. Rev.
460 C **80**, 025207 (2009).

- 461 [16] H. Kamano, B. Juliá-Díaz, T.-S. H. Lee, A. Matsuyama, and T. Sato, Phys. Rev. C **80**, 065203
462 (2009).
- 463 [17] N. Suzuki, B. Juliá-Díaz, H. Kamano, T.-S. H. Lee, A. Matsuyama, and T. Sato, Phys. Rev.
464 Lett. **104**, 042302 (2010).
- 465 [18] N. Suzuki, T. Sato, and T.-S. H. Lee, Phys. Rev. C **82** 045206 (2010).
- 466 [19] H. Kamano, S. X. Nakamura, T.-S. H. Lee, and T. Sato, Phys. Rev. C **81**, 065207 (2010).
- 467 [20] H. Kamano, S. X. Nakamura, T.-S. H. Lee, and T. Sato, Phys. Rev. D **86**, 097503 (2012).
- 468 [21] H. Kamano, S. X. Nakamura, T.-S. H. Lee, and T. Sato, Phys. Rev. C **88**, 035209 (2013).
- 469 [22] H. Kamano, Phys. Rev. C **88**, 045203 (2013).
- 470 [23] S. X. Nakamura, H. Kamano, and T. Sato, Phys. Rev. D **92**, 074024 (2015).
- 471 [24] H. Kamano, S. X. Nakamura, T.-S. H. Lee, and T. Sato, Phys. Rev. C **94**, 015201 (2016).
- 472 [25] J. A. Oller and U.-G. Meißner, Phys. Lett. **B500**, 263 (2001).
- 473 [26] Y. Ikeda, T. Hyodo, D. Jido, H. Kamano, T. Sato, and K. Yazaki, Prog. Theor. Phys. **125**,
474 1205 (2011).
- 475 [27] J. Haidenbauer, G. Krein, U.-G. Meißner, and L. Tolos, Eur. Phys. J. A **47**, 18 (2011).
- 476 [28] M. L. Goldberger and K. M. Watson, *Collision Theory* (John Wiley & Sons, New York, 1964).
- 477 [29] H. Feshbach *Theoretical Nuclear Physics, Nuclear Reactions* (Wiley, New York, 1992).
- 478 [30] H. Noumi *et al.*, Spectroscopic study of hyperon resonances below $\bar{K}N$ threshold via the
479 (K^-, n) reaction on deuteron (J-PARC E31),
480 http://j-parc.jp/researcher/Hadron/en/pac_1207/pdf/E31_2012-9.pdf .
- 481 [31] K. Miyagawa and J. Haidenbauer, Phys. Rev. C **85**, 065201 (2012).
- 482 [32] D. Jido, E. Oset, and T. Sekihara, Eur. Phys. J. A **42**, 257 (2009); **49**, 95 (2013);
- 483 [33] J. Yamagata-Sekihara, T. Sekihara, and D. Jido, PTEP **2013**, 043D02 (2013).
- 484 [34] S. Ohnishi, Y. Ikeda, T. Hyodo, and W. Weise, Phys. Rev. C **93**, 025207 (2016).
- 485 [35] R. B. Wiringa, V. G. J. Stoks, and R. Schiavilla Phys. Rev. C **51**, 38 (1995)
- 486 [36] E. O. Alt, P. Grassberger, and W. Sandhas, Nucl. Phys. **B2**, 167 (1967).
- 487 [37] J. J. Wu, T. Sato and T.-S. H. Lee, Phys. Rev. C **91**, 035203 (2015).
- 488 [38] E. Oset and A. Ramos, Nucl. Phys. **A635**, 99 (1998).
- 489 [39] H. Noumi (private communication).